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ORBIT DIFFERENTIAL CORRECTION - TRACKING PROGRAM

Volume I - Differential Correction Geocentric Orbit Computations Program

George E. Townsend

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FOREWORD

The Space and Information Systems Division (S&ID) of North American Aviation, Inc. (NAA) under Contract AF 30(602)-3638 with the Rome Air Development Center (RADC) of the United States Air Force agreed to perform a 10-month study designed to develop digital computer techniques in two areas of interest to the RADC tracking facility. First, a differential correction geocentric orbit computation program for reducing observed data was to be prepared which would operate in a near-optimum manner at the RADC computer center. Secondly, a computational logic which could be utilized in the tracking process for driving the tracking antennae in an open-loop mode was to be prepared. This second program would employ general perturbations theory in the definition of the predicted trajectory. (This latter task is reported in SID 65-1203-3).

This report was prepared as partial documentation of the first task. The contents present the program logic and FØRTRAN listings for the main body of the required program. The remaining portion of the logic for this program is associated with the identification, ordering, and smoothing of the raw data; this information is presented in the discussion of the processor in a separate document (SID 65-1203-2). This document should be reviewed carefully, since the interface between the two portions of the differential corrections orbit computation program is a magnetic tape containing the smoothed data in a compatible format.

The differential corrections program (DCP) is designed in such a manner that residuals associated with any one of the six types of data

- 1. Range
- 2. Range-Rate
- 3. Azimuth and Elevation
- 4. Range and Range-Rate
- 5. Range, Azimuth, and Elevation
- 6. Range-Rate, Azimuth, and Elevation

(defined by differencing the observed data and a computed set evaluated on the best estimate of the trajectory) are minimized in the sense of minimum variance. When this operation is accomplished (recursively), the nominal trajectory is adjusted. Thus, after processing data acquired over some as yet unspecified interval of time, the trajectory will be known to an accuracy sufficient to allow it to be predicted with confidence. At this time, data can be prepared to allow the program developed as the second task in this contract to be activated to acquire more data. In a sense, then, the system would be self-perpetuating.

Complete discussions of the program logic, and operation of the DCP will be presented in the various sections of this document. However, the most informative

discussions for the user will probably be included in the analysis of the sample problem (section 3.). This conclusion is based on the fact that complete descriptions of program input, program operation, and program output for a real problem are included. The remaining portion of the document will be a necessary part of the library of the programmer who wishes to modify or adapt the program to another use and of the individual who wishes to fully comprehend the rationale which is mechanized.

This contract has been managed at NAA S&ID by Mr. J. A. Hill and directed by Mr. G. E. Townsend. Mr. Townsend also designed the rationale for the program, coded the major portion of the logic, performed the preliminary checks of the operation, and prepared this document. Final checkout of the program was accomplished with the aid of Mr. C. C. DeBilzan.

The assistance offered by RADC personnel under the direction of Mr. Gordon Negus (Program Manager) is gratefully acknowledged. RADC Project 4519 applies.

This technical report has been reviewed and is approved.

Approved: Gordon & Negres Project Engineer

Approved:

CHARLES A. STROM, JR.

Acting Chief

Communications Division

FOR THE COMMANDER

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Chief, Advanced Studies Group

ABSTRACT

This document presents the formulation, computational logic and coding information developed for the purpose of effecting the definition of geocentric satellite orbits. The rationale for this process is constructed around the recursive minimum variance data filter developed by R.E. Kalman and a specially prepared magnetic tape generated in the preprocessor (SID 65 1203-2).

The trajectory portion of the program is formulated in the Encke manner and includes perturbing accelerations resulting from the first 3 harmonics of the Earth's potential function, atmospheric drag, solar radiation pressure, and solar and lunar gravitation. These accelerations are integrated via an uncorrected Gauss-Jackson routine started with a fourth order Runge-Kutta process.

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LIST OF SUBROUTINES AND THEIR FUNCTIONS

SECTION	ROUTINE	DEFINITION
2.1	MAIN	This routine mechanizes the subroutines and lower order driven routines designed to generate the trajectory of a satellite vehicle by a differential corrections process.
2.2.1	INPUT	INPUT provides all of the data (except the observation data) necessary to define the trajectory.
2.2.1.1	reld	REED is designed as a simple special purpose read package to provide the capability for inputting modified station data and estimated satellite data.
2.2.1.1.1	SICRD	A special purpose routine designed to assure that the first data card is the station identification card.
2.2.1.2	inital	INITAL sets up the solution process by defining all of the required vectors in the computational coordinate frame of 1950.0 from the information given in the true equation of data frame.
2.2.1.3	Posvel	This routine is designed to provide the user the option of reading either the satellites position and velocity vectors at the initial epoch or the equivalent set of orbital elements.
2.2.1.4	BLOCK	Data for the lunar and solar ephemerides and for the 1962 U. S. Standard atmosphere are stored in this routine. These data are loaded directly into memory at the time the program is loaded (BLOCK is not called).
2.2.1.5	DADUMP	A special purpose routine designed to DUMP the entire blank COMMON array when called.
2.3.1	traj	TRAJ mechanizes the working portion of the program and serves as the means whereby the reference trajectory is computed and the tracking stations of the problem checked.

SECTION	ROUTINE	DEFINITION
2.3.1.1	CONIC	conic generates the position and velocity on an arbitrary conic section defined by \vec{r} , \vec{v} , as a function of time. It is utilized for the purpose of defining the Encke reference trajectory and the luni-solar ephemerides.
2.3.1.1.1	SEARCH	This routine is designed to function in conjunction with CONIC for the purpose of iteratively solving Kepler's equation.
2.3.1.1.2	TIME	This routine defines time on the conic section as a function of a position anomaly.
2.3.1.1.3	PARTL	PARTL is the partial derivative of the time variable with respect to the anomaly variable. This information is utilized in a Newton iteration by SEARCH.
2.3.1.2	MOTION	MOTION is the driver routine for evaluating the total acceleration experienced by a vehicle moving in space relative to the Encke reference trajectory in the computational coordinate frame (1950.0).
2.3.1.2.1	OBLN	OBIN computes the acceleration resulting from the first three zonal harmonics of the Earth's potential function.
2.3.1.2.2	DRAG	This routine defines the acceleration produced by the tenuous atmosphere on a spherical satellite.
2.3.1.2.2.1	ATMS	ATMS operates in conjunction with DRAG and is designed to compute the instantaneous estimate of the atmospheric density.
2.3.1.2.3	ENCKE	Since the largest contribution to the acceleration is included in the reference trajectory and since off nominal motion produces a modification to the gravity vector, ENCKE is required to define the change in the acceleration resulting from the change in the central force.

SECTION	ROUTINE	DEFINITION
2.3.1.2.4	PRESS	PRESS computes the acceleration resulting from solar pressure on an equivalent spherical satellite.
2.3.1.2.4.1	SPOWER	This function operates in conjunction with PRESS. Its purpose is to define the ratio of the solar power to the speed of light.
2.3.1.2.5	PERT	PERT defines the gravitional acceleration experienced by the vehicle due to the sun and moon.
2.3.1.2.5.1	FQ	PERT is formulated in a manner similar to ENCKE and thus it employs a series to evaluate the off nominal nature of the acceleration. FQ is that series.
2.3.1.2.6	ЕРНЕМ	The position vectors for the sun and moon relative to the earth which are required by both PRESS and PERT are computed by EPHEM from data stored in BLOCK.
2.3.1.3	INGRAT	INGRAT is a driver routine for producing the first and second integrals of the output from MOTION.
2.3.1.3.1	HSIZE	This routine determines the optimum stepsize for a Gauss-Jackson intregration of the equations of motion.
2.3.1.3.2	START	START is a fourth order Runge-Kutta integration routine utilized to establish the data necessary to produce the difference table utilized in the Gauss-Jackson process.
2.3.1.3.3	DIFTAB	This routine differences the acceleration vectors established by START and evaluates the first and second sums on the leading diagonal of the difference table.
2.3.1.3.4	INTEG	INTEG mechanizes the Gauss-Jackson integration formulas for a stepwise integration of the equations of motion. INTEG also steps the leading diagonal in the difference table.

SECTION	ROUTINE	DEFINITION
2.3.1.4	TRAK	TRAK is the driver program which checks the tracking stations of the problem and determines if any can observe the satellite at that time. TRAK transfers to FILTER if observation data are available at this time.
2.3.1.4.1	UNIT	UNIT computes the position vector for the tracking station and establishes the up, east, north unit vectors at the station.
2.3.1.4.2	EQINOX	This routine defines the coordinate transformation relating the observational coordinate frame (true equator of date) and the computational frame (1950.0). This transformation is the result of nutation and precession.
2.3.1.4.3	GHA	GHA defines the Greenwich Hour Angle as a function of universal time and the number of days since 1950.0.
2.4.1	FILTER	FILTER is the driver routine for a Kalman estimate of the correction to position and velocity (state vector) resulting from processing the observed data.
2.4.1.1	KALMAN	This routine computes the minimum variance estimate of the state vector and the covariance matrix for the estimation errors.
2.4.1.2	STMAT	The errors at two points on the perturbed trajectory are related by employing an averaging process and two estimates of the transition matrix obtained using conic representation (TRANS).
2.4.1.2.1	'trans	TRANS provides STMAT the conic approximations of the transition matrices.

SECTION	ROUTINE	DEFINITION
2.4.1.2.2	INVAO	This routine works in conjunction with STMAT in the averaging process. It is designed to determine the analytic inverse of the output of TRANS.
2.4.1.3	MEASUR	MEASUR computes the matrix of partial derivatives of the observation vector with respect to the state vector.
2.4.1.4	ERROR	This routine computes the weighting matrix for the Kalman estimate. Data for Station errors and noise in the observations are employed.
2.4.1.5	UPSTAT	UPSTAT is designed to determine whether the state vector as computed by KALMAN is known to a degree which is satisfactory to allow the position and velocity to be corrected.
2.4.1.5.1	ELEMEN	Since the orbital elements of the osculating conic are of interest in the data reduction problem, ELEMEN is included to provide this information at those times when data is processed.
2.4.1.6	DATAPE	DATAPE defines the time of the next observation, the recording station, the type of data and the data itself. This information is recorded on magnetic tape by the preprocessor.
2.5	Mathematical	Subroutines
2.5.1	MATMPY	Matrix multiplication of two conformable matrices in double precision.
2.5.2	MTINV	Matrix inverse of a square matrix in double precision.

SECTION	ROUTINE	DEFINITION
2.5.2.1	CHOOSE	This routine functions in conjunction with MTINV to determine if the matrix is singular.
2.5.3	ADDMAT	Matrix addition
2.5.4	SUBMAT	Matrix subtraction
2.5.5	TRANSP	Matrix transposition
2.5.6	CROSS	Vector cross product
2.5.7	DOT	Vector scalar product
2.5.8	AMAG	Vector magnitude
2.6.1	SINH	Hyperbolic sine
2.6.2	COSH	Hyperbolic cosine
2.6.3	ARKTNS	Computes the single precision arc tangent and assigns the angle to the proper quadrant
2.6.4	DERAQ	The Kronecker delta

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1. INTRODUCTION

1.1 PURPOSE

FS4-305 is a FORTRAN IV IBM 7094 program which was written and checked using the standard North American Aviation monitor system (NAASYS - version 13). However, the program can also be operated on CDC equipment and other systems possessing FORTRAN capabilities. Consequently, to minimize possible system incompatibilities, care has been exercised to assure that only the basic features of the system are utilized. This approach assures that the program will be operable on new generation machines (e.g., the IBM system 360).

The primary function of this program is to construct an accurate trajectory of a geocentric satellite based on a series of observations (e.g., range, range-rate, azimuth and elevation, etc.). This task is performed through a differential corrections process by generating a reference trajectory and minimizing the observed minus computed residuals in a minimum variance sense. (The operation of the filter is explained in general in section 1.2 and in detail in section 2.4.)

The trajectory required in the corrections process is generated by numerical integration of the accelerations relative to a reference conic (Encke's method). Accelerations resulting from the off-nominal nature of the motion, the Earth's oblateness (first 3 zonal harmonics), solar-lunar gravitation, atmospheric drag, and solar radiation pressure are all included. Tracking station data and the corresponding relative position data are generated simultaneously as a function of universal time for the purpose of defining the predicted values of the observations from each station.

The observation data utilized in this program are provided on a magnetic tape by the preliminary processor (see FS4-305A, SID 65-1203-2). These data have been operated on in two distinct fashions. First, the raw data from each tracking station were smoothed by filtering the observations over a restricted interval of time (approximately 20 seconds) to a parabolic curve and the midpoint of this interval was selected for processing in the differential corrections program. This operation assures that the effect of random scatter in the data can be reduced and assures reasonably efficient operation of the differential corrections process by reducing the amount of raw data to be considered. Secondly, the data from the various sites were identified as to the station which recorded them and the type of information gathered; then the complete array was arranged in a chronological fashion to facilitate filtering of the data in a recursive mode.

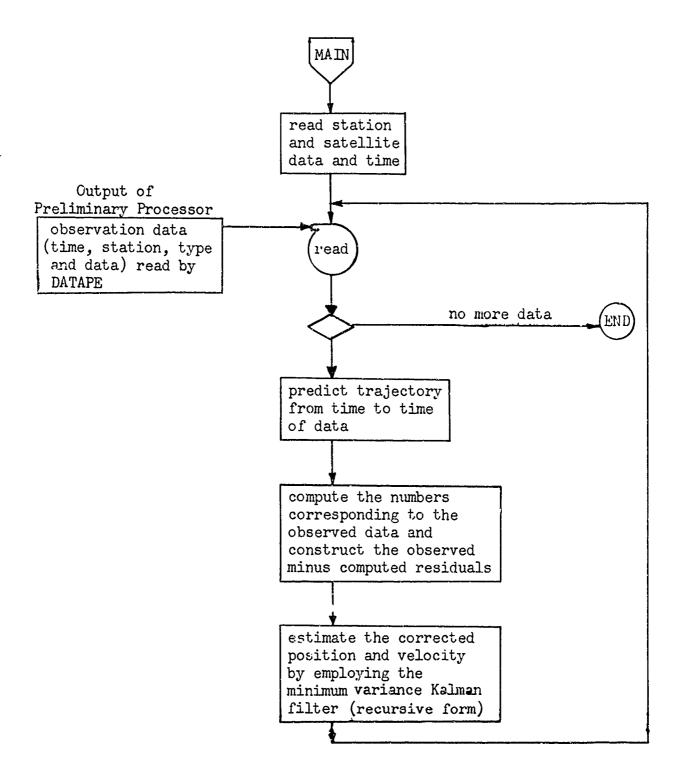
The interface of the preliminary processor and this program is provided by subroutine DATAPE (data tape). This routine reads the tape and identifies the data for use in differential corrections solution. Thus, complete consistency is assured.

1.2 Program Concept

The differential corrections orbit computation program is designed around the Kalman data filter developed and discussed in Subroutine KALMAN. Operation requires that input data be read to identify the stations which recorded the observed data, and estimates of the position and velocity (or orbital elements) of the vehicle at an arbitrary epoch. At this time, the first data point (time, type of data, recording station, and the observation vector) is read into memory and the trajectory from the initial epoch to the time of the observation is defined. When this is done, the position and velocity relative to the observing station are computed and an error signal is generated based on this data and the actual information recorded.

The filtering of this information or prediction of a corrected position and velocity is accomplished recursively (i.e., one set of observations at a time) by employing a minimum variance formulation (see KALMAN). This filter has been shown to approximate the true non-linear process very well. Further, the filter provides for weighting the data in a general manner not obtained with a simple least squares solution. Its inclusion is thus felt to constitute near optimum design of the differential corrections orbit computation program.

After predicting the best estimate of the position and velocity at the first data point, a second data point is read and the process is repeated. This operation is demonstrated in the following sketch.



An appreciation of the general nature of this program is now available. The immediate problem is, thus, to add detail to the flow diagram and establish a rationale which will assure efficient and accurate operation. This detail can best be included by dividing the program into logical blocks (driver subroutines) which accomplish the desired functions, and by discussing each block in terms of the intended purpose and formulation. Indeed, this division has been performed and is outlined fully in the discussion of the three principal drivers of the program, MAIN, TRAJ and FILTER. Therefore, attention will turn to the first, MAIN.

2.0 PROGRAM DISCUSSION

The formulation, rationale and computational logic for the routines designed to perform the differential correction of geocentric satellite trajectories is presented in the sections which follow. These discussions attempt to document each routine in a complete manner so that subsequent modification to any function presently being performed can be facilitated.

Careful review of these separate discussions is essential to establish the complete computational logic for the program and a working knowledge of its structure. However, if interest is centered in the area of program utilization, attention should be directed primarily into the structure of the sample problem and the associated input formats. (In the latter case, no detailed information of the program logic is essential.)

The mechanism for communicating between the routines of the program is the COMMON region DATA. A map of this region and the definition of the variables assigned is presented in Appendix 1. This information should be reviewed in conjunction with <u>any</u> attempt to revise the program logic.

2.1 MAIN Program

Purpose: To mechanize the subroutines and lower order

driver routines designed to effect the differential correction of a satellite's position and velocity vectors based on data recorded on a magnetic tape by the preliminary processor

routine, PROCES.

Deck Name: MAIN

Calling Sequence: None

Input/Output: None

Subroutines Required: INPUT (loads satellite and station data)

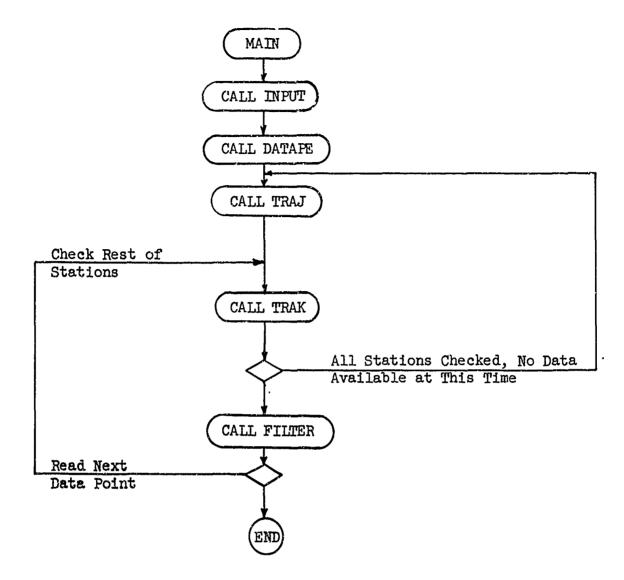
DATAPE (loads observation data)
TRAJ (generates trajectory)

Functions Required: None

Approximate Deck Length: 63 (octal)

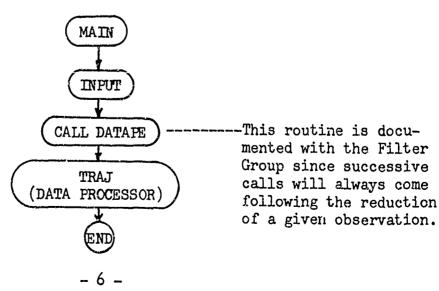
Description and Program Logic:

MAIN is the driver routine which mechanizes the complete program for the purpose of processing observed data for a single (i.e., one at a time) identifiable satellite and differentially correcting the estimate of the position and velocity vectors describing its motion. In order to accomplish this task efficiently and facilitate the development and checkout process, the program has been constructed in a series of major blocks (modules), each of which is itself subdivided into a number of subroutines. These modules serve to provide the input data for the program, to read into memory the first observed data point from the data tape, to generate an accurate trajectory which can be utilized in the computation of the observed minus computed residuals, to check the various tracking stations employed in the problem for the relative position and velocity information, and to process the observed data (recorded on a magnetic tape provided by PROCES) and differentially correct the elements of the trajectory. In its simplest form, then, the program can be viewed as the link between these modules, i.e.,



1

However, due to the fact that data required as input to TRAK and FILTER are available in TRAJ and TRAK respectively and are not utilized in the MAIN Program for any other purpose, this logic has been modified slightly. The modification consists of placing the call statement for TRAK (and FILTER) in TRAJ (and TRAK) and constructing a transfer within TRAJ which will assure that control is retained by TRAJ until all data have been processed. In this sense, then, TRAJ is the gross data processor and the flow diagram reduces to:



A careful review of these modules is essential to a thorough appreciation of the functioning of the program. For this reason, complete documentation of all routines employed will be presented in the following sections of this document. The task of reviewing this information, however, has been simplified by grouping the subroutines when their function relates them to a larger problem to assist in the comprehension.

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5 MAIN - EFN	TRAJ	NIRGI RETURNS TO A	THE PROCEDURE	WRITE(6.10)	CONTROL RE	DUMP	:	
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PAGE

SID 65-1203-1 - 9 -

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-10-	FS305 MAIN				STGRAGE MAP Main prøgram	MAP 18GRAM	11/23/85	Ŋ	PAGE	E 71.
				CGMMGN		VAR I ABI. ES				
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2.2 The INPUT Group

This group of routines is designed for the purpose of providing the communications link between the users of the differential corrections program and the program itself. The group contains a routine which provides nominal information to the program (INPUT), a routine which reads specific information regarding the satellite (REED), a routine which loads ephemeris and atmosphere information (BLOCK), a routine which effects conversion from orbital elements to position and velocity if this form of the data is provided (POSVEL), and a routine to set up the solution process by initializing various data cells in memory (INITAL).

The group also includes in a sense the routine (DATAPE) which reads the data tape prepared by the preliminary processor. However, since this routine is a more integral part of the logic associated with the filtering of the data, it is documented in the FILTER group.

2.2.1 Subroutine INPUT

Purpose:

INPUT provides all of the data(except the observation data) necessary to effect the differential corrections solution of a given trajectory. Data for the physical characteristics of the Earth, Sun, Moon, and vehicle, station location and error data, position and velocity information for the satellite, and an estimate of the covariance matrix for errors in the state vector at the

initial epoch are provided.

Deck Name:

INPUT

Calling Sequence: CALL INPUT

Input/Output:

111000	FORTRAN	Math		Common/	
1/0	Name	Name	Dimension	Argument	Definition
0	CON	-	15	DATA (1)	A subarray of common containing constants for the program
0	RE RPOL, COEFJ COEFH COEFD GMER'TH OMEGA	Re RP J H D	1 1 1 1 1	CON (1) CON (2) CON (3) CON (4) CON (5) CON (6) CON (7)	Equatorial and Polar radii (Km) for the reference ellipsoid, the first 3 coefficients of the potential function (Jefferies notation), the gravitational constant (Km3/sec2), and the spin rate for the Earth.
О	GMMOON GMSUN	Mm Ms.	1	CON (8)	Gravitational constants for the moon and sun (Km3/sec2)
0	AU	AU	1	con (10)	The astronomical Unit (Km)
0	CONDAY	SEC DAY	1	CON (11)	Conversion from days to seconds (86400.)
	CONA 5	RAD DEG	1	CON (12)	Conversion from degrees to radians
0	NIN NOUT	-	1	CON (13) CON (14)	Input and output tape numbers

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
Ι	SAT	-	20	DATA (16)	A subarray of common containing data pertaining to the satellite at the initial epoch.
I/O	SMASS AREA CD REFLEC	m A C _D R	1 1 1	SAT (1) SAT (2) SAT (3) SAT (4)	Satellite mass (K_g) , reference area $\binom{m^2}{n}$, drag coefficient, and surface reflectivity.
1/0	RVEC	r̄ (or a,e,i) v̄ (or Ω,ω,e,)	3	SAT (5) SAT (8)	Position and velocity vectors (or orbital elements) in the true equator of date frame at the initial epoch (Km-sec Units).
I/O	TW (DJ) TF (DJF)	t _o	1	SAT (11) SAT (12)	The whole and fractional part of the day corresponding to \vec{r} , \vec{v} relative to January 0 1950. (1950.0) J.D. 2433282.423.
1/0	WINDEX CHECK GO NO CODUMP	-	1 1 1	SAT (13) SAT (14) SAT (15) . SAT (16)	Indices utilized to define the format of RVEC and VVEC (cartesia vectors if 1. or orbital elements if 2.), whether or not each station is to be checked at each integration step (yes if 1. or no if 2.), whether or not trajectory data is to be prepared for each Nth integration step (yes if N. or no if 0.), and whether COMMON is printed (no if zero).
0	KCHECK NOGO	-	1 1	SAT (17) SAT (18)	Fixed point equivalents of SAT (14) and SAT (15).
ī	SDA		250	DATA (36)	A subarray of common containing station data.
I	N (I)	n _i	10		Station identification indices - used to select those stations to be employed.

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
0	STATN	I A H Name	40	SDA (1)	Station array (1 to 10) containing position information for each of the stations and a 6 character identification.
0	HORCOR	E	10	SDA (41)	Horizon corrections in elevation for each of the 10 stations.
. 0	STERR	2	30	SDA (51)	Station error array (1 to 10 stations) containing variance information for latitude, longitude and altitude (_, _, Km ²)
0	SNOISE	2	40	SDA (141)	Station noise array, (1 to 10 stations) containing variance information for measurement for errors in range, range in rate, azimuth and elevation, (Km ² , Km ² /sec ² , _, _,)
0	Number	-	1	SDA (241)	The total number of stations employed in the tracking program for this given simulation
I	STT		105	DATA (286)	A subarray of common containing statistical information (and related data) for the satellite
I/O	PP	P	6 X 6	STT (70)	Covariance matrix for the errors in \hat{r} and \hat{v} at t_0 (metric units) resulting from smoothing raw data as done in the preliminary processor.

Subroutines Required: RFFD (Relative Read rackage)

POSVFI (Converts elements to ro, vo)
IMITAI (initializes vectors for problem)

Functions Required: None

Approximate Deck

I ength:

1452 (octa7)

Description:

INPUT provides all of the constants, the data for a fixed network of ten tracking stations, and the logic for selecting (and modifying) from the fixed array of stations those to be employed on the analysis. In addition, INPUT serves as the driver for a read routine (REED) which is constructed in such a manner that any of the constants previously loaded into common can be changed at the time the physical data and estimated orbital data for the satellite being tracked are loaded. Upon return from REED a test is made to determine whether the 6 components of position and velocity or 6 constants of integration in the form of the orbital elements (a, e, i, α , ω , θ ₀) were provided. (In the latter case the corresponding radius and velocity vectors are computed). INPUT then calls subroutine INITAL which initializes the cells in the common array containing vectors used in the integration of the "best" trajectory and in the processing of the data. As a final step, all of the input data are printed for reference.

The first observation which should be made of INPUT is that variance data are given for the station errors (i.e., variance in latitude, longitude, and altitude) and for the noise errors (i.e., variance in range, range-rate, azimuth, and elevation) under the assumption that the errors are uncorrelated. If calibration of the stations employed in this simulation should subsequently prove that the present formulation is inadequate or could be improved, the complete arrays should be provided. The incorporation of these additional data requires only that the dimension of the SN, SF, SNOISE, and STERR arrays be altered and that the FIITER package be modified accordingly to accept the new data. Allowances for this modification have been made in the design of the common array in that extra locations have been provided.

A map of the COMMON array (DATA) utilized by this routine is presented as Appendix 1 to this report. This map should be utilized to facilitate communication with the program and to aid in analysis of the communication between routines.

The second observation which should be made is that, since the data being processed have been smoothed previously to reduce the number of raw data points and to remove the random scatter in the raw data, the variances utilized in the program should correspond to the smoothed data points rather than the raw data. Thus, to prepare these data if raw data variances are known, it is necessary to develop the covariance matrix for the difference in the true and smoothed values of the observation vector.

and note that the smoothed values obey the equation

$$Y_{\text{SMOOTH}} = \begin{bmatrix} 1 & X_1 & X_1^2 \\ 1 & X_2 & X_2^2 \\ & \vdots & \end{bmatrix} = \begin{bmatrix} a \\ b \\ c \end{bmatrix}$$

$$\stackrel{\text{a}}{=} M \stackrel{\text{c}}{=}$$

where: X₁ = t₁ - t_{midpoint}

a,b,c = coefficients of the parabola which best fits the data.

Further, the vector of constants (c) which is determined in an unweighted least squares fit of the parabola to the data can be represented as

$$\dot{z} = \not p \, \vec{V}_{\text{observed}}$$

(see the preliminary processor documentation of SMOOTH). Now, if the observed vector is represented as

$$\vec{V}_{\text{observed}} = \vec{V}_{\text{true}} + \vec{N},$$

substitution back into the equation for $4 \vec{\mathcal{G}}$ yields

$$\Delta \vec{\hat{V}} = (I - M\phi) \hat{\mathbf{Y}}_{TRUE} - M\phi \hat{\mathbf{N}}$$

$$\equiv A \vec{\hat{V}}_{TRUE} - K\hat{\mathbf{N}} .$$

Thus, the desired covariance matrix can be found by taking the expected value of the product $\Delta \vec{\nabla} \ \Delta \vec{\nabla}^{7}$.

$$E (\Delta \vec{\nabla} \Delta \vec{\nabla}^{T}) = E \left\{ A \vec{\nabla}_{T} \vec{\nabla}_{T}^{T} A^{T} - A \vec{\nabla}_{T} \vec{n}^{T} K^{T} - K \vec{n} \vec{\nabla}_{T}^{T} A^{T} + K \vec{n} \vec{n}^{T} K \right\}$$

AL

But:
$$E(\overrightarrow{\mathcal{V}}_{T} \overrightarrow{\mathcal{V}}_{T}^{T}) \equiv 0$$

$$E(\overrightarrow{\mathcal{V}}_{T} \overrightarrow{N}^{T}) \equiv 0$$

$$E(\overrightarrow{N} \overrightarrow{\mathcal{V}}_{T}^{T}) \equiv 0$$

$$E(\overrightarrow{N} \overrightarrow{N}^{T}) \equiv V$$

Leaving

$$E (\Delta \overline{Y} \Delta \overline{Y}^T) = K V K^T$$

which is generally not diagonal even for a diagonal V, but which (for the types of problems attempted during checkout) can be approximated with a diagonal matrix.

The operation of INFUT is controlled by data provided from REED and on the station identification card (SIC) which must precede all of the card input. This is accomplished as follows: the SIC (a card of 10 fixed point numbers of FORMAT 10 I 4) is read and those stations for which an index other than zero is recorded are assumed to be utilized in the data reduction problem (The numerical sequence of the utilized stations must be provided as input to the preliminary processor so that the observed data will be credited to the proper station). Now, INFUT selects data from arrays of numbers provided for these stations and loads these data into common for use in subsequent operations (it is thus important to note that the remaining station data are discarded and will not be available to the program at later time) subject to modification from REED if any or all of the data from one or more stations is to be changed.

Having selected the nominal station data, INPUT calls REED for the purpose of obtaining the required satellite data and varifying the nominal station arrays. REED provides data to the program by assigning any data (previous to the first blank 12 digit field) to the common location provided in the first 12 digit field (right justified) of the card. When REED recognizes the fixed point number 999 in the first field of a card it assumes all numerical data have been provided and begins to look for new station names (one to a card) until the location 9999 is read. At this point, all data are assumed to be available and control is returned to INPUT. It is important to note that with the exception of the grouping of the data cards before 999 and the name cards before 9999, no sequencing of the data cards for subroutine REED is required.

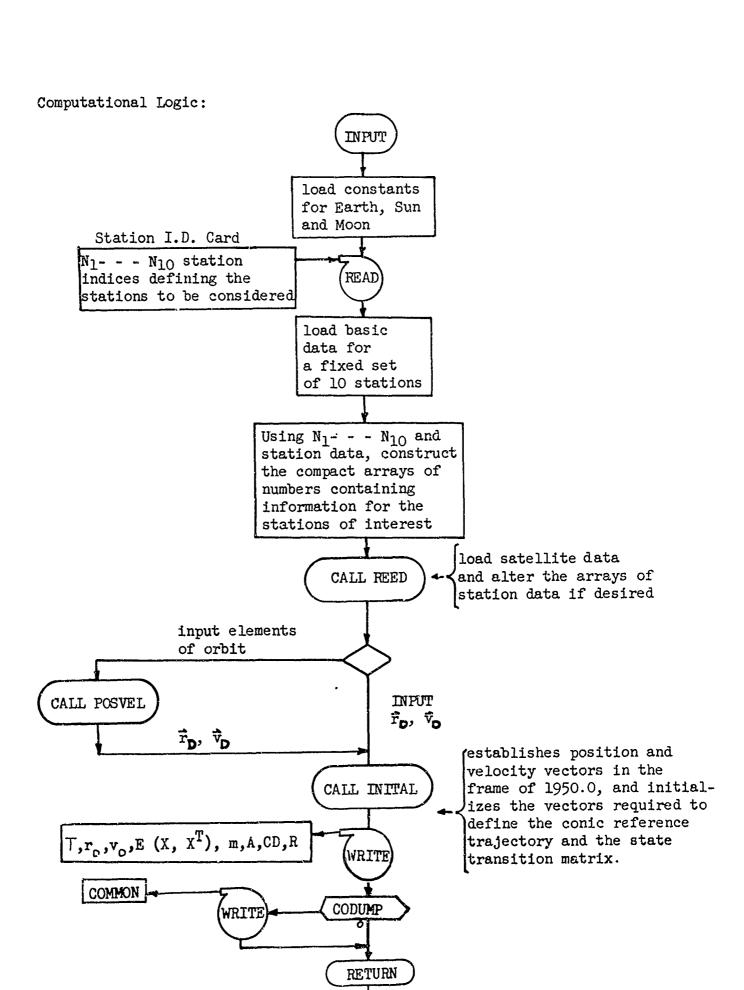
The data expected by INPUT from REED is as follows:

Data (16) = satellite mass (kg) Data (17) = cross section area (m²) Data (18) = drag coefficient Data (19) = surface reflectivity Data (20) = radius vector (X, Y, Z) (Km) or the orbital elements a, e, i in the true equator of date frame (Km, - , DEG) = velocity vector (X, Y, Z) (Km/sec) or the orbital Data (23) elements ω , Ω , Θ (true anomaly) (DEG, DEG, DEG) = whole number of days since 1950.0 to beginning of present Data (26) date fractional part of present day in U.T. expressed in days Data (27)

- Data (28) = WINDEX an index utilized to define the option for Data (104) (109). WINDEX = 1. if these data are position and velocity vectors; and 2. if they are orbital elements
- Data (29) = CHECK an index employed in TRAK to bypass checking the tracking stations unless tracking data are available at the given instant. CHECK = 1. no bypass; = 2. for efficiency
- Data (30) = GONO an index employed in TRAK to bypass checking the tracking stations unless the particular station involved recorded the data. GONO = 1. no bypass; = 2., bypass
- Data (31) = CODUMP an index used to assist checkout and as a permanent record of program constants, etc. If CODUMP = nonzero, the entire DATA array is printed following initialization.
- Data (356) = covariance matrix for the errors in the initial position and velocity vectors in the coordinate system of \vec{r} , and \vec{v} , and in units of Km^2 and $(KM/sec)^2$

These data <u>can</u> <u>be</u> <u>augmented</u> with station data if desired. This step is accomplished by identifying the number of the station to be changed (the number of stations on the SIC preceding the station to be changed) and loading data into the following locations.

```
Data (36 + 4N)
                 = Latitude in radians
Data (37 + 4N)
                    Longitude in radians
Data (38 + 4N)
                 = Altitude relative to the reference ellipsoid (KM)
Data (39 + 4N)
                 = Station name (6 characters)
Data (77 + N)
                 = Horizon correction (rad)
Data (87 + 3N)
                 = Variance in latitude (rad)^2
Data (88 + 3N)
                 = Variance in longitude (rad)2
Data (89 + 3N)
                 = Variance in altitude (KM)^2
Data (177 + 4N)
                 = Variance in range (KM)^2
Data (178 + 4N)
                 = Variance in range-rate (KM/sec)2
Data (179 + 4N)
                = Variance in azimuth (rad)^2
Data (180 + 4N)
                = Variance in elevation (rad)^2
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- EFN SCURCE STATEMENT - IFN(S) -
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PUT0050
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                                 INFORMATION * IT SHOULD BE REVIEWED CAREFULLY TO ASSURE CCMPATIBILITY WITH DESIRED TRAJECTORY AND STATIONS
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                                                                                                                                               INTO THE PROGRAM IN MKS UNITS . INCLUDED
IN THIS COLLECTION ARE CCNVERSION DATA , CONSTANTS FOR
THE EARTH, MOUN, SUN, INPUT AND OUTPUT TAPE NUMBERS.
                                                                                                                                   THE FOLLOWING SECTION OF THIS ROUTINE LOADS PHYSICAL CONSTANTS
                                                                                                                                                                                                                                                                                                                                      SN(10,4)
                      ROUTINE CONTAINS ALL OF THE REQUIRED INPUT DATA AND READ
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                                                                                                                                                                                                                                                                                                                          STATN(40)
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SUBROUTINE INPUT
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IPUT0750 TPUT0760 PUT0770 PUT0780

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¥ GROUP OF THESE 10 STATIONS CAN BE CONSIDERED SEPARATELY. THE ROUTINE ALSO PROVIDES FOR THE REPLACEMENT OF ANY OF THE FOLLOWING SECTION OF ** INPUT ** IS DESIGNED TO PROVIDE THE REQUIRED TRACKING SYSTEM DATA . THE ROUTINE HAS DATA FOR 10 STATIONS BUILT INTO THE ROUTINE THOUGH ANY

THE 10 STATIONS THROUGH THE MEDIUM OF THE READ STATEMENT AND THE SELECTIVE REPLACEMENT OF PORTIONS OF THE DATA

PUT0830

PUT0840 PUT0850 PUT0860 PUT0870

PUT0800 (PUT0810 PUT0820

THE SAME MANNER .

A SERIES OF FIXED POINT NUMBERS WHICH MUST BE READ INTO THE PROGRAM. THESE NUMBERS (N(I), I=1,10) FORCE THE PROGRAM TO INCLUDE A STATION IF N(I) IS NOT EQUAL TO THE ROUTINE IS SETUP TO UTILIZE THE STATION DATA DEPENDING ON

PUT0880

PUT0890 PUT0900 PUT 09 10 PUT0920

PUT0930

PUT0940

PUT0950 PUT0960 PUT0970 PUT0980 PUT0990 PUT1000

ZERO(E.G. , N(I) = THE NUMBER OF THE STATION)

CHANGED WILL BE ALTERED AS FOLLOWS . THE LOCATION IN THE UPCN COMPLETION OF THE STATION SF. ECTION TASK SUBROUTINE READ IS CALLED FOR THE PURPOSE OF COMPLETING THE REQUIRED INPUT DATA TABLE. DURING THIS OPERATION THOSE STATIONS TO BE

FIELD ON THE CARD , THEN THE NEW NUMBER IS PLACED IN THE DATA ARRAY IS LOCATED AND PLACED IN THE FIRST 12 DIGIT

SECOND FIELD . SUCCEDING NUMBERS CAN BE CHANGED ON THE SAME CARD. BUT, IF THE LOCATION SEQUENCE IS BROKEN A STATN ARRAY IS MODIFIED, ALLOWANCE MUST BE MADE FOR THE NEW CARD MUST BE STARTED. SIMILARLY, IF THF

NUMBER BUT IS RATHER A NAME (THUS, THESE NAME DATA MUST BE READ INTO MEMORY IN A SEPARATE MODE --AFTER ALL NUMERICAL DATA HAVE BEEN COMPLETED) . THIS ALLOWANCE WAS MADE BY TESTING THE LOCATION AND TRANSFERING FROM FACT THAT THE FOURTH ELEMENT IN THE ARRAY IS NOT A

PUT1010

PUT 1020 PUT1030 PUT1040

PUT1050

PUT1070 PUT1060 PUT1080 PUT 1090 CARDIUNTIL 9999 IS READ. AT THIS POINT INPUT IS STOPPED. REED THEN READS NAMES (ONE LOCATION AND ONE NAME TO THE THE DATA MODE TO THE NAME MODE WHEN 999 IS ENCOUNTERED. IMPORTANT TO NOTE THAT THE NUMBER OF STATIONS IS NOT READ IT IS

NUMBER OF NONZERO N(I) TO ASSURE PROPER PROGRAM FUNCTION. IPUT1110 THUS IT IS NECESSARY TO HAVE THE PROPER

SID 65-1203-1

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PAGE 13
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IPUT1130
                                                                                                                                                                    PUT1290
                                                                                                                                                                                                                                  PUT1350
                                                                                                                                                                                                                                             PUT1360
                                                                                                                                                                                                                                                                                       PUT1400
                                                                                                                                                                                                                                                                                                 PUT1410
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                                                                                                         CHECK**INDEX USED TO BYPASS CHECKING THE
                                                                                                                                                                                                   GONO** INDEX USED TO BYPASS CHECKING THE TRACKING STATIONS WHEN DATA IS AVAILABLE
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PUT 3720 PUT3730 PUT3750 PUT3760 PUT3740 IF(WINDEX-1,) 210,21C,220 KCFECK = CHECK NOGO = GONO = RVEC(1)= RVEC(2) VVEC(1) 11 33. = I) 0,4≡ Þ

> SID 65-1203-1 - 29 -29

PAGE 20

	;	,	43		4 4							67			• . †					4		
IPUT – EFN SOURCE STATEMENT – IFN(S) –	VVEC(3)	CALL POSVEL(A,E,O[,W,CM,TH)	210 CALL INITAL IPUT3820	WRITE(6,300)0J,0JF,(RVEC(I),I=1,3),(VVEC(I),I=1,3),((PP(I,J),JFUT3830	1=1,6),1=1,6) ,SMASS,AREA,CD,REFLEK	300 FORMAT(14H1 INPUT DATA //15H DATE(1950) = 2E17.8/15H RADIUS VEIPUT3850	/ 15H VFLOCITY VEC= 3E17.8 ///27H INITIAL COVARIANCE	6E17.8/6	LITE DATA /15H MASS == E17.8/15H AREA =	4E17.8 /15H CO ==E17.8/!5H REFLECTIVITY=E17.8 ////) IPUT3890	MP = 4 * NUMBER I PUT 3900	WRITE(6,301) (STATN(K), K=4, MP, 4) IPUT3910	WILL BE CONSIDERED // 5(10X, A	16) / 5(10x, A6 1) IPUT3930	2)	302 FORMAT(1H1) IPUT3932	IF(CODUMP.NE.O.) CALL DADUMP	1 PUT3940	, ******* IPUT3950	I PUT 3960	RETURN I PUT3970	END I PUT 3980

SID 65-1203-1

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		10900	► ≻αααααα αααααα π	TYPE R	T R R R R R
		LENGTH	LOCATION 00000 00435 00001 000012 00012 00012 00026 00028 00033 00043	LOCATION 00730	LGCATION 01014 01017 01022
		00001	SYMBOL CON STT RPOL COEFD GMMOON CONDAY NOUT CD VVEC WINDEX CODUMP STATN SNOISE	VARTABLES SYMBOL SE	VARIABLES SYMBO, V3 V6 V9
МАР	V AR I ABL ES		► > αααααπαααπαα m	PRGGRAM TYPE R I	PROGRAM TYPE R R R
STORAGE SUBROUTINE INPUT	COMMON VAF	0R1G1N	LUCATION 00000 000043 000003 000003 000011 00014 00020 00023 00035 00035 00040	DIMENSIONED LOCATION 00660 01000	UNDIMENSIONED LOCATION 01013 01016 01021
SUBR		1	SYMBOL DATA SDA SDA RE COFFH OMEGA AU NIN AREA RVEC DJF GOND NOGO STERR	SYMBOL SN N	SYMBOL V2 V5 V8
		4 BLOCK	F 	TYPE R R	н 9 9 9
IPUT		COMMON	LOCATION 00000 00017 00606 60002 00013 00013 00022 00021 00031	L DC ATICN C0610 00766	LOCATION 01012 01015 01020
* * * * *			SYMBOL DATA SAT WRK COEFJ GMERTH G4SUN CONV2 SMASS REFLEK D3 CHECK KCFECK HORCOR	SYMBOL P HC	SID 65-120 - 31 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4

203-1 31 -

26				10 113		LOCATION 01757 02042 01224
PAGE	- -			SECTION SECTION SECTION SECTION		LOCA 017 020 012
	61025 01030 01033 01036					1FN 26A 42A FORMAT
4/86				POSVEL DADUMP • FCNV• CC•3		
01/24/86	X O F		LED		DENCE	EFN 140 210 301
МАР		POINTS	NES CALLED	6 0 112 113 113	CORRESPONDENCE	LOCATION 01706 01774 01136
STORAGE		ENTRY PO	SUBROUTINES	SECTION SECTION SECTION SECTION SECTION		001000000000000000000000000000000000000
ST	01624 01027 01032 01035	Ш	าร	N N N N	EFN IFN	IFN 12A 34A FORMAT
				REED FWRD. FFIL. CC.2 SYSLOC	ѿ	11
						EFN 130 202 300
	∝ +	4		144		ATION 772 752 015 241 01372
		SECTION		CTICN CTION CTICN CTICN CTION		LOCATI 01772 01752 02015 01241
H	01023 01026 01031 01034 01037	SEC		S S E C		IFN 31A 23A 40A FORMAT
**** IPUT		INPUT		SICRD INITAL UNO6. CC.1 CC.4		1F 3 2 4 4 F0 F0 LENGTH
32	> 2 A 3 E P P					EFN 120 150 220 302 DECK

2.2.1.1 Subroutine REED

Purpose:

REED is designed as a simple reading routine for numeric 1 data and alphabetical characters. This routine is essential to the program if permanent data of the type listed in subroutine INPUT are to be retained or changed as desired

Deck Name:

READ

Calling Sequence: CALL REED

Input/Output:

	FORTRAN	Math		Common/	
I/0	Name	Name	Dimension	Argument	Definition
I	NIN	-	1	DATA (13)	The input tape number.
I	И		1	-	The location in the common array (DATA) at which the floating point number presented in the second field of the card is to be placed. This number is assigned a 12-digit field but should be rightly justified.
					When N = 999, the outines interprets this as a signal that no more data (numerical) are available and transfers to a second mode. In this mode, the routine reads one 6 character alphabetical rame per card into memor until N = 9999. At this time, return is triggered.
1/0	D(K)	DATA	5	DATA (N, N+1, N+2, N+3, N+4)	Up to 5 consecutive pieces of information (floating point numbers) which are to be stored in the common array. If any of the 5 numbers is blank, the balance of the card is not read.

Subroutines Required:

None

Functions Required:

None

Approximate Deck Length: 130 (decimal)

Description:

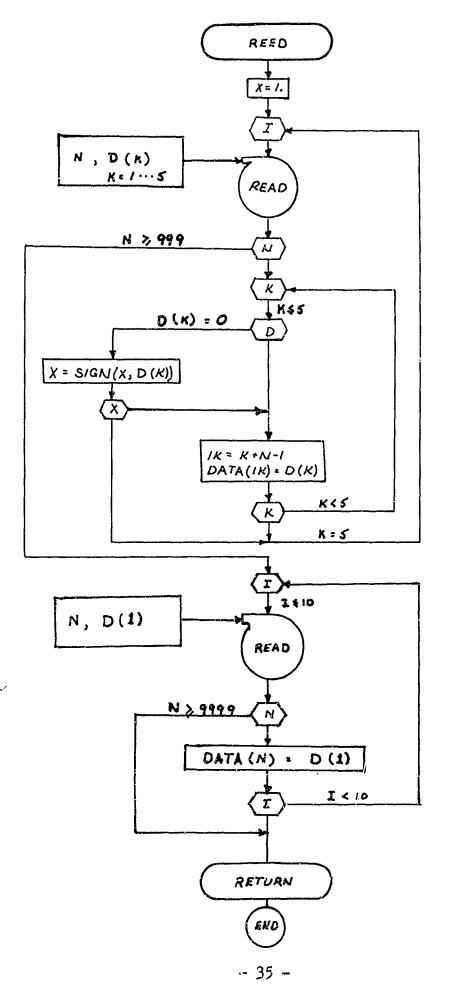
REED is a semi-general purpose read routine which is designed to accept cards in an Il2, 5E 12.8 Format and assign the data recorded in the second through sixth fields of the card to the consecutive locations in common (DATA), beginning with the location read in the first field. Several comments governing the operation of REED are in order, however, since they affect the functioning of REED and thus of the main program. The first is that REED will not search a data card past the first blank field which it recognizes. (Blanks are interpreted as -0.0; thus, zeros must be input using no sign or a plus, e.g., 0.0). If non-consecutive pieces of information are to be placed in the program as data or as new constants, it is necessary to start a new card following the point of discontinuity (or else fill in the data for the intervening location(s)).

The second observation is that all data are assumed to be floating point numbers for the sake of simplicity. Thus, if data are to be utilized as fixed point numbers, a fixing operation must be performed in the calling program after the data have been read. This operation is quite easily accomplished by equating a fixed point name to the floating point variable and equivalenting both variables to locations in the common array (DATA).

The third observation pertains to the method utilized to identify the time at which data are complete. A signal of quite arbitrary nature can be utilized; however, it was felt that the information should be recorded in the first field since this field alone is always read. Further, since the DATA array used for common generally requires fewer than 1000 locations, it was decided that when N > 999 no more numerical data would be read. A card hearing this number must thus follow all of the data.

When the program identifies a location N > 999, return to the calling routine is not triggered immediately. Rather, a test is made first to see if any alpha-numeric information is to be read. If N < 9999, additional cards are read in a format Il2, A6. If N>9999, transfer to the calling program is effected. Thus, this card must also be present in the deck whether there are alpha-numeric data or not.

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SID 65-1203-1

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READ0070
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                                               RFAD0020
                                                           READ0030
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                                                                                                 THIS ROUTINE READS A DATA ARRAY AND STORES IT IN COMMON
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PAGE
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                                                 F=AD0390
READ0400
PEAT0410
READ0420
READ0420
READ0440
                                                                                                              READO460
READO650
PFADO650
READO470
                              PEAU0370
RFAD0380
01/14/85
          IFN(S)
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READ( 5,402) N,D(1)

IF( N = 799) 403,500,500

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401 CONTINUE

402 FORMAT( 112,A6 )

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SID 65-1203-1 - 37 -

PAGE 34			00607	TYPE R R		TYPE		17PE 1 I				NS V
			LENGTH	LOCATIUN 0C000 00435		LOCATION		LOCATION 00617 00622				SECTION
01/14/86			01	SYMBOL CON STT	RIABLES	SYMBOL	21 481 50	ب			0;	• FRIN.
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		•	вгоск	T Y P E R R R .		TYPE R		TYPE R PE		4		ιν ω
READ			COMMON	LOCATICN 00000 00017 00606		LOCATION CO510		LOCATION 00615 00520		SECTION		SECTION SECTION
38				SYMBOL DATA SAT WRK		SYMBOL D		SYMBOL X K		8 E F.D		SID 65-1203-1

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PASE 35		LOCATION 30670	00706	00640	
		1 F N 1 1 A	19A	FURYAT	
01/14/86	ENCE	EFV 200	223	702	
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		100	210	401	
		LOCATION JG635	00723	00675	
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7¢		Z U H	400	730	403 DECK L

2.2.1.1.1 Subroutine SICRD

Purpose:

SICRD is a special purpose subroutine which operates in conjunction with the program logic to assure that the first data card is the station I. D. card. If not, execution is

terminated.

Deck Name:

SICR

Calling Sequence:

CALL SICRD (N)

Input/Output

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
0	n	-	1.0	Arg	array of numbers indicating which of the ten stations of the program are to be utilized (1 = yes, 0 = no)
I	nin Rout	64	1	CON (13) CON (14)	input and output tape numbers.

Subroutines Required Functions Required

None None

Approximate Deck Length

100 (Octal)

Discussion:

This routine is designed to read the first data card in an "A-FORMAT" and to test the first word on that card to determine if it is in fact the station I. D. card (SIC). If the card is identified as the SIC, the words in the next 10 fields of the card are tested for zeros. Finally, an array of numbers (N) is constructed of zeros and ones so that the main program will employ the proper network. It is important to note that since the data are read in an A Format any non-zero characters can be employed to identify the users desire to include a station.

If the first card is not the SIC, then execution is terminated with an error message.

特於公公

THIS SURRGUTINE REAUS THE FIRST DATA CARD AND INSURES THAT SIGNORS DIMENSITY 4(10), DW(IO), IDN(IO) (SIC CARJ). SIGNORS DIMENSITY 4(10), DW(IO), IDN(IO) (SIC, IDSIC, IDSIC, IZERO, IZERO), (DW, IDW) SIGNORS DATA SIC, ZERO / 44SIC, 44 O/ READ FIRST DATA CARD. SIGNORS SIGNORS DATA SIC, ZERO / 44SIC, A4H O/ READ FIRST DATA CARD. SIGNORS SIGNORS DATA SIC, ZERO / 44SIC, A4H O/ READ FIRST DATA CARD. SIC, CARD WAS SIGNORS DECAD AND TERMINATE ERROR SIGNORS DECAD ON THE CANDUL SIGNORS DECAD DECAD ON THE CANDUL SIGNORS DECAD DECA	THIS SUBROUTINE READS THE FIRS IT IS THE STATION INENTIFICATION OIMENSION W(10), DW(10), IDW(10) E PUIVALENCE (SIC, ISIC), (DSIC, IDS DATA SIC, ZEPO /4HSIC, 4H O/ READ(5,100) DSIC, (DM(I), I=1,10) IF(IDSIC, NE, ISIC) GD TO 40 IF(IDSIC, NE, ISIC) GD TO 40 IF(IDM(I) = 1 IF(IDM(I), FO, IZEAU) M(I) = 0 CONTINUE	DATA CARD AND INSURES THAT ARD (SIC CARD). C).(ZERO,IZEPD),(DN,IDN) EAD FIRST DATA CARD. EST FIRST FIELD. IF CARD WAS OT A SIC CARD, WRITE ERROR ESSAGE AND TERMINATE EXECUTION	S 1 C X D O O O O O O O O O O O O O O O O O O
IT IS THE STATION INENTIFICATION CARD (SIC CARD).	IT IS THE STATION INENTIFICATION DIMENSION W(10), DW(10), IDW(10) E DUIVALENCE (SIC, ISIC), (DSIC, IDS DATA SIC, ZFPO / CHSIC, 4H O/ READ(5, 100) DSIC, (DM(1), I = 1, 10) IF (IDSIC, NE, ISIC) GD TO 40 IF (IDSIC, NE, ISIC) GD TO 40 CONTRAINED	ARD (SIC CARD). C), (ZERO, IZERD), (DN, IDN) EAD FIRST DATA CARD. EST FIRST FIELD. IF CARD WAS OT A SIC CARD, WRITE ERROR ESSAGE AND TERMINATE EXECUTION	SICR D008 SICR D012 SICR D014 SICR D014 SICR D020 SICR D024 SICR D024 SICR D028 SICR D028 SICR D028 SICR D028 SICR D028
DIMENSION V(10),DW(10),DW(10) E) UIVALENCE (SIC,1SIC), (DSIC,1DSIC), (ZERD,1ZEFD), (DW,1DN) DATA SIC,ZFPD /4HSIC,4H O/ READ(5,100) DSIC,(JM(1),1=1,10) IEST FIRST DATA CARD, MRITE ERROR WOT A SIC CARD, MRITE ERROR WOT A SIC CARD, MRITE ERROR WOT A SIC CARD, LOAD N ARRAY AITH COMPARE AND SET TECHNIQUE. O) 20 1=1,1C N(1) = 1 If (IDM(1),FQ,1ZEAJ) N(1) = 0 CARD READ AAS A SIC CARD, LOAD N(1) = 1 If (IDM(1),FQ,1ZEAJ) N(1) = 0 CALD N(1),FQ,1ZEAJ) N(1) = 0 CALD DAYA FRANK FXIT GAL DAYA FLAMIT(11A4) FOR AITH FROM SUMROUTINE SICPD STORM CARD FOR AND FOR SUMR EXECT OR SIC CARD IS SILT IN PRODEK LUCATION WITHIN) ATA DECK /IH ,5X,39H EXECUTION 11 FROM INTERFER BY STORM BY INTERFER BY INTERFER BY INTERFER BY INTERFER BY INTERFER BY STORM BY INTERFER BY STORM BY INTERFER BY INTERFER BY STORM BY STOR	OIMENSION W(10), DW(10), IDN(10) E PUIVALENCE (SIC, ISIC), (DSIC, IDS DATA SIC, ZEPO / 4HSIC, 4H O/ READ(5, 10C) DSIC, (DN(I), I = 1, 10) IF(IDSIC, NE, ISIC) GD TO 40 IF(IDSIC, NE, ISIC) GD TO 40 IF(IDN(I) = 1 IF(IDN(I) = 1) IF(IDN(I) = 1 IF(IDN(I) = 1	C), (ZERO, IZERO), (ON, ION) EAD FIRST DATA CARO. EST FIRST FIELD. IF CARO WAS OT A SIC CARO, WRITE ERROR ESSAGE AND TERMINATE EXECUTION	SICR D010 SICR D014 SICR D014 SICR D016 SICR D024 SICR D024 SICR D026 SICR D026 SICR D026 SICR D026 SICR D026
DIMENSION W(10), DW(10), IDW(10) DATA SIC, ZFPO / ZHSIC, 1981C), (DSIC, 1081C), (ZERO, IZEPO), (DW, IDW) DATA SIC, ZFPO / ZHSIC, 4H 0/ READ FIRST DATA CARD. READ FIRST BATA CARD. READ FIRST BATA CARD. IFST FIRST BATA CARD. MESSAGE AND TERMINATE ERROR MESSAGE AND TERMINATE ERROR MESSAGE AND TERMINATE ERROR MESSAGE AND TERMINATE ERROR MESSAGE AND TERMINATE BATA MARRAY AITH COMPARE AND SFT TECHNIQUE. RETURN FIRST DATA COMPANIATE BATA FOR ANTICHIA4) FOR ANTICHIA4) FOR ANTICHIA4) FOR ANTICHIA4, FOR ANTICHI	OIMENSION W(10), DW(10), IDW(10) E PUIVALENCE (SIC, ISIC), (DSIC, IDS DATA SIC, ZEPO /4HSIC, 4H O/ READ(5, 10C) DSIC, (DM(I), I = 1, 10) IF(IDSIC, NE, ISIC) GO TO 40 ON 20 I = 1, IC N(I) = 1 IF(IDM(I), FO, IZEAU) N(I) = 0 CONTINUE	C), (ZERO, IZEPO), (ON, IDN) EAD FIRST DATA CARD. EST FIRST FIELD. IF CARD WAS OT A SIC CARD, WRITE ERROR ESSAGE AND TERMINATE EXECUTION	SICR D012 SICR D014 SICR D016 SICR D022 SICR D024 SICR D024 SICR D025 SICR D026 SICR D036 SICR D036
### ##################################	E 101VALENCE (SIC, ISIC), (DSIC, IDS DATA SIC, ZEPO /4HSIC, 4H 0/ NEAD(5, 10C) DSIC, (DN(I), I=1,10) IF (IDSIC, NE. ISIC) GD TO 40 OP 20 I=1,1C N(I) = 1 IF (IDN(I), F0.12EAJ) N(I) = 0 CONTINUE	C), (ZERO, IZERO), (DN, IDN) EAD FIRST DATA CARO. EST FIRST FIELD. IF CARO WAS OT A SIC CARO, WRITE ERROR ESSAGE AND TERMINATE EXECUTION	SICRDO16 SICRDO16 SICRDO20 SICRDO20 SICRDO26 SICRDO26 SICRDO26 SICRDO26 SICRDO36
E PUIVALENCE (SIC, ISIC), (OSIC, IOSIC), (ZERR, IZERO), (ON, IDN) DATA SIC, ZEPO / 448IC, 444 0/ READ(5, ICC) DSIC, (CN(I), I=1,10) LEST FIRST DATA CARD, AS NOT A SIC CARD, WAITE ERROR MESSAGE AND TERMINATE EXECUTION, ARRAY AITH COMPARE AND SET TECHNIQUE. OCARD READ AS A SIC CARD, LOAD N ARRAY AITH COMPARE AND SET TECHNIQUE. DETAIN (I) = 1 IF (ION (I) - FQ. IZEAJ) N(I) = 0 CALL DUMA WAITE(4, 110) CALL DUMA FERRIC FXIT WAITE(4, 110) CALL DUMA FERRIC FXIT TECHNIQUE. FERRIC FXIT TECHNIQUE. TERMINATE SICPD SETURA FOR ANTICIDAS, ANTICOME SICPD SETURA FOR ANTICOME SICPD ATTICOME SICPD ATTICO	E PUIVALENCE (SIC, ISIC), (DSIC, IDS DATA SIC, ZEPO / 44 SIC, 44 0/ 8 E AD(5, 100) DSIC, (DN(I), I=1,10) IE(IDSIC, NE, ISIC) GD TO 40 ON(I) = 1 IE(IDN(I), E0, IZEAJ) N(I) = 0 ON IN(I) IE(IDN(I), E0, IZEAJ) N(I) = 0 ON IN(I) IE(IDN(I), E0, IZEAJ) N(I) = 0	C), (ZERO, IZERO), (ON, ION) EAD FIRST DATA CARO. EST FIRST FIELD. IF CARO WAS OT A SIC CARO, WRITE ERROR ESSAGE AND TERMINATE EXECUTION	SICRDO16 SICRDO16 SICRDO20 SICRDO20 SICRDO20 SICRDO26 SICRDO26 SICRDO30 SICRDO30
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READ(5,100) DSIC,(DN(1),1=1,10) READ(5,100) DSIC,(DN(1),1=1,10) TEST FIRST FIELD. IF CARD WAS NOT A SIC CARD, WRITE ERROR MESSAGE AND TERMINATE EXECUTION. IF(TOSIC,NF,1SIC) G) TO 40 CARD READ WAS A SIC CARD. LOAD NOTION BETON TECHNAUE. UT 20 I=1,10 CARD READ WAS A SIC CARD. LOAD NOTION BETON TECHNAUE. WRITE(F,110) CALL OUAD RETURN FPRANT(11144) FORWATITION FORWAT NOT CORRECT OR SIC CARD IS SICH AND TENDER WITHIN DATA DECK 71H 55x,39H EXECUTION ENDING TECHNIAL DATA CARD FORMAT NOT CORRECT OR SIC CARD SAND THE PROMINATE OR PROGRAM IN THE PROMINATE OF PROGRAM IN THE PROMINATE OF PROGRAM IN THE PROMINATE OF PROGRAM IN THE	READ(5,100) DSIC, (NA(I), I=1,10) READ(5,100) DSIC, (NA(I), I=1,10) IF(I)SIC, NF. ISIC) GO TO 40 On 20 I=1,10 N(I) = 1 IF(I)N(I) = 0 IF(I)N(I) = 0	AD FIRST DATA CARD. ST FIRST FIELD. IF CARD WAS T A SIC CARD, WRITE ERROR	S1CRD026 S1CRD026 S1CRD026 S1CRD026 S1CRD027 S1CRD036
READ(5,100) DSIC,(DN(I),I=1,10) TEST FIRST FIELD. IF CARD WAS NOT A SIC CARD, WRITE ERROR MESSAGE AND TERMINATE EXECUTION. IF(IDSIC,ME,ISIC) G) TD 40 CARD READ WAS A SIC CARD. LOAD NAITH COMPARE AND SET TECHNIQUE. O) 20 I=1,IC N(I) = 1 IF(IDN(I),F0.12EAJ) N(I) = 0 CARD READ WAS A SIC CARD. LOAD N(I) = 0 CONTINUE RETURN FORM INTO SICON FORM SUBROUTINE SICPD FORM INTO CORRECT OR SIC CARD IS AND IN DRADER HOCATION WITHIN DATA DECK /IH,5X,39H EXECUTE EVECUTE FORM IN DRADER HOCATION WITHIN DATA DECK /IH,5X,39H EXECUTE EVECUTE TO AND SUBROUTINE SICPD FORM IN DRADER HOCATION WITHIN DATA DECK /IH,5X,39H EXECUTE FORM IN DRADER HOCATION WITHIN DATA DECK /IH,5X,39H EXECUTE FORM IN DRADER HOCATION WITHIN DATA DECK /IH,5X,39H EXECUTE FORM IN DRADER HOCATION WITHIN DATA DECK /IH,5X,39H EXECUTE	READ(5,100) DSIC, (DN(1), [=1,10) IF(IDSIC, NE, ISIC) G) TO 40 On 20	AD FIRST DATA CARD. ST FIRST FIELD. IF CARD WAS T A SIC CARD, WRITE ERROR SCACE AND TERMINATE EXECUTION	SICR0026 SICR0026 SICR0026 SICR0036 SICR0036
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TEST FIRED. IF CARD WAS NOT A SIC CARD, WRITE ERROR NOT A SIC CARD, WRITE ERROR MESSAGE AND TERMINATE EXECUTION. CARD READ WAS A SIC CARD. LCAD N ARRAY WITH COMPARE AND SET TECHNIQUE. FRANK FXIT WAITE(4,110) CALL DUMA FORMATION FOR	F(I)SIC.*NF. SIC) G) TO 40 O	ST FIRST FIELD. IF CARD WAS TA SIC CARD, WRITE ERROR	\$1CRD028 \$1CRD030 \$1CRD032 \$1CRD032
IF(I)SIC.NF.ISIC) G) ID 40 MESSAGE AND TERMINATE EXECUTION. CARD READ AS A SIC CARD. LCAD N ARRAY AITH COMPARE AND SET TECHNIQUE. RETURN WAITE(4,110) CALL DUMD RETURN F) MAI(1) A) F) MAI(1) A) FOR AI(1) A FX,39H***** ERROR PRINT FROM SUBROUTINE SICPD STURN F) MAI(1) A) FOR AI(1) A FX,39H AND AICARD IS A) IN PROPER LUCATION WITHIN DATA DECK /IH +5X,39H EXECUTY END	F(I)SIC. NF. ISIC)	I A SIC CARD, WRITE ERROR SAACE AND TERMINATE EXECUTION	SICR0030 SICR0032 SICR0034
MESSAGE AND TERMINATE EXECUTION. JETTOSIC.NE.ISIC) 63 TO 40 CARD READ AS A SIC CARD. LOAD N ARRAY AITH COMPARE AND SET TECHNIQUE. TECHNIQUE. TECHNIQUE. TECHNIQUE. TECHNIQUE. TECHNIQUE. TERMINE FXIT TECHNIQUE. TERMINE FXIT TERMINE FXIT TERMINE FXIT TECHNIQUE. TERMINE FXIT TERMINATED FX SUGRAP TERMINATED FX SUGRAP TERMINATED FY SAUGRAP TERMINE FY SAUGRAP TERMINATED FY SAUGRAP TERMINE FY SAUGRAP TERMINATED	<pre>IF(I)SIC.MF.ISIC) G) T0 40 0.0 20</pre>	NOTECONX REVIEWATE ON A ROLL OF	SICR 3032 SICR 1034
IF(I)SIC.NF.ISIC) 63 TO 40 CARD READ AS A SIC CARD. LOAD N ARRAY AITH COMPARE AND SFT TECHNIQUE. LETION(I).FQ.IZEAJ) N(I) = 0 CONTINUE RETURN WRITE(4,110) CALL DUWA RETURN FOR ANTICINA SUBROUTINE SICPO FOR ANTICINA SUBROUTINE SICPO SIC DATA CARD FORMAT NOT CORRECT OR SIC CARD IS 2 / 14 , £x,934 SIC DATA CARD FORMAT NOT CORRECT OR SIC CARD IS 3 N) I IN PROPER LUCATION WITHIN DATA OFCK / 14 ,5 x,394 EXECUTA 4 III & IF WHINAIED BY DRUGRAP) END	F()S C.NE. S C)	DAME AND LENGTHANK ENCOURS.	S1CR10034
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N ARRAY AITH COMPARE AND SET	N(1) = 1 IF(10N(1),F0.125AJ) N(1) = 0	ARD READ MAS A SIC CARD. L	SICRU036
### TECHNIQUE. N(I) = 1	N(1) = 1 IF(10N(1),F0,125AJ) N(1) = 0	ARRAY AITH COMPARE AND S	S 1CR 0038
0.7 %	0. 10	ũ	SICRD04(
N(I) = 1 N(I) = 1 IF(IDN(I).FQ.IZEAJ) N(I) = 0 C.NTINUE RETURN WRITE(4,110) CALL DUMP CALL DUMP RETURN F.DRMAT(11A4) F.DRMAT(1A4A)	N(I) = 1 IF(ION(I).FQ.IZEAJ) N(I) = CONTINUE		SICROU42
IF(IDN(I).FQ.IZEAJ) N(I) = 0 C)NTINUE RETURN CALL DUMP F) PMAT(I1A4) F) FOR PRINT FROM SUBROUTINE SICPD F) PMAT(I1IA4) F) FX PMAT(IIIA4) F) FX PMAT(IIIA4) F) FX PMAT(IIIA4) F) PMAT(IIA44) F) PMAT(IIA444) F) PMAT(IIA444) F) PMAT(IIA4444) F) PMAT(IIA4444444444444444444444444444444444	TP(OZ().FO.IZEAU)		SICR0046
CONTINUE RETURN WRITE(4,110) CALL DUWA RETURN FORMAT(1114) FORMAT(1114) FORMAT(1111,5x,29H***** ERROR PRINT FROM SUBROUTINE SICPO FORMAT(1111,5x,29H***** ERROR PRINT FROM SUBROUTINE EXECUTION FORMINATED RY PRUGRAP) FORMINATED RY PRUGRAP)	は		SICRO048
RETUPN WRITE(4,110) CALL OUWD CALL OUWD RETURN F)**WAT(11A4) F)**WAT(11A			S1CR 2050
FRROR FXIT WAITE(4,110) CALL OUMP RETURN F)**MAT(11A4) FOR AA1(1H1,5x,79H***** ERROR PRINT FROM SUBROUTINE SICPO FOR AA1(1H1,5x,79H**** ERROR PRINT FROM SUBROUTINE SICPO Z /1H ,5x,93H SIC DATA CARD FORMAT NOT CORRECT OR SIC CARD IS 3M)T IN PROPER LUCATION WITHIN DATA OFCK /1H ,5x,39H EXECUTA			SICRDO52
WRITE(F,110) CALL OUMD RETURN FJRMAT(11A4) FJRMAT(11H1,5x,79H**** ERROR PRINT FROM SUBROUTINE SICPO FJRMAT(1H1,5x,79H**** ERROR PRINT FROM SUBROUTINE SIC CARO IS Z 71H ,5x,97H SIC DATA CARD FDRMAT NOT CORRECT OR SIC CARO IS 3w JT IN PROPER LUCATION WITHIN DATA OFCK /1H ,5x,39H EXECUTA		RRJR F	\$108-0056
CALL DUMP RETURN FJRMAT(11A4) FJRMAT(1H1,5x,79H***** ERROR PRINT FROM SUBROUTINE SICPO FJRMAT(1H1,5x,79H***** ERROR PRINT FROM SUBROUTINE SICPO Z 71H ,5x,97H SIC DATA CARD FORMAT NOT CORRECT OR SIC CARD IS 3M JT IN PROPER LUCATION WITHIN DATA OFCK /1H ,5x,39H EXECUTA	WAITE(4,11		SICRDOSE
RETURN FJRMAT(11A4) FJRMAT(11A4) FJRMAT(1HI,5x,29H***** ERROR PRINT FROM SUBROUTINE SICPO Z /1H ,5x,97H SIC JATA CARJ FORMAT NOT CORRECT OR SIC CARD IS 3N JT IN PROPER LUCATION WITHIN DATA OFOR /1H ,5x,39H EXECUTA	ርላፐር ህበሓን		S1CR 2060
FJYMAT(11A4) FJYMAT(1H1, FX, 23H**** ERROR PRINT FROM SUBROUTINE SICPO Z /1H , £X, 97H SIC JATA CARJ FORMAT NOT CORRECT OR SIC CARD IS 3N JT IN PROPER LUCATION WITHIN JATA OFOR /1H , 5X, 39H EXECUTA	RETURN		S1CR-)062
, 29H***** ERROR PRINT FROM SUBROUTINE SICPO SIC DATA CARD FORMAT NOT CORRECT OR SIC CARD IS LUCATION WITHIN DATA OFCK /1H ,5x,39H EXECUT/ ED RY 22GGRAM)			S1CR.0066
FUR 4A1(1H1, FX, 29H**** ERROR PRINT FROM SUBROUTINE SICPO 2 / 1H , £X, 97H SIC DATA CARD FORMAT NOT CORRECT OR SIC CARD IS 3A)T IN PROPER LUCATION WITHIN DATA OFOK /1H ,5X, 39H EXECUT/ 4TIC & TERMINATED RY DRUGRAM) END			S1CR 3068
2 /14 , Ex, 97H SIC DATA CARD FORMAT NOT CORRECT OR SIC CARD IS 34)T IN PROPER LUCATION WITHIN DATA DECK /1H ,5x,39H EXECUTA 4TIC A TERMINATED RY PROGRAM) END	FUR AAT (141, 5x, 23H*** ERROR PR	FROM SUBROUTINE SICP	S1CR 7070
34.)T IN PROPER LUCATION WITHIN DATA DECK /1H ,5x,39H EXECUT/ 4TICA TERMINATED RY PROGRAM) END	2 /14 , Ex, 97H SIC DATA CARD	AMAT NOT CORRECT OR SIC CARD I	S1CR 3072
FO BY DRUGRAM)	LUCATION WITHIN	DFCK /1H ,5X,39H E	451CP 1076
	FD RY 22LIGR		SICR 337
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2.2.1.2 Subroutine INITAL

Purpose:

INITAL is designed to set up the solution to be performed within TRAJ by taking the input data and storing the position and velocity vectors and the associated epoch in cells set aside for the purpose of computing the conic reference trajectory and the state transition matrix.

Deck Name:

INIT

Calling Sequence: CALL INITAL

Input/Output:

I/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	R, V	r, v	3, 3	SAT (5) SAT (8)	Radius and velocity vectors in the true equator of date frame of reference (Km, Km/sec)
1/0	TW, TF	^t o	1., 1	SAT (11, 12) WRF (50, 51)	Whole and fractional number of mean solar days elapsed since the reference ence epoch of 1950.0 (JD 2433282.423)
0	ROTATE ROTINV	NP PTNT	3 X 3 3 X 3	WRK (1) WRK (10)	Transformation matrices relating true equator of date frame of reference to the mean equator of 1950.0 system. (rp = NPr ₅₀)
0	RCON VCON	r _c (0) v _c (0)	3 3	WRK (28) WRK (31)	Position and velocity vectors used to describe the conic reference trajectory for the Encke integration (Km, Km/sec)
0	TCON TCONF	tc	1, 1	WRK (34) WRK (35)	The epoch corresponding to the radius and velocity vectors used to define the conic reference trajectory.

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
0	RTRAN VTRAN	r _{n-l} v _{n-l}	3	WRK (36) WR". (39)	Position and velocity vectors utilized to define the state from which errors will propagate to the time of data acquisition. These vectors are in the true equator of date frame. (Km, Km/sec)
0	TTRANW, TTRANF	tn-1	1, 1_	WRK (42) WRK (43)	The epoch defining the point from which errors will be propagated
0 ,	R50 V50	T50 V50	3	WRK (44) WRK (47)	Position and velocity vectors corresponding to R and V in the frame of 1950.0 (Km, Km/sec)
0	DR DV	4r äv	3 3	WRK (52) WRK (55)	Position and velocity vectors for the satellite relative to the conic reference trajectory (Km, Km/sec)
0	RCONIC VCONIC	r̂ c (t) v c (t)	3 3	WRK (117) WRK (120)	Position and velocity vectors on the conic reference trajectory at the epoch t (Km, Km/sec)
0	STATE	X (t)	6	STT (64)	The initial components of the vector composed of errors in the radius and velocity vectors (Km, Km/sec)

Subroutines Required: EQINOX (relates frame of date to 1950.0) MATMPY (matrix multiplication)

Functions Required: None

Approximate Deck

134 (octal)

Length:

Discussion:

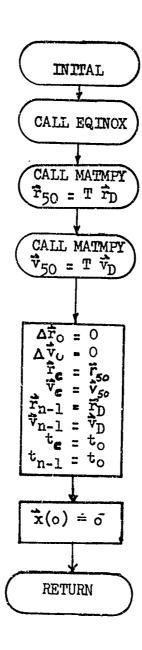
TNTTAL is intended to take the position and velocity vectors in the true equator of date frame of reference and compute the corresponding position and velocity vectors in the computational frame (the mean equator of 1950.0). This is accomplished by calling FQTMOY and performing the following multiplication

$$\vec{r}_{50} = p^{T} N^{T} \vec{r}_{D}$$

$$\vec{v}_{50} = p^{T} N^{T} \vec{v}_{D}$$

Having completed this operation, the vectors required to perform the integration of the trajectory and the computation of the state transition matrix are loaded into common. At this point, the process is completed by establishing the components of the initial state vector (i.e., $\{67, 60\}$).

Computational Logic:



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2.2.1.3 Subroutine POSVEL

Purpose:

POSVEL accepts data in for form of the orbital elements

and computes the position and velocity vectors corresponding to the epoch of the elements.

Deck Name:

POSVEL

Calling Sequence: CALL POSVEL (GM A, E, OINC, OMEGAW, OMEGA, TRETA,

R, V)

Input/Output:

I/o	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	GM	AL.	1	CON(4)	The product of Newton's gravitational constant and the mass of the Earth. (Km ³ /sec ²)
I	A E OINC ØMEGAW OMEGA THETA	ε :i :ω .Ω. Θ _Ο	1 1 1 1	Arg Arg Arg Arg Arg	The semi-major axis, eccentricity, orbital inclination, argument of perigee, longitude of the ascending node and true anomaly of epoch for the elliptical orbit of interest as expressed in the true equator and equinox of date frame of reference (Km, -, deg, deg, deg, deg)
0	R V	ř	3	SAT(5) SAT(8)	The position and velocity vectors in the true equator and equinox of date frame of reference (Km, Km/sec) (cartesian coordinates)

Subroutines Required: None

Functions Required:

(sine function) SIN, SIND (cosine function) COS, COSD

(square root) SQRT (arc tangent) ATAN

Approximate Deck

231 (decimal)

Length:

Formulation:

The orbital elements define a corresponding set of position and velocity components (in the same coordinate system). POSVEL is designed to compute this equivalent set of numbers by utilizing elliptic formulae. However, since these formulae are reasonably well known, they will not be developed; rather, those employed will be presented.

The elements which are assumed to be available make up a variation of the classic set to be specific.

- a semi-major axis (Km)
- e orbital eccentricity
- i orbital inclination to-the true equator of date (deg)
- ω argument of perigee (deg)
- Ω longitude of the ascending node relative to the true vernal equinox of date (deg)
- $\Theta_{\rm O}$ true anomaly of epoch (deg). This element is utilized rather than the time of perigee passage due to be fact that it simplifies the resolution process

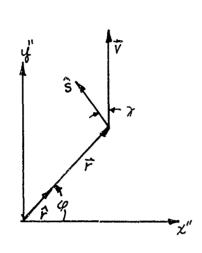
Thus, the dynamics of the problem is introduced through these elements by employing elliptic equations as follows:

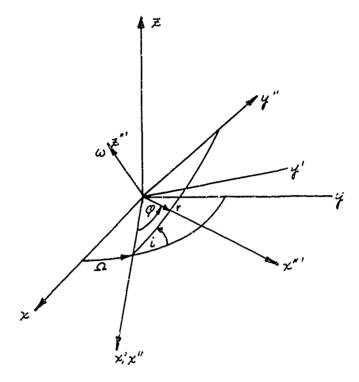
$$r_{0} = \frac{a(1-e^{2})}{1 + e \cos \theta_{0}}$$

$$v_{0} = \sqrt{u \left(\frac{2}{r_{0}} - \frac{1}{a}\right)}$$

$$v_{0} = \tan^{-1} \left[\frac{e \sin \theta_{0}}{1 + e \cos \theta_{0}}\right] \qquad -90 \le v_{0} \le +90$$
where
$$v_{0} = \sin^{-1} \left[\frac{\dot{r}_{0} \cdot \dot{v}_{0}}{r_{0} \cdot v_{0}}\right]$$

These quantities fail to fully establish the desired information, however, since the orientation of the plane of motion has not been introduced, this step is accomplished by referring to the following sketches.





r = r r

 $\vec{v} = v \sin \gamma \hat{r} + v \cos \gamma \hat{s}$

where $\hat{\mathbf{r}}$ and $\hat{\mathbf{s}}$ are obtained from

$$\begin{cases} \hat{\mathbf{r}} \\ \hat{\mathbf{s}} \\ \hat{\boldsymbol{z}} \end{cases} \equiv \begin{cases} \mathbf{x}^{u'} \\ \mathbf{y}^{u'} \\ \mathbf{z}^{u'} \end{cases} = \mathbf{T}_{\mathbf{Z}}(\boldsymbol{\phi}) \mathbf{T}_{\mathbf{X}}(\mathbf{1}) \mathbf{T}_{\mathbf{Z}}(\boldsymbol{\Omega}) \begin{cases} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \end{cases}$$

 $= \begin{cases} \cos \varphi \cos \Omega - \sin \varphi \cos i \sin \Omega & \cos \varphi \sin \Omega + \sin \varphi \cos i \cos \Omega \\ -\sin \varphi \cos \Omega - \cos \varphi \cos i \sin \Omega & -\sin \varphi \sin \Omega + \cos \varphi \cos i \cos \Omega \end{cases}$ $= \sin i \sin \Omega \qquad \qquad -\sin i \cos \Omega$

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cos \varphi sini \\
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y \\
z
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\right\}$

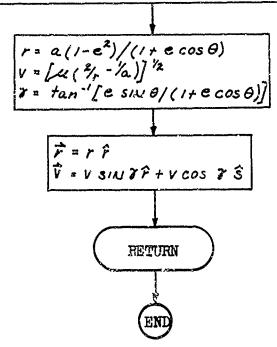
- and where $T_{\alpha}(\,\Omega\,\,)$ means the transformation constructed by rotating the coordinates about the Z - axis in a ccw sense through the angle α
 - $T_{\mathbf{v}}(\mathbf{i})$ means the transformation constructed by rotating the coordinates about the x - axis in a ccw sense through the angle i

 $\varphi = \theta + \omega$

Computational Logic:

POSVEL

 $\hat{F} = (\cos \phi \cos \Omega - \sin \phi \cos i \sin \Omega)\hat{X} + (\cos \phi \sin \Omega + \sin \phi \cos i \cos \Omega)\hat{Y} + \sin i \sin \phi \hat{Z}$ $\hat{S} = (\sin \phi \cos \Omega - \cos \phi \cos i \sin \Omega)\hat{X} + (-\sin \phi \sin \Omega + \cos \phi \cos i \cos \Omega)\hat{Y} + \cos \phi \sin i \hat{Z}$



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                                                                                                                                                   COMPUTATION OF RADIUS VELOCITY AND FLIGHT PATH ANGLE
             IFN(S)
                                                                                                                                                                              RAD =A*(1.-E*E)/(1.+E*CGSD(THETA))

VEL = SQRT( GM *( 2./RAD - 1./A))

GAM = ATAN( E*SIND(THETA)/(1.+E*CGSD(THETA)))
                                                                                                                                                                                                                                                              CONSTRUCTION OF POSITION AND VELOCITY VECTORS
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             SOURCE STATEMENT
                                                                                                                                                                                                                                                                                          D0 10 I = 1,3

V(I) = CGV * S(I) + SGV * R(I)

R(I) = RAD * R(I)
                                                                    = CP * SP * CP * CG
                                                                                              CP*CI*SB
                                                                                                           S(2) =-SP*SG + CP*C1*CG
                                                      SG #CI #SP
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                                                                                                                                                                                                                                   CGV = COS(GAM) * VEL
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R(3)

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RETURN

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2.2.1.4 Block DATA

Purpose:

BLOCK stores atmospheric density and lapse rate data and solar-lunar ephemeris data into cells utilized by subroutines ATMS and EPHEM, respectively. BLOCK is executed at the time the program is loaded; thus, the

routine is never called in the program.

Deck Name:

BLOCK

Calling Sequence:

None

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
0	ALT 1 ALT 2 ALT 3	h ₁ h ₂ h3	1 1 1	ATCON (1) ATCON (2) ATCON (3)	the altitudes in Km corresponding to the ranges over which lapse rate and density data for the 1962 U.S. standard atmosphere will be quoted.
0	REQT RPOL	R _e Rp	1 1	ATCON (4) ATCON (5)	the equatorial and polar radii of the earth in Km
0	STEP 1 STEP 2	Ah ₁	1	ATCON (6) ATCON (7)	the intervals at which density data are quoted (between h _l and h ₂ , and h ₂ and h ₃ , respectively)
0	RHOF RATE	, К	21 21	TABLE (1) TABLE (22)	the density and lapse rate for the 1962 U.S. standard atmosphere at the tabulated intervals
0	ЕРНАМ	to Atm vm rs, vs	1 1 270 66	EPHOM (1) EPHOM (2) EPHOM (3) EPHOM (4) EPHOM (274)	the date relative to 1950.0 (J.D. 2433282.423) at which the tabulated data begin (days), the time interval for solar ephemeris entries (days), the time interval for lunar ephemeris entries(days), position and velocity vectors for the moon (Km, Km/sec), and position and velocity vectors for the sun (km, Km/sec)

Subroutines Required: None

Functions Required: None

Approximate Deck Length:

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0.25787921E 0.48887521E

0.25836263E

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01, 0.21261606E

BL 0K 1200

BL 0K 1250 BL 0K 1260

8L 0K1270

BL 0K1240

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01, 0.21306460E 08, 0.29810207E 08,-0.13284796E 01, 0.21281333E 0.25901888E 02, 0.49201572E 69,-0.57606132E 0.49080602E 0.25926496E 0.49136171E 09,-0.57606748E 02, 016 02,

> 08,-0.13284121E 0.21318875E 0.29809216E 08,-0.13284449E

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0.21297985E 0.29810709E 08,-0.13285235E 01, 0.21270791E 08, 0.49118402E

0.29812188E DATA (EPHAM(I), 1=304,339)/ 1-0.57608C23E

08,-0.13285182E 0.25848795E 0.48991868E C. 49056256E

1 0.25891495E -0.57608055E -0.576093295 0.25809715E

01, 0.29814C70E 08,-0.13286313E 0.21243198E 0.29813546E -0.57615668E

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BLGCK

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		TABLE	SYMBGL RATE	ATCON ALT2 RPOL	ЕРН ОМ С0001.
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			SYMBOL RHOF	ALT1 REQT STEP2	EPHAM DECK

2.2.1.5 SUBROUTINE DADUMP

Purpose:

DADUMP prints the entire contents of the unlabeled COMMON region DATA. A complete description of the

output data may be found in Appendix (COMMON map).

Deck Name:

DADMP

Calling Sequence: CALL DEDUMP

Input/Cutput

1/0	FORTRAN Name	Dimension	COMMON/ Argument	Definition
I/O	DATA	525	COMMON	Unlabeled COMMON region composed of the subarrays CON, SAT, SDA, STT, WRK.
I	NOUT	1	CON(17)	Output tape number

Subroutines Required:

None

Functions Required:

None

Approximate Deck Length: 533 (octal)

Discussion:

The principal purpose of this routine is to provide a print-out of the pertinent conditions at program initiation. After reading the program input data and performing any necessary initialization, subroutine DADUMP is mechanized from subroutine INPUT by setting the flag CODUMP to a non-zero value (input data location 31).

Utilization of this option provides a permanent record of all of the numbers associated with a particular run (gravitational constants, etc.), and a convenient means of checking for system incompatibilities during program checkout.

F DADUMP SUBRGUTINE PE AATA. (CAN(15), SA TA (DATA (CAN(15), SA (
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SOURCE STATEMENT

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                                                                                                                                                                                                                                                                                                   NO, NSTT, (STT(J), J=NSTT, NSTTE )
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2.3 THE TRAJECTORY GROUP

The second of the major blocks included within the differential corrections program is the trajectory program. This group of routines evaluates the acceleration vector, integrates the acceleration to define the position and velocity and computes the data relative to the selected tracking stations. These functions are discharged by four separate driver routines.

1)	CONIC	(Generates conic reference trajectory for an Encke solution to the equations of motion - called from INGRAT)
2)	MOTION	(Generates the total acceleration vector for motion relative to the reference ellipse)
3)	INGRAT	(Integrates the acceleration vector obtained from MOTION and defines the position and velocity vectors)

4) TRAK (Defines the position and velocity vectors relative to the tracking stations and computes the predicted values of the observed data)

which are mechanized to function in conjunction with a master routine TRAJ. This master is discussed on the following pages and the manner in which these routines are incorporated into the total computational problem is demonstrated.

2.3.1 Subroutine TRAJ

Purpose:

TRAJ mechanizes the working portion of the program and serves as the means whereby the reference trajectory is computed and the tracking stations of the problem checked. Once entered, control is not returned to MAIN until the final data point is

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processed.

Deck Name:

TRAJEC

Calling Sequence:

CALL TRAJ

Input/Output:

		FORTRAN	Math		Common/	
L	I/0	Name	Name	Dimension	Argument	
	I	TCONW TCONF	^t conic	1	WRK(34) WRK(35)	TW and TF corresponding to the epoch at which the reference ellipse was defined (days).
	I	RVEC VVEC	rv	3 3	WRK(44) WRK(47)	The position and velocity vectors in the frame of 1950.0 (Km, Km/sec.)
	I	TW TF	t	1	WRK(50) WRK(51)	Whole & fractional part of the number of days since 1950.0 for present epoch (Days from J.D. 2433283.423)
	I	R RD	Δr Δv	3	WRK(52) WRK(55)	Position and velocity vectors defining the motion relative to the Encke ellipse (Km, Km/sec.)
	0	TIME	t-t _o	1.	WRK(104)	time in seconds since last reference trajectory rectification
	ဝ	RCONIC VCONIC	rc Vc	3 3	WRK(117) WRK(120	Position and velocity vectors at TW plus TF for the conic reference tra-jectory (Km, Km/sec.)

Subroutines Required: EPHEM (ephemeris for Sun and Moon position vectors)

MOTION (driver for evaluating the total acceleration

experienced by vehicle)

INGRAT (numerical integration driver)

EQINOX (routine for relating the true equator of date

to the mean equator of 1950.0)

TRAK (routine designed to compute topocentric data

for tracking stations)

Functions Required:

None

Approximate Deck

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Length:

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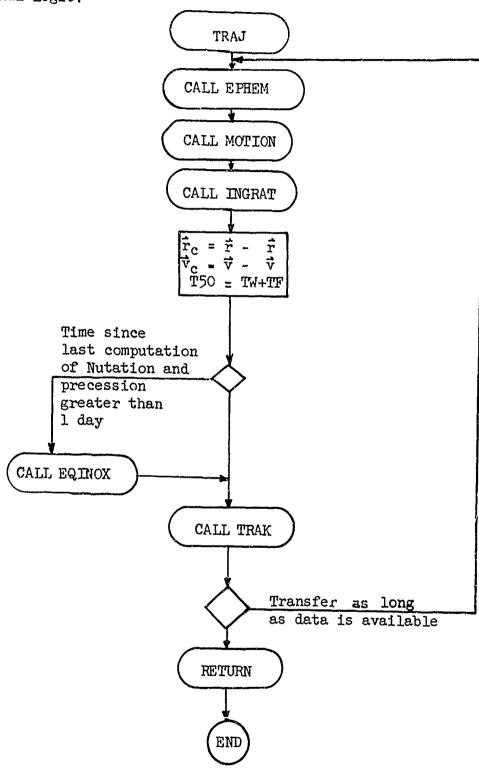
Discussion:

TRAJ does not in itself accomplish any portion of the required solution. Rather it is constructed for the purpose of sequencing the operations which are performed in generating the trajectory and checking the stations for visibility. In this sense, then, TRAJ is a direct extension of the program entitled MAIN and may appear unnecessary. However, for the purpose of checkout, it was deemed desirable to test the input and output functions of the program separately. Further, for the purpose of program appreciation and understanding it was deemed preferable to retain the checkout structure.

The first step taken upon entry into TRAJ is the computation of the solar and lunar position vectors (EPHEM) to aid in the computation of the gravitational and solar pressure contributions to the acceleration vector. This done, MOTION is entered for the purpose of computing the total acceleration vector and INGRAT is called for the purpose of estimating the position and velocity vectors at a time subsequent to the present epoch, (the step size for this integration is determined by the time interval between two successive data points and the magnitude of fifth difference of the acceleration vector as described in the discussion of the integration package). At this point, all vectors are known at the new epoch, time has been stepped, etc. and the conversion to the true equator of date from the mean equator of 1950.0 is defined. (For the sake of efficiency, this operation is performed only at one day intervals of time.) As a final step TRAK is called to determine if any of the tracking stations being employed observe the satellite and if there is data available at this epoch to process. (in the latter case, TRAK calls FILTER).

A transfer is constructed in TRAJ immediately after return from TRAK back to the computation of new solar and lunar position vectors. The cycle then repeats. Thus, on the surface there appears to be no means for the program to terminate. This conclusion is improper since at the time the last data point is processed, execution is terminated from within FILTER.

Computational Logic:



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2.3.1.1 Conic Reference Motion Group

The trajectory for the space vehicle is formulated in the Encke Manner to assure numerical precision. That is, the difference in the acceleration vectors for a vehicle moving on the true trajectory and an imaginary vehicle which is moving along a conic trajectory (selected in such a manner that \vec{r}_0 and \vec{v}_0 are equal for the two trajectories) is evaluated at every point. This differential acceleration is then integrated to obtain the differential position and velocity vectors and the true motion constructed by adding the reference position and velocities to the corrections.

This group of routines is designed to provide the reference \hat{r} and \hat{v} as functions of the time utilizing a deterministic set of variables to assure numerical significance in all computations. The group is completely self contained save for several math functions which are provided elsewhere in the program and for the gravitational constant which is acquired from common.

Subroutine CONIC

Purpose:

CONIC provides the conic reference trajectory to be utilized in conjunction with an Encke integration being performed in other portions of the program. The variables are those recommended by Dr. S. Herrick and are employed to avoid ambiguities in the solution as the eccentricity approaches zero or one and/or as the inclination of the reference orbit plane approaches zero.

Deck Name:

COM

Calling Sequence:

CALL CONIC (RO, SO, TIME, X, DTIME, R, V)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	RO SO	r _{co} v _{co}	3 3	Arg Arg	The position and velocity vectors at an arbitrary epoch in cartesian coordinates (Km, Km/sec.)
I	TIME	t	1	Arg	The time in seconds from the epoch of \vec{r}_0 , \vec{v}_0 to the epoch at which \vec{r} and \vec{v} are desired.
I/O	Х	Х	1	Arg	The eccentric anomaly variables $(E - E_0)$ defining the position at the desired time. The quantity is saved to aid in future iterative solutions for $Y = X$ (t)
I	DTIME	t	1	Arg	The incremental time in seconds since the previous solution yielded the value of X being fed back into CONIC

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
0	R V	Ť V	3 3	Arg	The radius and velocity vectors at time t (in the same coordinate frame as \vec{r}_0 , \vec{v}_0) expressed in Km and Km/sec.
I	GM	м	1	con(6)	The gravitational constant for the central body (Km 3/sec2)

Subroutines Required: SEARCH (numerical-analytic search for the position

variable satisfying the time constraint)

Functions Required: DOT (vector dot product)

AMAG (vector magnitude)
COSH (hyperbolic cosine)

SINH (hyperbolic sine)

COS (cosine)
SIN (sine)

SQRT (square root)

Approximate Deck

Length:

420 (octal)

Formulation:

The equations of motion for the central force problem are

$$\dot{\vec{r}} = -\frac{\mu}{r^3} \dot{\vec{r}} \tag{1}$$

Thus, the rate of change of the angular momentum vector is

$$\frac{d}{dt}(\hat{h}) = \hat{r} \times \hat{E} = \hat{r} \times \left(-\frac{\mathcal{M}}{r^3}\right) \hat{r} = 0$$
 (2)

This equation states that the angular momentum (thus the plane of motion) of the resultant conic is constant and leads directly to the fact that any vector in the plane can be constructed by linear combination of any two vectors selected. i.e.,

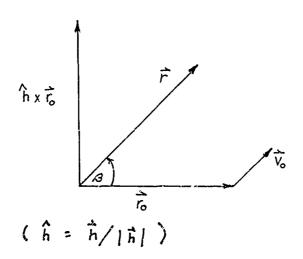
$$\vec{r} = f \vec{r}_0 + q \vec{V}_0 \tag{3}$$

Further, since \vec{r}_0 and \vec{v}_0 are constants and since $\vec{v} = d/dt$ (\vec{r})

$$\vec{\nabla} = \vec{f} \ \vec{r}_o + \vec{q} \ \vec{V}_o \tag{4}$$

This representation of \tilde{r} and \tilde{v} is completely definitive for all conic trajectories and exhibits none of the ambiguities or indeterminances encountered with the solution employing the classic set of elements (a, e, i, ω , α , Mo). For this reason, equations 3 and 4 will be employed in this program and attention will be turned to the evaluation of the quantities f, g, f and g

Consider the following sketch which illustrates motion in the orbit plane



$$\vec{r} = \frac{r}{r_0} \cos \beta \vec{r_0} + \frac{r}{r_0} \sin \beta \vec{h} \times \vec{r_0}$$

$$= \frac{r}{r_0} \cos \beta \vec{r_0} + \frac{r}{r_0} \sin \beta \left[\vec{v_0} r_0^2 - \vec{r_0} (\vec{r_0} \cdot \vec{v_0}) \right]$$

$$= \frac{r}{r_0} \left(\cos \beta - \frac{\vec{r_0} \cdot \vec{v_0}}{r_0} \sin \beta \right) \vec{r_0} + \frac{r}{r_0} \sin \beta \vec{v_0}$$

Now since equations 3 and 5 represent the same vector

$$f = \frac{r}{r_0} \left(\cos \beta - \frac{r_0 \cdot \vec{v_0}}{h} - \sin \beta \right) \tag{6}$$

$$g = \frac{rr_0}{h} \sin \beta$$

$$h = \sqrt{u\rho} = \sqrt{u \, a \, (1 - e^2)}$$

$$(7)$$

where

The basic problem at this point now reduces itself to the evaluation of the angle $\mathcal B$ in terms of variables which can be related to time through the dynamics of the motion. This task requires that equation 1 be integrated and that the solution shown to be conic. However, since this process has been accomplished in such a large number of references (e.g., Reference 1), the solution is assumed to be known and the angle $\mathcal B$ is recognized to be the difference in the true anomalies at positions corresponding to $\hat{r_0}$ and \hat{r} .

Under these observations the trigonometric functions $\sin \varnothing$ and $\cos \varnothing$ may be reduced to functions of the eccentric anomaly (selected due to the fact that Kepler's equation will be utilized to obtain f, g, f and g as function of time) by substituting the following identities:

$$\sin \Theta = \alpha \sqrt{1 - e^2} \quad \sin E \tag{8}$$

$$\cos \theta = \frac{a}{r} \left[\cos E - e \right] \tag{9}$$

$$\sin \beta = \sin (\theta - \theta_0) = \sin \theta \cos \theta_0 - \sin \theta_0 \cos \theta$$

$$= \frac{a^2}{rr_0} \sqrt{1 - e^2} \left[SE(CE_0 - e) - SE_0(CE - e) \right]$$

$$= \frac{a^2}{rr_0} \sqrt{1 - e^2} \left[SECE_0 - SE_0CE \right] - e(SE - SE_0)$$

$$= \frac{a^2}{rr_0} \sqrt{1 - e^2} \left[SX - e(SE - SE_0) \right]$$

$$= rr_0$$
(10)

where: the notation $s \propto = \sin \alpha$; $c \propto = \cos \infty$ and $X = E - E_0$ but $SE = \sin (E_0 + X)$ $= sXcE_0 + cX SE_0$

so that

$$sin \mathcal{B} = \frac{\alpha^{2}}{rr_{o}} \sqrt{1-e^{2}} \left[SX \left(1-eCE_{o} \right) + eSE_{o} \left(-cX+I \right) \right]$$

$$= \frac{\alpha^{2}}{rr_{o}} \sqrt{1-e^{2}} \left[\frac{r_{o}}{a} SX + \frac{\vec{r}_{o} \cdot \vec{V}_{o}}{\sqrt{\mu a}} \left(1-cX \right) \right]$$
(11)

similarly

$$\cos \beta = \cos \theta \cos \theta_{0} + \sin \theta \sin \theta_{0}$$

$$= \frac{\alpha^{2}}{rr_{0}} \left[(CE - e)(CE_{0} - e) + (I - e^{2}) SE SE_{0} \right]$$

$$= \frac{\alpha^{2}}{rr_{0}} \left[(CECE_{0} + SESE_{0}) + e^{2}(I - SESE_{0}) - e(CE + CE_{0}) \right]$$

$$= \frac{\alpha^{2}}{rr_{0}} \left[Cx + e^{2} \left[I - (SxCE_{0} + CxSE_{0}) SE_{0} \right] - e(CxCE_{0} - SxSE_{0} + CE_{0}) \right]$$

$$= \frac{a^2}{rr_o} \left[c_X + e^2 - e^2 SXCE_o SE_o - e^2 CX SE_o^2 - eC XCE_o + e SXSE_o - eCE_o \right]$$
(12)

which can be grouped and reduced as follows

$$coo \mathcal{B} = \frac{\alpha^{2}}{rr_{o}} \left[(cx - ecxcF_{o}) + e^{2}sE_{o}^{2}cx + r_{o} \right]$$

$$= \frac{\alpha^{2}}{rr_{o}} \left[\frac{r_{o}}{\alpha} cx - \frac{r_{o} \cdot \vec{v}_{o}}{ra} cx + esE_{o} + (e^{2}) - (ecE_{o}) \right]$$

$$= \frac{\alpha^{2}}{rr_{o}} \left[\frac{r_{o}}{\alpha} cx - \frac{r_{o} \cdot \vec{v}_{o}}{ra} cx + sx \left(\frac{r_{o}}{ra} \frac{\vec{r}_{o} \cdot \vec{v}_{o}}{raa} \right) + \left(l - \frac{\rho}{\alpha} \right) - \left(l - \frac{r_{o}}{ra} \right) \right]$$

$$= \frac{\alpha^{2}}{rr_{o}} \left[\frac{r_{o}}{r_{o}} (cx + l) - \frac{r_{o} \cdot \vec{v}_{o}}{raa} cx + sx \left(\frac{r_{o}}{ra} \frac{\vec{r}_{o} \cdot \vec{v}_{o}}{raa} \right) - \frac{r_{o}^{2} \cdot v_{o}^{2}}{raa} \left(l - r_{o} \cdot \vec{v}_{o} \right)^{2} (l - cx) + sx \left(\frac{r_{o}}{r_{o}} \frac{\vec{r}_{o} \cdot \vec{v}_{o}}{raa} \right) - \frac{r_{o}^{2} \cdot v_{o}^{2}}{rr_{o}} \left[-\frac{r_{o}}{r_{o}} \left(l - cx \right) + \left(\frac{\vec{r}_{o} \cdot \vec{v}_{o}}{raa} \right)^{2} (l - cx) + sx \left(\frac{r_{o}}{r_{o}} \frac{\vec{r}_{o} \cdot \vec{v}_{o}}{raa} \right) - \frac{r_{o}^{2}}{rr_{o}} \left[-\frac{r_{o}}{r_{o}} \left(l - cx \right) + \left(\frac{\vec{r}_{o} \cdot \vec{v}_{o}}{raa} \right)^{2} (l - cx) + sx \left(\frac{r_{o}}{r_{o}} \frac{\vec{r}_{o} \cdot \vec{v}_{o}}{raa} \right) - \frac{r_{o}^{2}}{rr_{o}} \left[\frac{r_{o}^{2}}{rr_{o}} \cdot \vec{v}_{o} \right] - \frac{r_{o}^{2}}{rr_{o}} \left[\frac{\vec{r}_{o} \cdot \vec{v}_{o}}{raa} \right] + sx \left(\frac{r_{o}}{r_{o}} \frac{\vec{r}_{o} \cdot \vec{v}_{o}}{raa} \right) + \left(\frac{r_{o}^{2}}{rr_{o}} \right)^{2} \right]$$

$$+ \left(\frac{r_{o}^{2}}{r_{o}} \right)^{2}$$

Finally, Kepler's equation in terms of the time of transit from \vec{r}_o to \vec{r} can be obtained as

$$\frac{Z}{a^{3}}(t-t_{o}) = (E-esE) - (E_{o}-esE_{o})$$

$$= X - e(SE-SE_{o})$$

$$= X - e(SxCE_{o} + CxSE_{o} - SE_{o})$$

$$= X + sx(-ecE_{o}) - esE_{o}(1-cx)$$

$$= X - (1-\frac{r}{a})sx - \frac{\vec{r}_{o} \cdot \vec{V}_{o}}{\sqrt{x}a}(1-cx)$$

$$= (X-sx) + \frac{r_{o}}{a}sx - \frac{\vec{r}_{o} \cdot \vec{V}_{o}}{\sqrt{x}a}(1-cx)$$
(15)

and the quantities f and g determined as follows

$$f = \frac{r}{r_0} \left(\frac{\cos \beta - \frac{r}{r_0} \cdot \vec{V}_0}{\sqrt{up}} \right)$$

$$= \left(\frac{a}{r_0} \right)^2 \left\{ \left(1 - Cx \right) \left[\frac{\left(\vec{r}_0 \cdot \vec{V}_0 \right)^2 - r_0}{\sqrt{u}a} \right] + sx \left(\frac{r_0}{a} \frac{\vec{r}_0 \cdot \vec{V}_0}{\sqrt{u}a} \right)$$

$$+ \left(\frac{r_0}{a} \right)^2 \right\} + \left(\frac{a}{r_0} \right)^2 \frac{\sqrt{1 - e^2} \vec{r}_0 \cdot \vec{V}_0}{\sqrt{u}a \left(1 - e^2 \right)} \left\{ \frac{r_0}{a} sx \right\}$$

$$+ \frac{\vec{r}_0 \cdot \vec{V}_0}{\sqrt{u}a} \left(1 - cx \right) \right\}$$

$$f = I - \frac{a}{b} \left(I - c x \right). \tag{16}$$

similarly

$$g = \frac{rr_o}{\sqrt{ua(1-e^2)}} \left\{ \frac{a^2}{rr_o} \sqrt{1-e^2} \left[\frac{r_o}{a} SX + \frac{\vec{r}_o \cdot \vec{V_o}}{\sqrt{u \cdot a}} (1-cX) \right] \right\}$$
$$= \sqrt{\frac{a^3}{u}} \left[\frac{r_o}{a} SX + \frac{\vec{r}_o \cdot \vec{V_o}}{ua} (1-cX) \right]$$

which may be simplified by observing the form of Kepler's equation to yield

$$g = \sqrt{\frac{a^{3}}{u}} \left[\frac{r_{o}}{\alpha} SX + \sqrt{\frac{u}{a^{3}}} (t \cdot t_{o}) - (X - SX) - \frac{r_{o}}{\alpha} SX \right]$$

$$= (t - t_{o}) - \sqrt{\frac{a^{3}}{u}} (X - SX)$$
(17)

The coefficients \hat{f} and \hat{g} can now be determined by differentiating Kepler's equation as follows:

$$\frac{d}{dt} \left[\sqrt{\frac{\mathcal{U}}{a^{3}}} (t \cdot t_{o}) \right] = \frac{d}{dt} \left[(E - e \sin E) - (E_{o} - e \sin E_{o}) \right]$$

$$\int \frac{\mathcal{U}}{a^{3}} = \dot{E} (I - e \cos E)$$

$$= \dot{E} \frac{\pi}{a}$$

or

$$\dot{E} = \dot{X} = \frac{1}{r} \sqrt{\frac{\omega}{a}} \tag{18}$$

and by returning to equation 3 to note that

$$\dot{f} = \frac{d}{dt}(f)$$

$$= \frac{a}{r_0} \frac{d}{dt}(CX) = -\frac{a}{r_0} SX \dot{X}$$

$$= -\sqrt{\frac{au}{rr_0}} SX$$

$$= -\sqrt{\frac{a}{rr_0}} (1 - CX)(\frac{1}{r} \sqrt{\frac{u}{a}})$$

$$= 1 - \frac{a}{r}(1 - CX)$$

$$= 1 - \frac{a}{r}(1 - CX)$$

and

Equations 3, 4, 15, 16, 17, 19, and 20 now provide the complete description of the conic motion problem in a completely deterministic set of variables. These equations are utilized as follows to define \vec{r} and \vec{v} as functions of $t-t_0$:

- 1) solve 15 for X (iterative)
- 2) solve 16, 17, 19, and 20 for f, g, f and g
- 3) solve 3 and 4 for $\dot{\vec{r}}$ and $\dot{\vec{v}}$

At this point Dr. S. Herrick's notation in "Universal" variables (Reference 2) can be adopted by defining the following quantities

$$\hat{S} = \sqrt{a} \quad S \times$$

$$\hat{C} = \alpha (1 - C \times)$$

$$\hat{V} = \alpha^{\frac{4}{2}} (X - S \times)$$

$$T = \sqrt{u} (\xi - \xi_0)$$

$$\hat{V}' = \vec{V} / \sqrt{u}$$

(20)

and f', g', \dot{f}' , and \dot{g}' can now be expressed in the form in which they will be coded.

$$f' = 1 - \frac{\hat{\zeta}}{r_0}$$

$$g' = \sqrt{u} g = \hat{I} - \hat{U}$$

$$\dot{f}' = \frac{\hat{\zeta}}{r_0} = \frac{\hat{\zeta}}{r_0}$$

$$\dot{g}' = 1 - \hat{\zeta}_{r_0}$$

It is noted that at every step in the development of these equations the implicit assumption of elliptic motion has been made (see equation 8). However, since for hyperbolic motion

$$a_h$$
 = negative
 F = i E
 $F - F_0$ = Y = i X

only the following modifications need be made to provide for a hyperbolic reference orbit capability

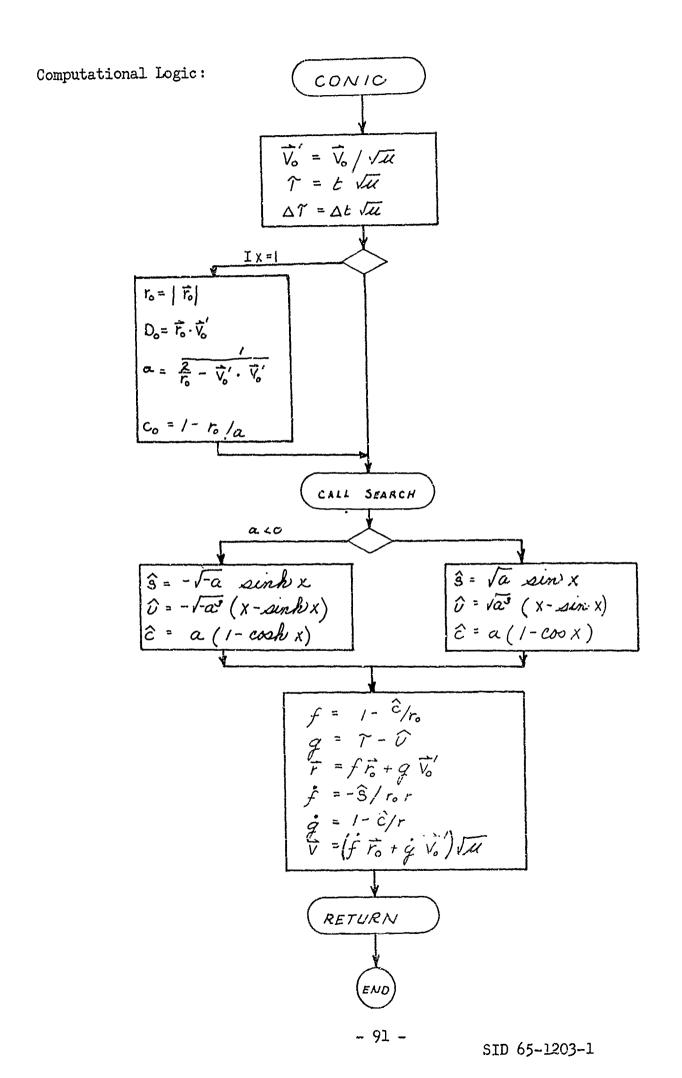
$$\hat{S} = -\sqrt{-a_h} \quad sinh \quad Y$$

$$\hat{C} = a_h \left(1 - \cosh Y \right)$$

$$\hat{D} = -\sqrt{-a_h^3} \left(Y - sinh Y \right)$$

Thus, this generalization will be included.

- 1. Townsend, G. E., "Orbital Mechanics" Chapter 3 in The Orbital Flight Handbook, NASA SP-33 Part 1, 1964.
- 2. Herrick, S., "Universal Variables" published by the author, University of California (L.A.) November 2, 1964.



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FFN 60 30

2.3.1.1.1 Subroutine SEARCH

Purpose:

SEARCH is the iterative logic utilized to solve Kepler's equation for the position variable X (see CONIC) as a function of the time elapsed

since the epoch of ro, vo.

Deck Name:

LOOK

Calling Sequence:

CALL SEARCH (TAU, DTAU, X)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	TAU	7	1	Arg	Universal time variable defined by $\tau = \sqrt{u} t$
I	DTAU	۵۲	1	Arg	the change in tau since the solution was last iterated. (Tau for first solution)
I	ELEM	T _O D _O a C _O	1	WRK(130)	the array of constants describing the nature of the motion
0	Х	Х	1	Arg	the eccentric (hyper- bolic) anomaly variable defining position on a conic section as a function of $t-t_0$

Subroutines Required:

None

Function Required:

PARTL

(partial derivative of Keplers equation with respect to X)

Function Required (continued) TIME (Time relative to the epoch

of r_0 , v_0)

SQRT (square root)

SIGN (function for attaching the

sign of one variable to

another)

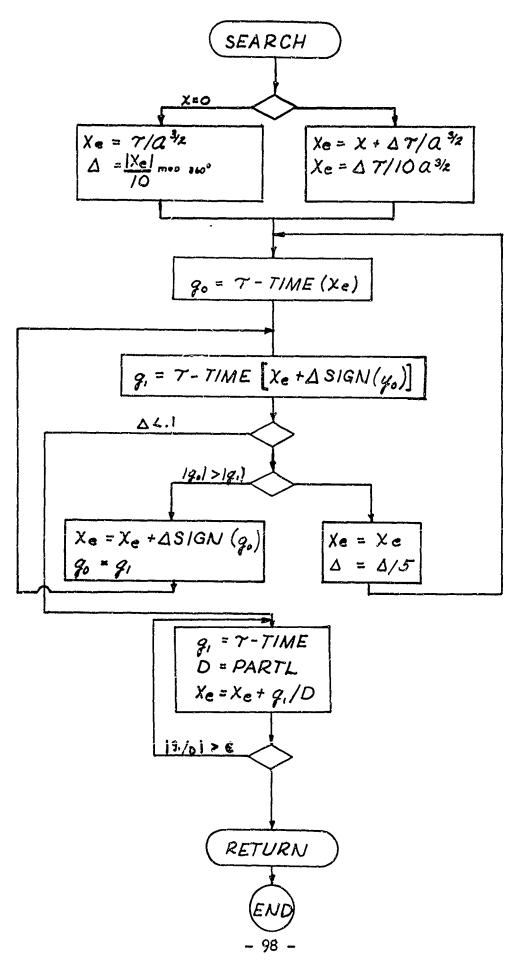
ABS (absolute value)

Approximate Deck Length: 190 (decimal)

Discussion:

SEARCH solves a monotonic transcendental equation of one degree of freedon in a two stage iteration process. First, a guess of the solution is made and the function evaluated at the guess and at the guess plus a fixed increment. The error in the functions are then computed and the value of guess which produced the smallest error in an absolute sense is saved. The process then repeats itself until the desired solution is approached. At this time, the step size is reduced and the search continued in stages until the error in the desired root is small enough to assure that a Newton type iteration will converge to the answer. At this time a variable step size is computed based on the error in the function and the slope of the transcendental equation at this argument.

SEARCH may, thus, be constructed as a general purpose routine for functions of this type with provision for incorporating a means of generating the initial guess, the transcendental function being solved, and an analytic partial of the function with respect to its argument. This approach has been taken in the routine being discussed with minor revision for the sake of brevity and with only the specific application in mind (that of solving Kepler's equation of the anomaly variable as a function of time).



SID 65-1203-1

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	102	11 21 20 DECK

2.3.1.1.2 Function TIME

rurpose:

TIME is the function which computes the difference

in the epochs at two points on an arbitrary conic

section.

Deck Name:

TIME

Calling Sequence:

TIME (X)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	Х	Х	1	Arg	the eccentric or hyperbolic anomaly variable defining position relative to that of an initial epoch
I	ELEM	l. D _G	1 1	WRK(130)	array of constants used to describe the conic section.
0	TIME	C _o	1	-	the normalized time variable γ (t - t_0)

Subroutines Required:	None	
Functions Required:	COS SIN COSH SINH SQRT	<pre>(cosine) (sine) (hyperbolic cosines) (hyperbolic sine) (square root)</pre>
Approximate Deck Length:	150	(decimal)

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                                                                                                                                                                                                                                                                                                                                      TIME=XHAT*ELEM(1)+CHAT*ELEM(2) +UHAT*ELEM(4)
                                                                                                                                                                                                                                                                                                                         XHAT=SQRT ( ABS ( EL. EM ( 3 ) ) ) *X * S I GN ( AA , EL EM ( 3 ) )
               SGURCE STATEMENT
                                                                                                                                                                                                                                        IF(ELEM(3)) 1,2,2
UHAT=SQRT(-ELEM(3)**3)*(X-SINH(X))*(-1.)
                                                                                                                                                                                               (WRK (130), ELEM
                                                                                                                                        (DATA(391); WRK
                                                                                                                                                                                                                                                                                              UHAT=SORT(ELEM(3) **3) *(X-SIN(X))
                                                                                                                                                                                                                                                                   CHAT=ELEM(3) * (1, -COSH(X))
                                                                                                                                                                                                                                                                                                            CHAT=ELEM(3) *(1, -COS(X))
               EFIN
                  ı
                                                                                    DIMENSION WRK(I)
                                                                                                                                                                     DIMENSION ELEM(4)
                                                         FUNCTION TIME(X)
                                                                                                                                         EQUIVALENCE
                                                                                                                                                                                               EQUIVALENCE
                                                                                                               COMMON DATA
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FS305				SYMBOL Data		SYMBOL F.000C CHAT		TIME		SORT		E FN	SID 65-1203-1 - 105 -

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2.3.1.1.3 Function PARTL

Purpose:

PARTL provides the derivative of Kepler's equation

with respect to the anomaly variable (X).

Deck Name:

PART

Calling Sequence:

PARTL (X)

Input/Output:

1/0	FORTRAN Name	Math Neme	Dimension	Common/ Argument	Definition
I	Х	Х	1	Arg	the eccentric or hyper- bolic anomaly variable defining position relative to that of an arbitrary initial epoch
I	elem	ro Do a	1 1 1	wrk(130)	array of constants used to describe the conic section
0	PARTL	<u>37</u> 3x	1	-	the partial derivative of the normalized time variable with respect to X

Subroutines Required:

None

Functions Required:

cos (cosine)

sin (sine)

cosh (hyperbolic cosine)

sinh (hyperbolic sine)

SQRT (square root)

Approximate Deck Length

120 (decimal)

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PARTCO8C
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PARTC170
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PART0230
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11/23/85
             1
           IFN(S)
                                                                                                                                                                                                                                           F3 =-SQRT(-A*A*A) *(1.-CUSH(X))
PARTL = ELEM(1)*F1 + LLEM(2)* F2 + ELEM(4)* F3
           SGURCE STATEMENT
                                                                                                        (DATA(391), WRK
                                                                                                                                                (WRK(130), ELEM
                                                                                                                                                                                                   * (1. -COS(X))
            E II
               i
                                           FUNCTION PARTL(X)
                                                                                                                            DIMENSIGN FLEM(4)
                                                                                                                                                                                                 = SORT(A*A*A)
                                                                DIMENSION ARK(1)
                                                                                                                                                                     IF(A) 10,19,20
                                                                                                                                                                                                                                =-A*SINH(X)
                                                                                                                                                                                        = \Delta \times SIN(X)
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                                                                                                                                                                              FI = SORT(A)
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LENGTH	LGCATION 01007	LGCATIGN 01016
00001	SYMBOL ELEM	VARIABLES SYMBØL F1
O	TYPE R	PROGRAM TYPE R R
GRIGIN	L BC A T J B N 90606	UNDIMENSIGNED PROGRAM VARIABLES LOCATION TYPE SYMBOL
`	SYMBOL WRK	SYMBOL A F3
COMMON BLOCK	TYPE R	TYPE R R
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	SYMBOL Data	SYM80L F.00CC F2

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SID 65-1203-1

08

2.3.1.2 MOTION and the Motion Group

This group consists of those routines designed to evaluate the acceleration vector in the mean equation of 1950.0 frame (selected to eliminate terms in the equations of motion resulting from rotating coordinate systems). Forces resulting from

- 1) the earth's oblateness
- 2) atmospheric drag
- 3) displacement from the reference conic
- 4) solar radiation pressure
- 5) solar-lunar gravitational forces

are all included and the group is designed to be complete to itself in that it contains all routines (save general purpose math routines) necessary to evaluate the forces in question (i.e., an atmospheric routine, an ephemeris routine and a solar power function). These routines will be discussed on the following pages.

Subroutine MOTION

Purpose:

MOTION serves as the driver routine for all of the previously discussed routines in the Motion Group (i.e., it is designed to compute the differential acceleration vector which will be integrated to define the trajectory as a function of time).

Deck Name:

MOTN

Calling Sequence:

Call 'OTION (ISTART, INDEX)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
O	RC O VC O	rco vco	3 3	WRK (28) WRK (31)	the conic position and velocity vectors to be utilized in subsequent computations of the reference trajectory if the orbit is rectified in FNCKF (Em, Km/sec)
0	TWCON TFCCN	t	1	WRK (34) WRK (35)	the time of the last rectification of the conic reference (Julian date in days)
I	R V	1º 4>	3 3	WRK (44) WRK (47)	radius and velocity vectors on the true trajectory (Km and Km/sec) in the frame of 1950.0
I	TW TF	t	1	WRK (50) WRX (51)	whole and fractional part of the date (days) relative to J.D. 2433282.423
I	DR DRDOT RDD	af Af Af	3 3 3	WRK (52) WRK (55) WRK (58)	displacement, velocity and acceleration vectors relative to the reference conic in the frame of 1950.0 (Km,Km/sec)

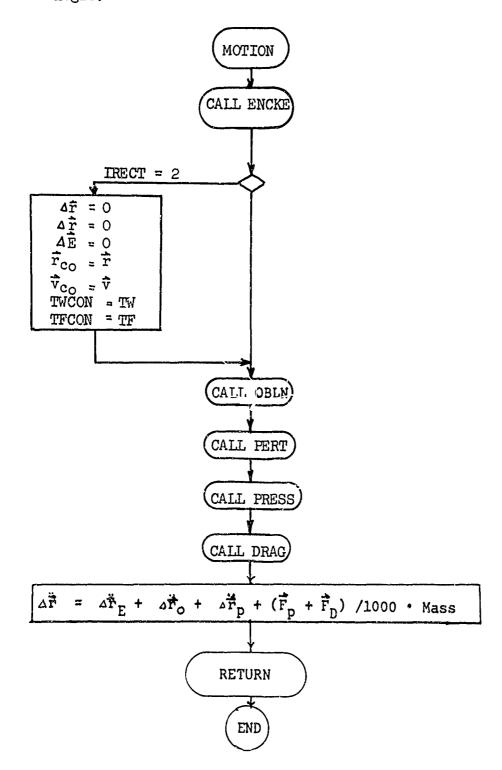
I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	RCONIC VCONIC	3rc 1∨ c	3	WRK (117) WRK (120)	radius and velocity vectors defining the present esti- mate of the conic reference path (Km, Km/sec)
0	ISTART	-	1	ARG	counter which is equal to l set upon rectifying the conic reference to restart the numerical integration
I	INDEX	-	1.	ARG	counter used to identify the source of the call of motion (TRAJ or START)

Piscussion:

No discussion of MOTION as an independent routine is considered essential except insofar as two points are concerned. First, upon exit from FNOVE, a test is made to determine if ENOVE considered the displacement from the conic reference to be excessive. If so, the conic is rectified, the differential position and velocity vectors are zeroed, the epoch is recorded as the time of rectification, and the ENOVE acceleration is zeroed prior to evaluating all of the other accelerations.

The other point is that since the forces due to drag and solar radiation pressure are expressed in newtons and since the accelerations are being evaluated in Km/sec² rather than m/sec², the resultant force vector must be divided by 1,000 times the mass to obtain consistent units.

Computational Logic:



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                                                                                                                                                                   THE EARTHS OBLATENESS (OBLN), SOLAR RADIATION PRESSURE (PRESS) AND ATMOSPHERIC DRAG, OTHER FURCES CAN BE ADDED
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                                                                                                 SERVES AS THE DRIVER ROUTINE IN THE COMPUTATION OF ALL ACCELERATIONS BEING EXPERIENCED. THE ROUTINE PRESENTLY
                                                                                                                                                                                                    WHEN THEY CAN BE DESCRIBED ( METEOROID IMPACT, MAGNETIC DRAG, HIGHER ORDER TERMS IN THE EARTHS POTENTIAL ).
                                                                                                                                                                                                                                                                           NECESSARY UNLESS DATA IS DESIRED IN ANDTHER FRAME (FOR
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SOURCE STATEMENT

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MOTNO730 MOTNO740 MOTNO750 MOTNO760 MOTNO770

IFN(S)

SOURCE STATEMENT

MTN

CALL PRESS(FS)
CALL DRAG(FD)
DO 1 I=1,3
PDD(I) = AE(I) + AO3(I)+ AP(I) +(FS(I)+FD(I))/(SMASS*1000.)
RETURN
END

SID 65-1203-1 -113-

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2.3.1.2.1 Subroutine OBLN*

Purpose:

To compute the non-central nature of the force (expressed in the mean equator of 1950.0 frame) exerted on the satellite resulting from the second, third and fourth spherical harmonics of the Earth's

potential function.

Deck Name:

OBIN

Calling Sequence:

Call OBLN (ACCEL)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
0	ACCEL	F'	3	Arg	the difference in the force per unit mass exerted by the model of the Earth and the central force for the same satellite position
I	RE	R _e	1	CON (1)	equatorial radius of the Earth (Km)
I	CJ,CH,CD	J,H,D	1,1,1	CON (3,4,5)	second, third and fourth coefficient of Jeffrey's potential function
I	GM	μ	1	CON (6)	gravitational constant for the Earth (Km ³ /sec ²)
I	AN	NP	3 x 3	WRK (1)	the rotational matrix relating the frame of 1950.0 to the true equator of date
I	RVEC	ŕ	3	WRK (44)	radius vector in the frame of 1950.0

^{*} Note: This routine is a version of a routine by the same name originally prepared by JPL (one reference is JPL TR 32-223)

Subroutines Required: None

Functions Required: SQRT

Approximate Deck

Length: 250 (decimal)

Formulation:

The potential function (Jeffrey's notation) for a vehicle of unit mass moving in the vicinity of an oblate Earth is

$$U = -\frac{\mathcal{U}}{r} \left\{ \frac{JR_e^2}{3r^2} \left(1 - 3\sin^2 L \right) + \frac{HR_e^3}{5r^3} \left(3 - 5\sin^2 L \right) \sin L + \frac{DR_e^4}{3i5r^4} \left(3 - 30\sin^2 L + 35\sin^4 L \right) + \dots \right\}$$

where

$$\vec{r} = r \hat{r}$$
 = position vector in the true equator of date frame
$$L = \text{geodetic latitude} = \sin^{-1}(\hat{r}_3) = \sin^{-1}(\frac{Z}{r})$$

and the force per unit mass may be evaluated by constructing the negative gradient of $\ensuremath{\mathsf{U}}$

$$F = -\nabla U = -\left(\frac{\partial U}{\partial X}, \frac{\partial U}{\partial Y}, \frac{\partial U}{\partial Z}\right)$$

However, the force vector (\vec{F}) would be expressed in the true equator of date frame rather than in the desired frame of 1950.0. Thus, before constructing the partials, it is noted that the radius rector in the two frames are related as follows:

$$\vec{r} = A_r \vec{R} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \vec{R}$$

$$R = r$$

and thus that

$$sin L = \frac{1}{R} \left(a_{31} R_1 + a_{32} R_2 + a_{33} R_3 \right)$$

With these substitutions established, the force vector (\vec{F}') expressed in the frame of 1950.0 is

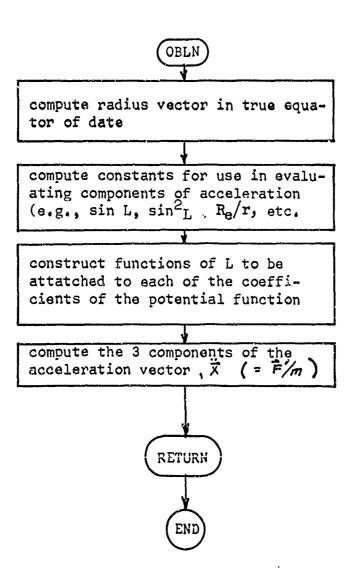
$$\vec{F}' = -\left(\frac{\partial U}{\partial R_1}, \frac{\partial U}{\partial R_2}, \frac{\partial U}{\partial R_3}\right)$$

Where

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$$-\frac{\partial U}{\partial u_{i}} = -\frac{\mathcal{I}_{\mathcal{U}}}{R^{4}} R_{e}^{2} \left\{ \left(1 - \frac{5z^{2}}{R^{2}} \right) \frac{U_{i}}{R} + 2 \frac{z}{R} a_{3i} \right\}
-\frac{H_{\mathcal{U}}}{R^{3}} R_{e}^{3} \left\{ \left(3 - 7 \frac{z^{2}}{R^{2}} \right) \frac{z}{R^{3}} U_{i} + \left(-\frac{3}{5} + 3 \frac{z^{2}}{R^{3}} \right) a_{3i} \right\}
-\frac{D_{\mathcal{U}}}{R^{6}} R_{e}^{4} \left\{ \left(\frac{3}{7} - 6 \frac{z^{2}}{R^{2}} + 9 \frac{z^{4}}{R^{4}} \right) \frac{U_{i}}{R} + \left(\frac{12}{7} - \frac{4z^{2}}{R^{2}} \right) \frac{z}{R} a_{3i} \right\}
U_{i} = R_{i} \text{ on } R_{2} \text{ ou } R_{3}$$

Computational Logic:



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                                                                                  THIS AGUTINE COMPUTES THE OBLATENESS ACCELETATION ACTING ON A SATELLITE MOVING IN THE FORCE FIELD OF A BODY DESCRIBED BY JEFFRIES POTENTIAL FUNCTION. IT CAN ALSO COMPUTE THE AVEC. = INSTANTANEOUS RADIUS VECTOR IN FRAME OF 1950.0
                                                                                                                                                                        CJ,CH,CD=CGEFFICIENTS OF THE SECOND,THIRD AND FUURTH HARMONICS ACCEL = PERTURBING ACCELERATION VECTOR IN FRAME OF 1950.0 AN = INPUT ARRAY TO CONVERT PERTJRBATION TO FRAME OF DATE
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                                                                                                                              = (.42857143-5.*ZR2+9.*ZR4)/R
                                                                                                                                         = (1.7142857-4.*ZR2)*ZR
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2.3.1.2.2 Subroutine DRAG

Purpose:

To evaluate the force acting on a satellite (in the mean

equator of 1950.0 frame) resulting from passage through

a rotating oblate atmosphere.

Deck Name:

DRAG

Calling Sequence:

Call DRAG (DF)

Input/Output:

T/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	OMEGA	w	1	CON (7)	Spin rate of the Earth
I	A	A	1	SAT (2)	Reference area
I	CD	c_D	1	SAT (3)	Drag coefficient
I	ROTATE	T-1	3 x 3	WRK (1)	Rotational matrices
	ROTINV	Т	3 x 3	WRK (10)	relating vectors in the true equator of date frame to 1950.0
T	R	r	3	WRK (44)	Radius vector (1950.0)
I	v	Ÿ	3	WRK (47)	Velocity vector (1950.0)
I	TW	t	1	WRK (50)	Day number relative to 1950.0 (used as in- put into atmospheric density routine)
0	קת	ה ה	3	Arg _.	Drag force (if A =scuare meters, density = Kg/m³, and velocity = Km/sec, then D = newtons)

Subroutines Required: ATMS (atmospheric density), CROSS (cross-product)

Functions Required: AMAG (vector magnitude)

Approximate Deck

Length: 146 (octal)

Formulation:

The drag force is computed in the frame of 1950.0 as follows $\widetilde{\omega}' = [T] \; \widetilde{\omega}$

where [T] = rotational transformation relating the true equator of date to the mean equator of 1950.0

 $\vec{\omega}$ = spin vector of the Earth in the true equator of date frame

 $\vec{\omega}'$ = spin vector in the frame of 1950.0

$$\vec{V}_{\omega} = \vec{\omega}' \times \vec{r}$$

$$\vec{\nabla}_r = \vec{\nabla} - \vec{\nabla}_{\omega}$$

where \vec{r} = radius vector (1950.0)

 \vec{V} = velocity vector (1950.0)

 \vec{v}_r = velocity relative to the wind (1950.0)

 \overline{V}_{ω} = velocity of the wind (1950.0)

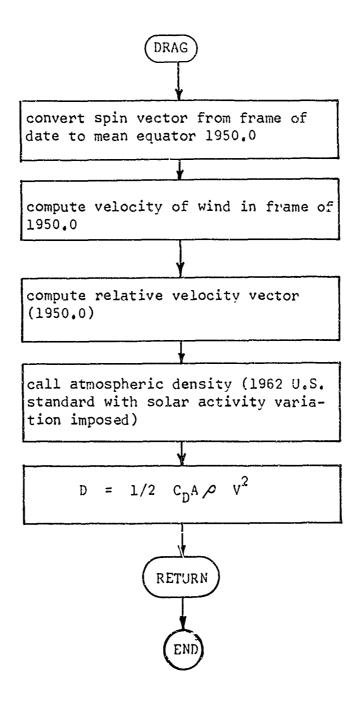
$$\vec{D} = -\frac{1}{2} \mathcal{P}(\vec{r}, T) C_0 A \vec{V}_r / \vec{V}_r /$$

where \vec{D} = drag force in newtons

 $\beta(\vec{r},T)$ = mass density of the atmosphere

C_nA = drag coefficient times reference area

Computational Logic:



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OF DATE FRAME	300
= POSITION VECTOR IN FRAME OF 1950	300
= VELOCITY VECTOR IN FRAME OF 1950.0	300
CGEFFICIENT OF DRAG	301
= CROSS SECTIONAL AREA OF	301
= ANGULAR VELOCITY OF CEN	301
= INVERSE OF MATRIX REL	301
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DIMENSION CON(1), SAT(1), SDA(1), MRK(1), STT(1)	301
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CGMMGN DATA	302
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, V(3) , RE(302
3) , VREL(3)	302
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EQUIVALENCE (CON(7), OMEGA), (SAT(303
), (WRK(50), TW), (WRK(1),	303
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SUBRGUTINE DRAG(DF)

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D3AG0480
                                      DRAG0380
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                                                                                                                                                                                                                               DRAG053C
 11/24/85
                                                                                                                           THE ATMOSPHERE WILL NOW BE CALLED AND THE DEVSITY COMPUTED IN KG/M**3 . DRAG VECTOR THEN DEFINED IN NEWTONS . CALL MATMPY( ROTATE,3,3,R,3,1,RE ) CALL MATMPY( RE,TW,DENS )
                 ı
               IFV(S)
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                                                                                                                                                                                                        = -CGNST * VREL(I) * VMAG * 1.E5
                                                                                                                                                                              CGNST = .5 * DENS * CD * Al
DG 3 I = 1,3
                                       = GMESA*RGTINV(2,3)
= GMESA*RGTINV(3,3)
                EFN
                                                                 CALL CRGSS(W,R ,VW)
DG 1 I=1,3
                                                                                         VREL(I) = V(I) - VW(I)
                   ı
                                                                                                      VMAS = AMAG(VREL)
  FS305
DRAGG
                                                                                                                                                                                                                  RETURN
                                                                                                                                                                                                        0F(1)
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2.3.1.2.2.1 Subroutine ATMS

Purpose:

ATMS computes an approximate atmospheric mass density (Kg/m³) at any altitude (h) between 100 and 700 Km.
(Below 100 Km the density is set equal to that of 100 Km and an error message is recorded; above 700 Km the density is set equal to zero). The U. S. Standard Atmosphere 1962, is used as a reference for a table (stored in memory within the Data Input Group) with 21 entries (10 Km steps 100 < h < 200, 50 Km steps 200 < h < 700). A dichotomic interpolation is then used in conjunction with the assumed exponential atmosphere (in the neighborhoods of the tabulated point) to produce an interpolated density (2 to 3 place accuracy throughout the table). These data are then corrected for the 11-year sunspot activity cycle.

Deck Name

ATMS

Calling Sequence:

CALL ATMS (RVEC, TJD, DENS)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	RVEC	ŕ	3	Arg	radius vector in the true equator of date frame
I	TJD	t	1	Arg	dummy variable (such as the Julian date) which can be used to compute corrections to ρ
0	DENS	P	1	Arg	atmospheric mass density (Kg/m ³)
I	ALT 1 ALT 2 ALT 3	h ₁ h ₂ h ₃	1 1 1	ATCON (1) ATCON (2) ATCON (3)	Altitude limits for density data

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	REQT RPOL	$egin{array}{c} \mathbf{r_e} \\ \mathbf{r_p} \end{array}$	1	ATCON (4) ATCON (5)	equatorial and polar radii for the Earth
I	STEP 1 STEP 2	Δh, Δh ₂	1 1	ATCON (6) ATCON (7)	altitude increment for density and lapse rate tables
I	RHOF RATE	рі Кі	21 21	TABLE (1) TABLE (22)	density and lapse rate at altitudes between hl and h3

Subroutines Required: None

Functions Required: SQRT

EXP SIN ALOG AMAG

Deck Length:

00524 (octal)

Formulation:

Atmospheric density will be approximated utilizing data taken from the 1962 U. S. Standard Atmosphere and assumed exponential behavior with a single parameter, altitude. Thus, the first task is to compute the radial distance from the center of the Earth to the subsatellite point (the intersection of the radius vector to the satellite with the Earth's surface) which will be defined to be r. This task, in turn, will be accomplished by employing the oblate spheroid representation of the Earth.

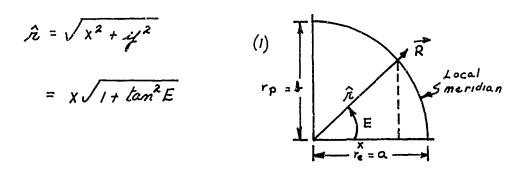
Let R be the satellite position vector and c be the projection in the plane of the true equator of date

$$r^2 = r_1^2 + r_2^2 + r_3^2$$
 $c^2 = r_1^2 + r_2^2$

If c = 0, the satellite is directly above either the North or South Pole, and

$$\hat{\mathbf{r}} = \mathbf{r}_{p}$$

where $r_p = polar$ Earth radius and $\hat{r} = local$ Earth radius. However, if $c \neq 0$,



where $\tan E = \frac{n_3}{C}$

Then from the equation for an ellipse,

$$\frac{\chi^{2}}{a^{2}} + \frac{4}{4} \frac{z^{2}}{z^{2}} = 1$$

$$\frac{L^{2}}{a^{2}} + \tan^{2} E = \frac{L^{2}}{\chi^{2}}$$

or
$$X = \frac{k}{\sqrt{\frac{k^2}{a^2} + \tan^2 E}}$$

Substituting into (1)
$$\hat{R} = \frac{b\sqrt{1 + \tan^2 E}}{\sqrt{\frac{b^2}{a^2} + \tan^2 E}}$$

and the height above the Earth is

$$h = r - \hat{r}$$

Now the atmosphere is assumed to be constructed in uniform concentric shells around the (oblate spheroid) Earth with densities which agree with those predicted by the 1962 U. S. Standard Model. For simplicity, a two part table of these data has been prepared. Part one covers altitudes from 100 Km to 200 Km in 10 Km steps while part 2 covers from 200 Km to 700 Km altitude in 50 Km steps (there are, therefore, 21 entries in the table). Since this region contains all altitudes for which the tenuous atmosphere should be considered in studies of satellite motion, the table was not extended. Rather, below 100 Km the density is set equal to the value at 100 Km, and above 700 Km the density is set equal to zero.

For any altitude, h, between 100 Km and 700 Km the values in the table corresponding to the nearest altitude above and below h, must be determined and interpolated to find the density at h. Let m be the index corresponding to the nearest tabulated altitude below h, then,

- (1) between 100 and 200 Km, $m = \text{greatest integer} \left(\frac{\hat{H} 100}{10} \right) + 1$
- (2) between 200 and 700 Km, m = greatest integer $\left(\frac{h-200}{50}\right)$ + 11

Let Δ h be the distance between h and the nearest tabulated altitude below h,

(1) if 100 Km
$$\stackrel{?}{=}$$
 h $\stackrel{\checkmark}{=}$ 200 Km

$$X = \text{greatest integer in } \frac{4-10}{10}$$

 $\Delta h = (h-100) - X (10)$

(2) if
$$200 \text{ Km} \le h \le 700 \text{ Km}$$

$$X = \text{greatest integer in} \left(\frac{f_{-200}}{50}\right)$$

 $\Delta h = (h-200) - X (50)$

The tabular values of density above and below h can now be extrapolated to predict two values of the density at h; then, an interpolation can be made between the two predicted values of density to include the non-exponential nature of the atmosphere.

Let $\Delta \widetilde{h}$ be the distance between h and the nearest tabulated altitude above h, then

$$\Delta \tilde{h} = \Delta h - 10$$
 if $100 \le h \le 200$
 $\Delta \tilde{h} = \Delta h - 50$ if $200 \le h \le 700$

and let ρ_1 = extrapolation of lower value (index m) and ρ_2 = extrapolation of upper value (index m + 1)

$$P_{l} = \widetilde{p}_{m} e^{-nm \Delta \hat{h}}$$

$$P_{2} = \widetilde{p}_{m+l} e^{-(nm+l)\Delta \hat{h}}$$

where

$$\widetilde{\mathcal{P}}$$
 = tabulated value of density

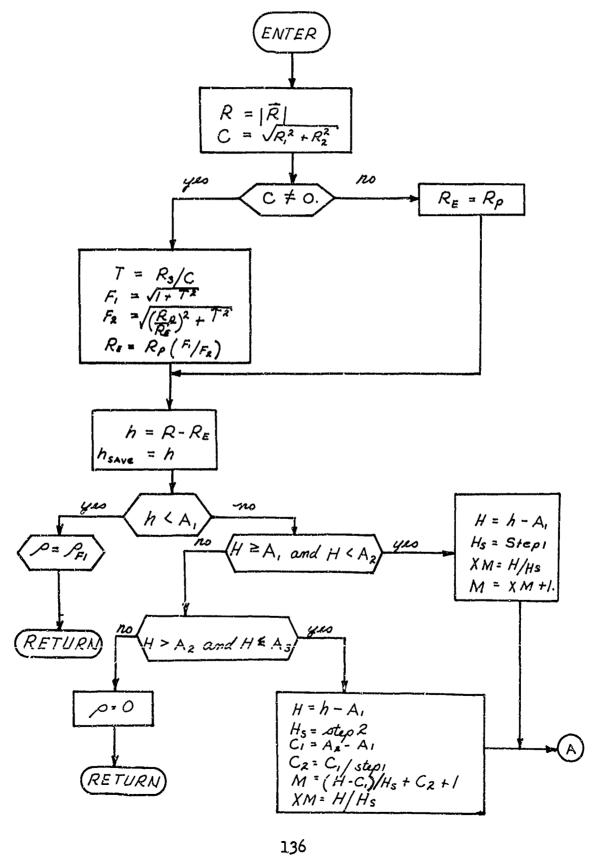
$$r = \text{tabulated slope (lapse rate)} = \frac{d\rho}{dh}$$

Finally, by linear interpolation between

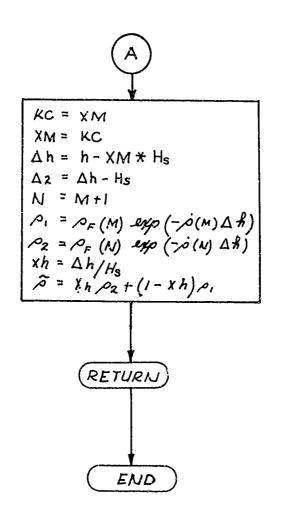
$$p = y p_2 + (1-y) p_1$$

$$y = \Delta h /_{10} or \Delta h /_{50}$$

Computational Logic:



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SOURCE STATEMENT

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ATMOS

H / HSTEP

XM + 11.

X* = H M = XM GO TO 100

- ALTI

H - Ai. STEP1

11

HSTEP

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ATMS0530
                                                                                                                                                                                                                                     ATMSO600
                                                                                                                                                                                                                                               ATMS9610
                                    ATMS0390
                                             ATMS04nn
                                                       ATMS0410
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                            ATWS0380
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                                                                                           ATMS0450
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12/13/85
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GO TO 104 HSTEP CONS CONI ۶ × 7 ں

ALT2 - 4LT1

CON1

H - ALTI

STEP2

(H - CON1) / STEP2 + CON2 + 1.

= H / HSTEP

DENS = 0.000**၁**

100

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= DELTAH - HSTEP = H - XM*HSTEP W + 1 DELTAH **DELTA2**

RHOF(M) * EXP(-RATE(M)*DELTAH) RHOF(N) * EXP(-RATE(N)*DELTA2) DELTAH / HSTEP RH02 R.H01 ×

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ATMS0780

XH*RHO2 + (1. - XH)*RHO1 DENS

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2.3.1.2.3 Subroutine ENCKE

Purpose:

ENCKE provides the correction to the acceleration vector

resulting from motion on the true (rather than the

reference) trajectory

Deck Name:

ENCK

Calling Sequence:

CALL ENCKE (ACCEL, IRECT)

Input/Output:

, I/o	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	GM	м	1	CON (6)	Gravitational constant for the central body
I	RCONIC ·	Þ	3	WRK (117)	Position vector on the conic reference trajectory
I	DELTA	Δ̈́T	3	WRK (52)	Displacement relative to conic position (ムアョティラ)
0	ACCEL	ΔΫ	3	Arg	Differential accelera- tion vector
0	IRECT	-	1	Arg	Signal for MOTION to alter the reference tra- jectory

Subroutine Required: None

Functions Required:

DOT (dot product)

SQRT (square root)

Approximate Deck

Length:

213 (octal)

Formulation:

Encke's method of integration involves the computation of the acceleration vector relative to a known reference which in the present case is an ellipse. Thus in addition to real perturbing forces there are terms which must be included for the off-nominal nature of the motion. Consider

$$\ddot{\vec{r}} = -\underline{u}\vec{r} + \vec{F} \tag{1}$$

$$\overset{::}{\rho} = \mathcal{M} \underbrace{\overset{::}{\rho}}_{\rho s} \tag{2}$$

where

 \vec{r} = radius vector (in some frame) for true trajectory

 \vec{F} = summation of all non-central forces

p = radius vector (at the time corresponding to the instantaneous position on the true trajectory) on the conic reference

defining

$$\Delta \vec{r} = \vec{r} - \vec{o} \tag{3}$$

The differential equations for $\Delta \vec{r}$ can be obtained

$$\Delta \ddot{\vec{r}} = F + \mathcal{L} \left[\frac{\vec{\rho}}{\rho^3} - \frac{\vec{r}}{r^3} \right]$$

But since $|\Delta \vec{r}|$ may be small, the term in the brackets may be known to less accuracy than \vec{r} or $\vec{\rho}$ due to the fact that two nearly equal numbers are differenced. Thus, a modification to maintain accuracy for such cases will be presented.

$$\Delta \vec{r} = \vec{F} + \mathcal{A} \left[\vec{\rho} - \rho^{3} \vec{r} \right]$$

$$= \vec{F} + \mathcal{A} \left[\vec{\rho} - (1 - fg) \vec{r} \right] \qquad fg < (4)$$

$$= \vec{F} + \mathcal{A} \left[-\Delta \vec{r} + fg \vec{r} \right]$$

Now f_q has one more degree of freedom than does the ratio $(f_r)^3$ so the following identity can be written arbitrarily

$$(1-f_q) = (1+2q)^{-3/2} = (^{\circ}/r)^3$$
 (5)

or

$$fg = 1 - (1 + 2g)^{-\frac{3}{2}}$$

$$= 3g - \frac{3 \cdot 5}{2}g^{2} + \frac{3 \cdot 5 \cdot 7}{2 \cdot 3}g^{3} - \frac{3 \cdot 5 \cdot 7 \cdot 9}{2 \cdot 3 \cdot 4}g^{4}$$

$$+ \tag{6b}$$

where

$$\frac{r^{2}}{\rho^{2}} = 1 + 2g$$

$$g = \frac{r^{2} - \rho^{2}}{2\rho^{2}}$$

$$= \frac{1}{2\rho^{2}} \left\{ (\vec{\rho} + \vec{\Delta r}) \cdot (\vec{\rho} + \vec{\Delta r}) - \vec{\rho} \cdot \vec{\rho} \right\}$$

$$= \frac{\vec{\rho} \cdot \vec{\Delta r} + 2\vec{\Delta r} \cdot \vec{\Delta r}}{\vec{\rho} \cdot \vec{\rho}}$$
(7)

Equation 6b, when truncated at any given term, defines the accuracy to be obtained from equation 4 for the case where $/\vec{r}/\approx /\vec{\rho}/$. Thus, if a fixed number of terms are consistently carried, the maximum value that q can attain before the reference trajectory is altered (rectified) (or before the equation for evaluating fq is changed from equation 6b to 6a) is defined by the maximum error allowable in the scalar fq. For example, if this allowable error is arbitrarily set at 10^{-8} , and if seven terms in fq are carried, the upper limit in q is defined by

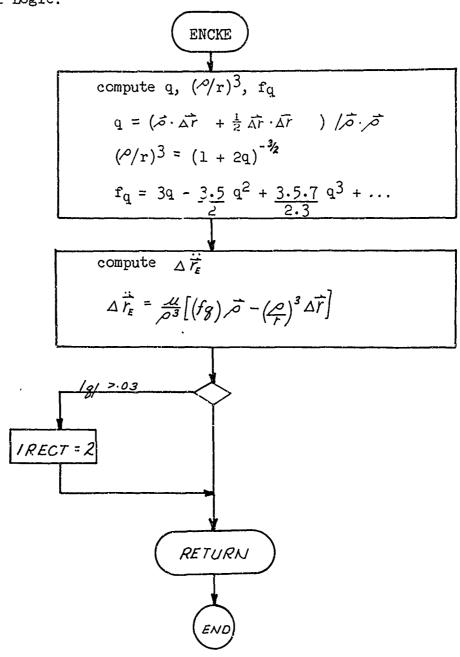
$$\frac{3.5.7.9.11.13.15}{2.3.4.5.6.7} \quad q_{\text{max}} < 10^{-8}$$

$$q_{\text{max}} \approx 2.5 \times 10^{-11}$$

which corresponds roughly to

$$q_{max} = .03$$

Computational Logic:



SOURCE STATEMENT - IFN(S)

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SUBRGUTINE ENCKE (ACCEL, IRECT)	ENCKE020
CELERATION VECTOR EX	ENCKE04
VEHICLE DUE 10 MGTION ON A TRAJECTORY OTHER THAN THE	ENCKE050
SIGNIFICANCE IN THE F	ENCKE07
A RECTIFICATION SISVA	ENCKEO
EXCESSIVE. THIS STER	ENCKEO
HE EFFECT OF SERIES I	ENCKEL
3 ELIMINATE NEED FOR	ENCKE1
	TACKE!
KCGNIC = POSILIGN VECTOR ON KEPEKENCE - KAJECIGKY (1950-0) DELIA = DISOLACEMENT VECTOR DELATIVE IA DEE, TDA (1950-0)	
****************	_
DIMENSION CON(1), SAT(1), SDA(1), WRK(1), STT(1)	_
	_
COMMON DATA	\sim 1
	\sim 1
1), CGN), (DATA(15), SAT	AI.
, (DATA(3	\sim 1
	\sim 1
	C.I
DIMENSION RCONIC(3) , DELTA(3) , ACCEL(3)	A.
	$\sim 10^{\circ}$
EQUIVALENCE (CON DIJOR IN (ACC) DELIA I	NI O
77144416	NI P
*************	ENCKE300 ENCKE310
	∼
R2 = DGT(RCGNIC, RCGNIC)	NCKE330
Q = (DGT(RCGNIC,DELFA)+.5*DGT(DELTA,DELFA))/32	NCKE3
)**3	CKE350
FQ=Q=Q=(3-+1*(-7-5+Q*(17-5+Q*(-39-375+Q*(86-525+1*(-187-6875+Q*	NCKE3
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FS305 ENCK

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IFV(S)

SOURCE STATEMENT

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FNCK

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R3 = R2 *SQRI(R2) G0F = GM*F /R3 G3FQ = GM*FQ/R3

DG 1 I=1,3 ACCEL(I) =

EVCKE380 ENCKE390

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ENCKE400 ENCKE410 ENCKE420

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ENCKE430 ENCKE440 *ENCKE450

ENCKE460 ENCKE470

ENCKE480

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SID 65-1203-1

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DECK LENGTH IN OCTAL IS

FS305 ENCK

2.3.1.2.4 Subroutine PRESS

Purpose:

To compute the force exerted on a spherical satellite

due to the pressure of the impinging light

Deck Name:

PRES

Calling Sequence:

Call PRESS (SFOR)

Input/Output:

I/O,	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
0	SFOR	∓ F _s	3	Arg	Solar pressure force vector in the frame of 1950.0
I	RVEC	r	3	WRK (44)	radius vector in the frame of 1950.0
I	RSUN	r _s	3	WRK (98)	Position vector for the sun relative to the earth (1950.0)
I	A	A	1	SAT (2)	Cross sectional area of spherical satellite
I	R	R	1	SAT (4)	Surface reflectivity
I	RE	R _e	1	CON (1)	Equatorial radius of the earth

Subroutines Required: None

Functions Required:

AMAG

(vector magnitude)

DOT

(Dot product)

SPOWER

(solar power)

SQRT

(square root)

Approximate Deck

Length:

220 (octal)

Formulation:

The solar force exerted on a spherical satellite resulting from impinging light can be obtained directly from the expression relating the solar pressure, i.e.,

$$P = \frac{P}{C}$$
 (1+R) $\cos^2 \alpha$

where

P is the power of the incident radiation

C is the speed of light

R is the surface reflectivity

w is the angle between the surface normal and the impinging light.

This is accomplished by integrating the pressure over the surface and (due to symmetry) applying the result in the direction of the impinging light.

$$F_s = \frac{P}{C} (1+R) \int_A \cos^2 \alpha dA$$

But for the spherical satellite

$$dA = 2\pi S^2 \sin \alpha d\alpha$$

where

S = radius of the satellite

 angle between an arbitrary radius vector to the satellite skin from its center and the vector defining the direction of the impinging light.

and the integration over the surface reduces to the integration with respect to \propto from 0 to $\pi/2$. The result is

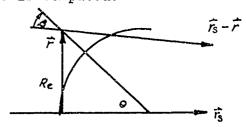
$$F_{S} = \frac{P}{C} \quad (1+R) \frac{2}{3} \pi \quad S^{2}$$

$$\vec{F}_{S} = -F_{S} (\vec{r}_{S} - \vec{r}) / |\vec{r}_{S} - \vec{r}|$$

This description of the problem is not, however, complete since it fails to consider the effects of any time which might be spent in the earth's shadow. This correction might be made by zeroing P for these times but for reasons of data availability in PRESS and not in SPOWER (which computes P/C) the following approach will be followed to determine if the sun is visible before the force is computed.

First, the angle between the relative sun and the radius vector is

$$\beta = \cos^{-1} \left[\frac{-\vec{r} \cdot (\vec{r} - \hat{r})}{r | \vec{r} - \vec{r}|} \right]$$



Then, the angle defining the limits of the cylindrical shadow can be defined as

$$\theta = \sin^{-1}\left(\frac{R_e}{r}\right)$$

and the requirement for visibility is

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There are, of course, several assumptions which have been made which, though not completely apparent, should be noted since they introduce slight errors

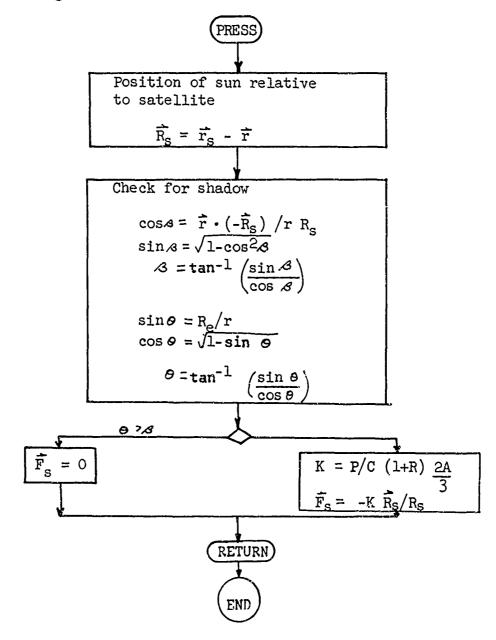
- 1) The sun is assumed to be a point
- 2) The earth is assumed spherical for the purposes of defining the shadow

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3) The shadow is assured cylindrical

These assumptions are believed to be reasonable for most applications and should introduce negligible errors due to the small effect of $F_{\rm S}$ on most trajectories.

Computational Logic:



Then, the angle defining the limits of the cylindrical shadow can be defined as

$$\theta = \sin^{-1}\left(\frac{R_e}{r}\right)$$

and the requirement for visibility is

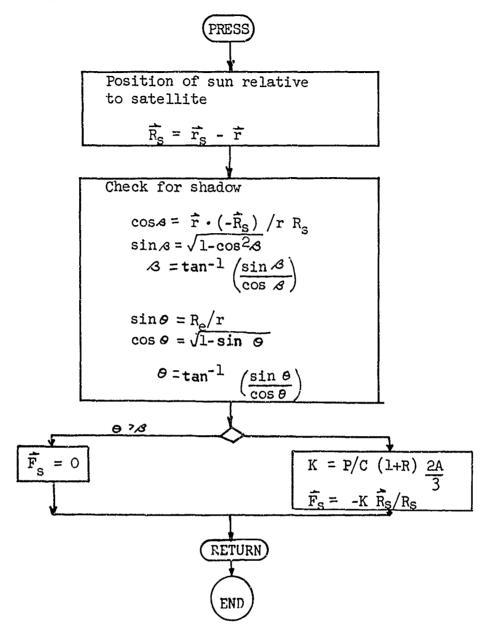
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There are, of course, several assumptions which have been made which, though not completely apparent, should be noted since they introduce slight errors

- 1) The sun is assumed to be a point
- 2) The earth is assumed spherical for the purposes of defining the shadow
- 3) The shadow is assumed cylindrical

These assumptions are believed to be reasonable for most applications and should introduce negligible errors due to the small effect of $F_{\rm S}$ on most trajectories.

Computational Logic:



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2.3.1.2.4.1 Function SPOWER

Purpose:

. ROWER computes the ratios of the solar power to the used of light in mks units. This routine was intended to allow for motion about bodies other than the earth

Deck Name:

3POWER

Calling Sequence: SPOWER (RS)

Input/Output:

, I/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
Ι	RS	r̄s-r̄	3	Arg	Position of sun relative to the satellite
0	SPOWER	P/C	1	-	Ratio of solar power to the speed of light

Subroutine Required:

None

Functions Required:

None

Approximate Deck

Length:

50 (octal)

IFN(S)

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SBURCE STATEMENT

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SPUWR

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P = POWER OF INCIDENT LIGHT WAVE

SPEED OF LIGHT

NEWTONS / SQUARE METER

FUNCTION SPOWER(RS)

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RETURN

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END

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SPRBG3CG

SID 65-1203-1 -159-

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DIMENSION CON(1), SAT(1), SDA(1), WRK(1), STT(1) Ą

EQUIVALENCE

COMMON DATA

, (DATA(286), STTI; (DATA(391), WRK)

DIMENSION RS(3)

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2.3.1.2.5 Subroutine PERT

Purpose:

PERT is a special purpose routine which computes the gravitational accelerations (perturbative) of the sur and moon on a geocentric satellite. The assumption is made in the development that the geocentric radial distance is small compared to the distance to the disturbing mass: thus a more exact formulation is required for the general case.

Deck Name:

PFRT

Calling Sequence:

Call PERT (ACCEL)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	R	r	3	WRK (44)	radius vector in the frame of 1950.0
1	RS RM	r r	3	WRK (101)	radius vector of the sur (moon) in the frame of 1950.0 rela- tive to the Earth
T	IIM US	M _m M _s	1 1	COM (8)	gravitational constant for the moon and sun
0	ACCEL	Ơ	3	Arg	perturbative accelera- tion vector due to gravitational accel- eration of the sun and moon

Subroutines Required:

Morie

Functions Required:

AMAG (vector magnitude), FQ (Encke series function)

Approximate Deck

Length:

170 (octal)

Formulation:

The acceleration experienced by a body (traveling about the Earth, for example) resulting from masses other than the central body (i.e., the sun, and moon) is the summation of terms of the following form.

$$\ddot{\vec{r}}' = -\mathcal{L}\left[\frac{\dot{r} - \dot{R}}{|\dot{r} - \dot{R}|^3} - \frac{\dot{R}}{R^3}\right]$$

This equation, while correct, exhibits a very undesirable nature for $\mathcal{A} << \mathcal{R}$ since for these cases the term in the brackets is the difference of two nearly equal quantities. Therefore, since this limiting case is the case of primary interest, an alternate form is necessary if these terms in the acceleration are to be included. One such modification is based on the similarity of this perturbation equation and that for the Encke acceleration.

consider:

$$\vec{r}' = -\mu \left[-\frac{\vec{\rho}}{\rho^3} + \frac{\vec{R}}{R^3} \right] \qquad \rho \cdot \vec{R} - \vec{r}$$

$$= -\mu \left[-\frac{\vec{R}}{R^3} - \vec{\rho} \left(\frac{R}{\rho} \right)^3 \right]$$

$$= -\mu \left[-\frac{\vec{R}}{R^3} - (1 - fg) \vec{\rho} \right]$$

$$= -\mu \left[-\frac{\vec{R}}{R^3} - (1 - fg) \vec{\rho} \right]$$

$$= -\mu \left[-\frac{\vec{R}}{R^3} - (1 - fg) \vec{\rho} \right]$$

where as before, since fg has one more degree of freedom than the ratio R/p, g can be defined as follows

or

$$fg = 1 - (1 + 2g)^{-3/2}$$

$$= 3g - \frac{3.5}{2}g^{2} + \frac{3.5.7}{2.3}g^{3} - \frac{3.5.7.9}{2.3.4}g^{4} + \cdots$$

also

$$Q = \frac{2^{2}}{R^{2}} - 1 = \frac{1}{2R^{2}} \left(2^{2} - R^{2} \right)$$
$$= -\frac{1}{2R^{2}} \left(R^{2} - 2^{2} \right)$$

but

$$\vec{>} = \vec{R} - \vec{r}$$
$$= (\vec{x} - \vec{x}) \hat{x} - \cdots$$

therefore

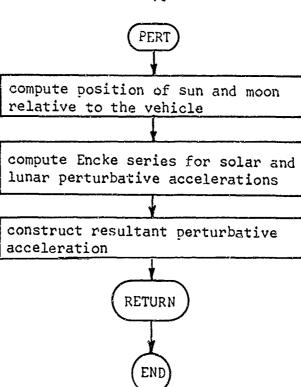
$$g = -\frac{1}{2R^{2}} \left(\bar{x}^{2} + \bar{y}^{2} + Z^{2} - (\bar{x} - x)^{2} - (\bar{y} - y)^{2} - (\bar{z} - Z)^{2} \right)$$

$$= -\frac{1}{2R^{2}} \left(2(\bar{x}x + \bar{y}y + Zz) - (x^{2} + y^{2} + z^{2}) \right)$$

$$= -\frac{1}{R^{2}} \left(\vec{R} \cdot \vec{r} - \vec{r} \cdot \vec{r} \right)$$

$$= -\frac{\vec{R} \cdot \vec{r} + (\vec{r} \cdot \vec{r})^{2}}{R^{2}}$$

Computational Logic:



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IFN(S)

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SOURCE STATEMENT

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PERTA

FS305

SUBROUTINE PERT (ACCEL)

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            ROUTINE COMPUTES THE PURTURBATIVE ACCELERATIONS EXPERIENCED BY A SATELLITE DUE TO THE SUN AND MOON. THIS ACCELERATION IS COMPUTED UTILIZING THE ENCKE SERIES RATHER THAN BY UTILIZING THE DIFFERENCES IN NEARLY EQUAL
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PAGE 193		LGCATION	1
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2.3.1.2.5.1 Function FQ

Purpose:

to evaluate the Encke series utilized in constructing solar and lunar gravitational accelerations of close geocentric

satellites.

Deck Name:

FQ

Calling Sequence:

FQ (RN, R)

Input/Output;

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	RN	ъ }	3	Arg	radius vector for the sun (or moon) in the frame of 1950.0
I	R	F	3	Arg	radius vector for the vehicle in the frame of 1950.0
0	FQ	<i>f</i> 3	1	مد	numerical value of Encke series

Subroutines Required: None

Functions Required: None

Approximate Deck

120 (octal) Length:

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                                              FQ**0C20
                                                                     FQ**CC4C
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                                                                                                                                              F3**C1CS
                                                                                                                                                           FQ**0110
                                                                                                                                                                      F0**0120
                                                                                                                                                                                 Q = ( DCI(RN,R ) +.5*DUI(R,R))/ DOI(RN,RN)
FQ= Q*(3.+Q*(-7.5+Q*(17.5 +Q*(-39.375+Q*(96.625+Q*(-187.6875))))))FQ**C14C
                                                                                                                                                                                                          F0**15C
                                                                                                                                                                                                                      FQ**0160
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170			SYMBOL F.DOCC		FQ		DGT		EFN	DECK LENG

2.3.1.2.6 Subroutine EPHEM

Purpose: EPHEM is designed to compute approximate position

vectors for the sur and moon from two-body equations of motion and tabulated position and velocity inform-

ation obtained from the Data Input Group.

Dеск Name:

EPHEM

Calling Sequence:

Call EPHEM

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I.	TW	t	1	WRY (50)	The whole and functional part of a mean solar
	न पृ]	WRK (51)	day defining the desired epoch for \vec{r}_{α} and \vec{r}_{D}
0	RS	rs	3	WRK (98)	Solar and lurar posi- tion vectors in the
	RM	$\mathbf{\hat{r}}_{\mathrm{m}}$	3	WRK (101)	coordinate frame of
I	GME GMM	jii.] 1	CON (6)	gravitational constants for the Earth, the
	GMS	M Mm Ms	1	CON (9)	moon and the sun (in $\frac{1}{5}$ /sec ²)
Т	FPHAM	\vec{r}_i , \vec{v}_i	339	ЕРНОМ	Tabulated position and velocity vectors for the sun and moon for the time period 1965 - 1975
I	FPHM .	\hat{r}_{i}, \hat{v}_{i}	271	EPHAM (L)	Subarray containing the lunar data
I	FPHS	\vec{r}_i, \vec{v}_i	66	EPHAM (274)	Subarray containing the solar data

Subroutines Required: CONIC (conic section routine)

Functions Required: None

Approximate Deck

Length: 456 (octal)

Formulation:

The equations of two-body motion (i.e., the Earth-sun and the Earth-moon systems) relative to the center of mass are

$$\frac{\ddot{r}}{r_i} = -G m_2 \left(\frac{m_2}{m_i + m_2}\right)^2 \frac{\vec{r_i}}{r_i^3}$$

$$\frac{\ddot{r}_{2}}{\ddot{r}_{2}} = -Gm_{1}\left(\frac{-m_{1}}{m_{1}+m_{2}}\right)^{2}\frac{\vec{r}_{2}}{r_{2}^{3}}$$

which are immediately recognizable as the equations of conic motion. This fact will be utilized in the following paragraphs to approximate the true ephemeris of the moon and sun relative to the Earth.

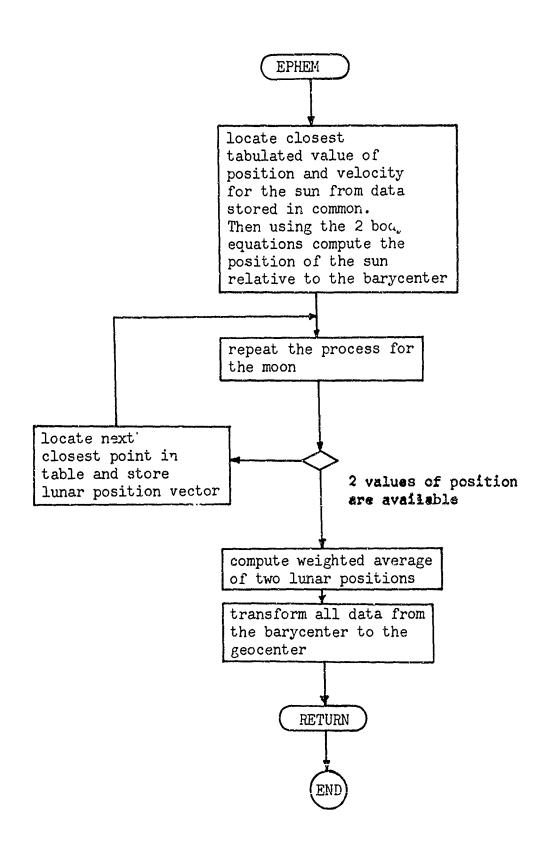
Consider a table of values for \vec{k} and \vec{V}_0 at regular intervals of approximately 1 year from which the conic describing the motion of the sun (relative to barycenter) can be computed. The problem is simply to locate the closest tabulated point (no more than about 6 months), define the time over which the body has moved, and compute \vec{r} and \vec{v} utilizing the conic section routine developed for the reference trajectory. Since this conic is altered but a very little by planetary perturbations, the result is of moderate precision.

Now consider the problem of the moon's motion when the sun produces a significant perturbation. First, it is obvious that the time interval between values of \vec{r}_o and \vec{v}_o must be reduced so that the effect of the perturbations can be kept small (for the present case $\Delta t = 3$ months). Second, it is apparent that the results obtained with the technique would be more accurate if they could include some of the effects predicted if the next-to-closest point in the table were utilized for extrapolation purposes. This correction was included by weighting two separate computations of the position vector (in a manner which resulted in even weighting for a date midway from either point in the table and a weight of 1 for the term designed to include the effects of the closest point if the time was equal to a tabular time) and averaging the results.

The final step in both cases was to translate the origin from the bary-center to the geocenter.

Results prepared by this routine have been checked against a true ephemeris to compute the errors inherent in the process. This analysis showed that the solar position data were completely satisfactory (from the standpoint of accuracy) for the computation of both the solar radiation force and the

solar gravitational acceleration in that the noise in the data would normally produce errors in the total perturbating acceleration (from MOTION) which were beyond the 8-digit limitations of the machine. The same is not quite true (for near-Earth satellites) of the lunar ephemeris even though the correction cycle is employed. However, it is noted, in defense of its use, that the second integral of the total resultant differential acceleration ($\Delta \hat{r}$) is in itself a correction to the conic position vector (\hat{r}_c). Therefore, the noise which is not lost when summing the perturbative terms in MOTION is generally lost when adding $\Delta \hat{r}$ to \hat{r}_c .



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) ,EPHS(K6) ,VS(3) ,RM1(2)	HM0240
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2.3.1.3 THE INTEGRATION GROUP

The differential acceleration vector (relative to the central force acceleration describing the reference ellipse) is integrated to define both the differential position and velocity vectors with a Gauss-Jackson backwards difference formulation. This solution is accomplished by mechanizing several separate routines.

INGRAT	The driver routine
HSIZE	Dynamically varies the step size for the integration to maximize accuracy and efficiency
START	A fourth order Runge-Kutta integration routine utilized to establish the required difference table.
DIFTAB	Evaluates the leading diagonal in the sum- difference tables
INTEG	Gauss-Jackson backwards difference uncorrected integration

The various portions of this group are in themselves general purpose routines. However, the group as a whole has been designed as a special purpose routine for the differential corrections program. This design philosophy can be understood when the requirements for the routines operation, the nature of the acceleration being integrated, and the requirements for communication between the calling program and INGRAT are analyzed. This approach also affords the maximum efficiency from this integration concept by eliminating checks for alternate stops, etc.

Subroutine INGRAT

Purpose:

INGRAT serves as the driver for the integration of the equations of motion employed in this program and is intended to function in the mode of a Gauss-Jackson integration. Complete logic is included for starting the integration and/or varying the step size and restarting the process.

Deck Name:

INGRT

Calling Sequence:

Call INGRAT (ISTART)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
1/0	ISTART	Cas	1	ARG	A fixed point index utilized to define the mode of operation for INGRAT. ISTART = 1 for Runge-Kutta starter; = 2 for Gamss-Jackson continuation
I	CONVI	<u>sec</u> day	1	CON (11)	Conversion from mean solar days to seconds
I	RCO	\vec{r}_{c}	3	WRK (28)	Position and velocity vectors for the conic
	VCO	Ϋc	3	WRK (31)	reference trajectory at the time of the most recent rectification (Km,Km/sec) in the frame of 1950.0
1/0	RVEC	ŕ	3	MBK (TT)	The position and velocity vectors in the mean
	VVEC	<u> </u>	3	WRK (47)	equator of date frame of 1950.0 (Km, Km/sec)
1/0	TW	t	1	WRK (50)	The whole and fractional number of days elapsed
	TF		. 1	WRK (51)	since the reference date 1950.0 (JD 2433282.423) for the present epoch

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I I/O I/O	RDD RD R	Ɣ Ɣ Ɣ	3 3 3	WRK (58) WRK (55) WRK (52)	The acceleration, velocity, and position vectors defining the true motion relative to the reference ellipse in the frame of 1950.0 (Km/sec ² , Km/sec, Km)
I	TSTOPW TSTOPF	^t stop	1	WRK (61) WRK (62)	The whole and fractional number of days since 1950.0 for the data
1/0	н	h	1	WRK (68)	The step size in sec- onds for the numerical integration
I	RS RM	rs rm	3	WRK (98) WRK (101)	The position vectors for the sun and moon in the form of 1950.0 (Km)
1/0	TIME	t-t _c	1	WRK (104)	The time interval in seconds since the reference trajectory was last rectified

Subroutines Required: CONIC (conic reference trajectory)

START (Runge-Kutta starter)
DIFTAB (difference table)

INTEG (Gauss-Jackson integration)

HSIZE (step size control)

Functions Required: AMAG (vector magnitude)

Approximate Deck

Length: 501 (octal)

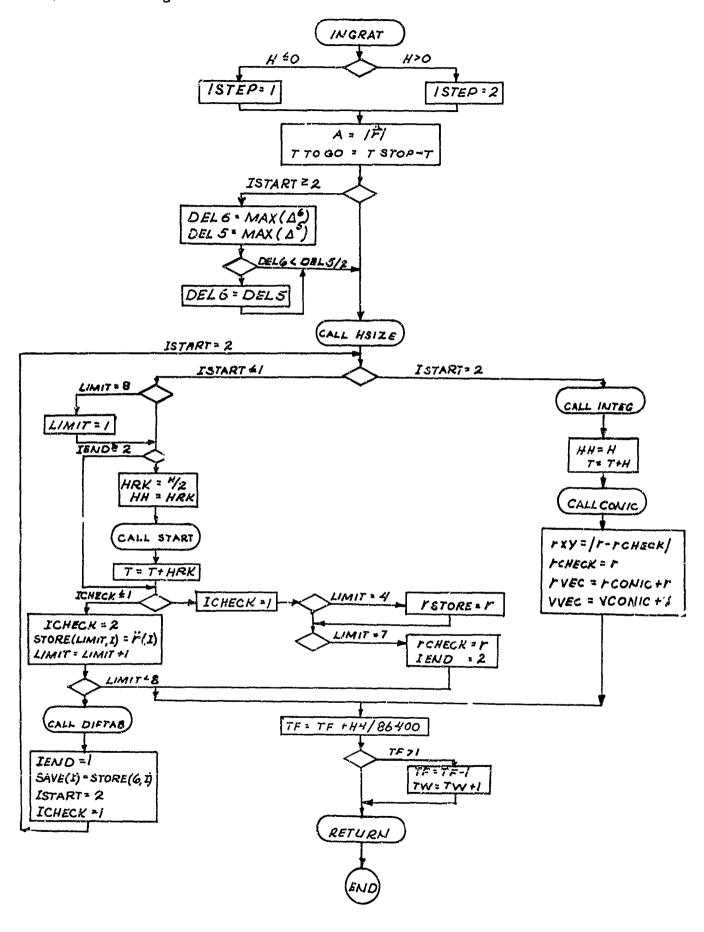
Discussion:

INGRAT is a special-purpose driver routine for a step-by-step numerical integration of the equations of motion as developed for this program. This integration is accomplished by mechanizing a step size check routine and either a fourth-order Runge-Kutta starter or a Gauss-Jackson (double-sum) backwards difference (through sixth difference) continuation routine.

INGRAT accomplishes its objective by continuously monitoring the time interval from the present epoch to the time at which data will be available and defining the information required during the checks performed within HSIZE to assure that an optimum step size can be utilized to arrive at the target epoch exactly in the fewest number of Gauss-Jackson steps possible. In addition, INGRAT serves as the means by which data generated in START (the fourth order Runge-Lutta starter) are stored and differenced to set up the solution by the Gauss-Jackson routine.

Several steps are taken to assure that the solution proceeds in an accurate and efficient manner. However, no corrector cycle has been employed either in the starting process or in the continuation process. This step is felt justifiable since:

- 1. The equations being integrated represent the displacement from and velocity relative to the reference ellipse (Thus, even moderate errors will not generally be realized when the true position and velocity vectors are computed by adding the results of the integration to the conic position and velocity.).
- 2. The Gauss-Jackson formulation has demonstrated superior performance capabilities when compared to the Runge-Kutta formulation in the integration of X = -KX for similar step sizes without employing the corrector. (For this reason, the Runge-Kutta method [which is employed to start the Gauss-Jackson integration] will utilize a step which is one-half of that to be employed in the Gauss-Jackson method.)
- 3. The step size itself will be controlled in such a manner that the predictor formula alone will provide the required accuracy by monitoring the contribution of the last term carried in the integration series to the integral (this procedure will cause the step size for this routine to be less than that for a predictor-corrector formulation; however, sample calculations have shown that the slight improvement in accuracy [about one digit] and step size [a factor of about 2]) does not justify this procedure for this application.



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2.3.1.3.1 Subroutine HSIZE

Purpose:

HSIZE is a step-size, control routine designed to operate in conjunction with the Gauss-Jackson integration package. In its simplest form, HSIZE determines whether the stepsize (h) should be halved or whether it can be doubled without loss of accuracy or chance of producing a loop.

Deck Name:

SIZE

Calling Sequence:

HSIZE (TTOGO, DEL6, ACCEL, RXX, ISTART, L, IH, H)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	TTOGO	ŧ go	1	ARG	the time interval (sec) between the present epoch and the epoch of the next piece of observed data.
I	DEL6	Δ.	1	ARG	the magnitude of the largest component of the vector composed of the sixth differences in the acceleration ($\Delta \vec{r}$ = Km/sec ²).
ĭ	ACCEL	اتما	1	ARG	the magnitude of the acceleration vector (Km/sec ²)
I	RXX	-	1	ARG	the magnitude of the change in the second integral compared to the previous step. (Km)
I	ISTART		1	ARG	an index used to define if INGRAT is functioning in the start mode (ISTART=1 for Runge-Kutta) or the continue

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
					mode (ISTART=2 for Gauss- Jackson)
I	Ľ		1	ARG	an index used to check the number of consecutive times through HSIZE that the step size has been adjudged to be too small (when L=4 the step is doubled)
I	IH	-	1	ARG	an index used to deter- mine if a step is to be guessed (to be refined later) or if the present step is to be checked. IH=1 for guess; =2 for present step
C	Ħ	h	1.	ARG	the step size to be employed in the numerical integration of the equations of motion employing the Gauss-Jackson backwards difference formulation. (sec)

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Subroutines Required: None

Functions Required: ALOG10 (log to the base 10)

Approximate Deck

Length: 377 (octal)

Discussion:

The basic rationale for deciding whether the stepsize for the integration (Gauss) is adequate is based on a set of more or less arbitrary limits for the absolute value of the largest sixth difference (DEL6). These limits, in turn, are based on the order of the magnitude of the acceleration and were selected in such a manner that the integration series would be convergent to the desired degree with terms through the sixth difference included.

One slight problem arises in the application of this rationals in that if the acceleration itself ever passes through zero, the tolerance goes to zero; and the stepsize is immediately adjudged to be too large. To surmount this problem, a second test is employed in those cases where the quantity DEL6 is larger than that allowed by the upper limit. This second test requires that the contribution of the sixth difference to the second integral be less than one part in 10^4 of the change in the second integral for the last step, i.e.

$$\Delta r^{6H} \approx H^2 \Delta^6 / 15$$

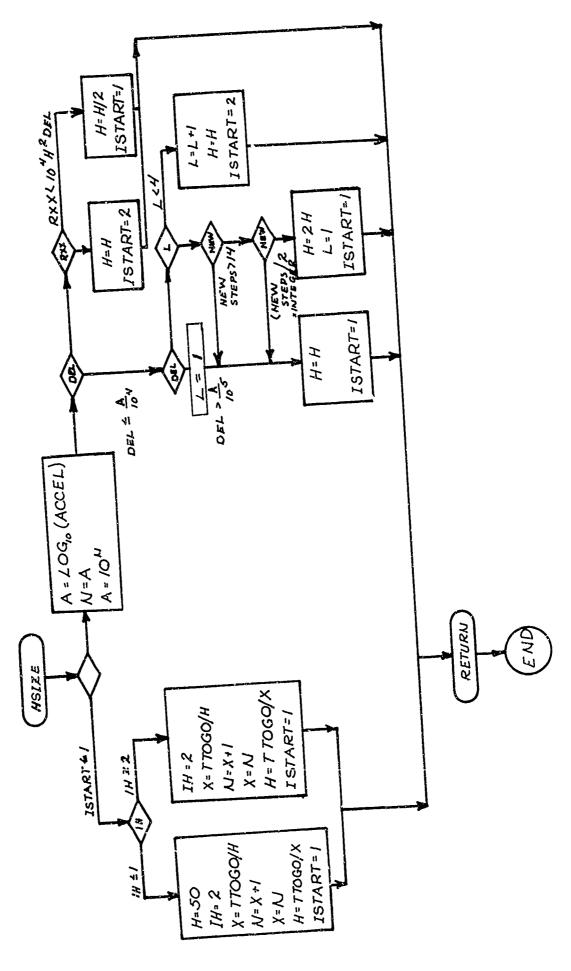
$$\leq 10^{-4} \left| \Delta \vec{r}_{n-1} - \Delta \vec{r}_{n-2} \right|$$

or say

$$10^3 H^2 \Delta^6 < |\Delta \hat{r}_{n-1} - \Delta \hat{r}_{n-2}|$$

(The second integral is the displacement from the reference conic which is growing in a reasonably slow fashion.) The step is always halved if the upper tolerance level is violated.

Three other modifications to this basic rationals were also coded for the sake of operation, efficiency and accuracy. Each of the three pertains to the case where a signal would normally be generated to double the step size (DEL6 less than lower limit). The first modification is employed to assure that the step size is too small at several consecutive points before a signal is generated to double the step. This practice assures that fewer cases in which the tolerance range is temporarily violated on the low end will result in restart. The second modification is employed to assure that after a whole number of the new integration steps, the time-to-go can be reduced to zero (this performance is essential in the operation of the program). This second test is passed automatically if the step is halved; however, if the step is doubled, time-to-go divided by the old step must be even. The third modification is employed to assure that the integration can be effectively restarted prior to the time that the time-to-go will reach zero.



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SOURCE STATEMENT

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                                                     INTEGRATION VIA GAUSS METHOD. THE SELECTED INTERVAL
WILL BE DOUBLED OR HALVED IF SUCH IS CONSISTENT WITH THE
PRINT TIME (OR TERMINAL TIME ) CONSTRAINT, IF THE SIXTH
                                                                                                                                                                            SMALL FRACTION OF THE CHANGE IN RXX FROM THE PREVIOUS H.
                                                                                                                                                                                                                                                                                                                  COUNT TO SEE HOW MANY TIMES THAT DELS IS LESS THAN LIMIT
                                                                                                                                                       SIXTH DIFFERENCE TO THE SECOND INTEGRAL IS LESS THAN A
                                                                                                                                      OF THE ACCELERATION , AND IF THE CONTRIBUTION OF THE
                                      HSIZE DETERMINES THE STEP SIZE TO BE UTILIZED IN NUMERICAL
                                                                                                                                                                                                                                                         CHANGE IN THE SECOND INTEGRAL FOR PREVIOUS STEP
I IF INTEG IS TO COMMAND A RESTART ** =2 IF INTEG
                                                                                                                                                                                                                                                                                                                                                                                                                                       GAUSS INTEGRATION ( H RUNGE-KUTTA
SUBROUTINE HSIZE( [TOGO,DEL6, ACCEL, RXX, ISTART, L, IH, H
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SOURCE STATEMENT
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                                                   CHECK6 = 1.E3 *H*H*ABSDEL
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EFN
                     = 10° **N*.2E-3
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                              SCALE1/40.
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GO TO 20

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X = XI

Y = Y

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ABSUEL

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60 TO 10

H = H/2.

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			SYMBOL X SCALE1 CHECK6 IY		-		. –		SID 65-1203-1 25 -197-

2.3.1.3.2 Subroutine START

Purpose:

START is a fourth order Runge-Kutta integration routine utilized to establish the accelerations at the seven points along the trajectory and define the difference table required by the Gauss-Jackson integration.

Deck Name:

START

Calling Sequence:

Call START

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	RCO	rco	3	WRK (28)	The position and vel- ocity vectors in the
	VCO	₹co	3	WRK (31)	frame of 1950.0 des- cribing the conic reference trajectory at the time of the last rectification (Km, Km/sec)
n	RAD	₹ ₅₀	3	WRK (44)	the position and velo- city vectors in the
	VEL	₹50	3	WRK (47)	computational coordinate frame of 1950.0 (Km, Km/sec) at the epoch t+h
1/0	RDD	Ar	3	WRK (58)	the acceleration (Km/sec2) the velocity
	RD	Å.	3	WRK (55)	(Km/sec), and the posi- tion (Km) vectors
	R	ΔŤ	3	WRK (52)	relative to the reference ellipse in the coordinate frame of 1950.0
1/0	TIME	t-t _c	1	WRK (104)	the time interval in seconds since the last rectification of the reference ellipse

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
0	RC	rc	3	WRK (117)	the instantaneous reference position
	VC	\overline{v}_{c}	3	WRK (120)	and velocity vectors (1950.0) (Km,Km/sec)
I	H	h	1	WRK (1.23)	the step size employed in the integration (sec). This quantity is one-half that employed in the Gaussian integration.

Subroutines Required: CONIC (reference conic)

MOTION (total acceleration vector relative to ellip-

tical reference)

Functions Required: None

Approximate Deck

Length: 500 (octal)

Discussion:

START functions in the standard single integration Runge-Kutta mode. That is, the second-order differential equation is reduced to two first-order differential equations with the substitution

$$\frac{\dot{\vec{v}}}{\dot{\vec{r}}} = \frac{\ddot{\vec{r}}}{\ddot{\vec{r}}}$$

and each part which may be represented as

$$\dot{x} = f(t,x)$$

as integrated as follows:

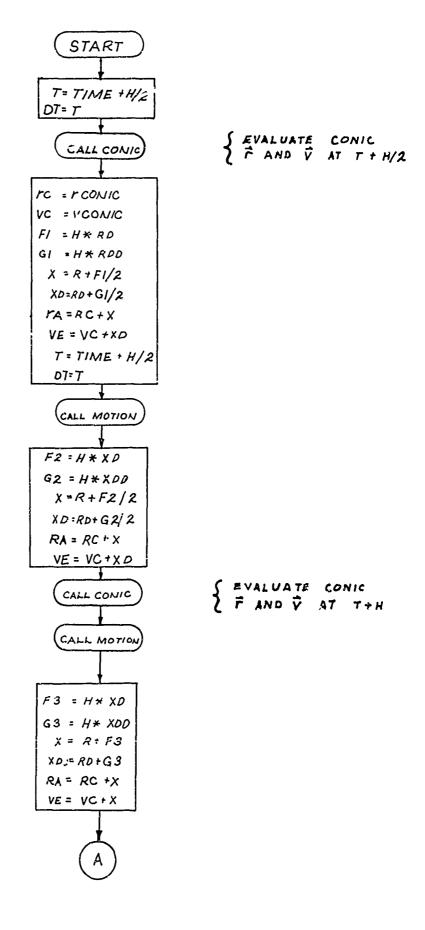
$$x (t+h) = x (t) + \frac{h}{6} (f_1 + 2f_2 + 2f_3 + f_4)$$

where:

$$f_1 = f(t,x)$$
 $f_2 = f(t+h, x+h f_1)$
 $f_3 = f(t+h, x+h f_2)$
 $f_4 = f(t+h, x+h f_3)$

No corrector cycles or smoothing operations are superimposed on this procedure. Thus, since the errors tend to grow more rapidly in this method of integration than is the case with the Gauss-Jackson integration, it was decided that the step size utilized for each step of the starter would be no more than one-half of that utilized for the continuation integration. This step (made in INGRAT) assures a more consistent level of accuracy in the two routines. It is noted, however, that the subroutine MOTION must now be called eight times in this mode of operation, compared to one time in the Gauss mode.

A complete discussion of the development of the Runge-Kutta family of integration formulae can be found in many texts treating the subject of numerical integration. One such text is <u>Numerical Analysis</u> by K. Z. Kunz and published by McGraw-Hill in 1957.



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CALL MOTION

F4 = H * XDD

G4 = H * XDD

R = R + FI/6 + F2/3 + F3/3 + F4/6

RD = RD + G1/6 + G2/3 + G3/3 + G4/5

RAD = RCN + R

VEL = VCN + RD

RETURN

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SOURCE STATEMENT

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START130 START160 START190 START230 START040 START050 START070 START090 STARTIOC START110 START120 START150 START170 START180 START210 START240 START280 START290 START330 STAR T030 START060 STARTOBO START140 START200 START22C STAR 1250 START260 START270 STAR T300 START305 START310 START320 START340 THE VERSIUN USED IN THIS ROUTINE IS THE KUTTA-SIMPSON ONE-THIRD START SETS-UP A 4-TH ORDER RUNGE-KUTTA INTEGRATION AND EVALUATES Ħ THE POSITIONS AND VELOCITIES NECESSARY TO COMPUTE THE ACCELERATIONS USED IN A GAUSS-JACKSON INTEGRATION . (DATA(1), CUN), (DATA(16), SAT), (DATA(36), SDA) ¥ , RDD (3) , XD(3) , F3(3) A (4) (WRK(44), RAD = ACCELERATION VECTUR FOR RELATIVE MOTION (1950.0) (WRK(55), RD RULE EXTENSION OF THE QUADRATURE FORMULA DIMENSION CON(1), SAT(1), SDA(1), WRK(1), STT(1) , RO (3) F2(3) 64(3 , X(3) , (DATA(286),STT), (DATA(391), WRK) Ħ = RELATIVE VELOCITY VECTUR (1950.0 VE(3) , F1(3) 63(3) TIME= SECUNDS FROM LAST RECTIFICATION ,R(3) R= RELATIVE PUSITION VECTOR (1950.0) [WRK[31) , VCO (WRK(52) , R = VELOCITY VECTOR(1950.0) = RADIUS VECTOR (1950.C) VEL (3) , RDK (3 ,RA(3) STEP SIZE IN SECONDS **KAD(3)** ,RR(3) (WRK(28), RCU 47), VEL , VC (3) SUBKUUTINE START EQUIVALENCE EJUIVALENCE CUMMON DATA **#** · UI MENSION , I WRK! 5, KUUR (3) 3, x00(3) 2,80(3) 4,84(3) VEL RDD KAD R C STD 65-1203-1 -203-

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(WRK (120) , VC (WRK(117), RC

(WRK (104), TIME

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                                                                                                                                                                           =RR(1) + F1(1)/2.
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              IFN(S)
                                                                                                                                                                                                          R(I) =RR(I) + (F)(I)+2.*(F2(I)+F3(I))+F4(I))/6.
RU(I) =RDR(I)+ (C)(I)+2.*(G2(I)+G3(I))+G4(I))/6.
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              SOURCE STATEMENT
               EFN
                                                                                                                                                                                                                                                               VEL(1) = VC (1) +RD(1)
                                                                                                                                                                                                                                      RAU(I)= RC (I) + R(I)
                                                                                                RA (I) = RC (I) + X(I)

VE (I) = VC (I) + XD(I)
                                                                      X (1) = KR(1) + F3(1)
                                                                                  XU(1) = RUR(1) + G3(1)
                                                                                                                                                                                F4(1) = H^* \times D(1)

C4(1) = H^* \times DD(1)
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                                           F3(I) = H^* \times D(I)

G3(I) = H^* \times D(I)
                                                                                                                          CALL MOTION(1,2)
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2.3.1.3.3 Subroutine DIFTAB

Purpose:

DIFTAB differences seven values of the acceleration

vector and constructs the diagonal of backward differences and leading sums required in the Gauss-Jackson integration

routine (INTEG).

Deck Name:

DIFTAB

Calling Sequence: CALL DIFTAB (RCTORE, VSTORE, STORE, H, COEF)

Input/Output:

I/o	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	RSTORE VSTORE	Δr _ų Δv _ų	3 3	Arg Arg	the position and velocity vectors relative to the reference ellipse at the center point in the table. (Km, Km/sec)
I	STORE	Δ Ϊ 1	7, 3	Arg	the array of acceleration vectors at seven times (spaced at intervals of h) which are to be differenced and summed (Km/sec ²)
I	н	h	1	Arg	the step in time which correlates the various entries in the STORE array (sec)
0	COEF	Σ; Σ; Δ; Δ;	8, 3	Arg	the array of numbers which is required by INTEG for the integration of the equations of Motion. The first subscript denotes the second sum, the first sum, the first difference, the sixth difference. The second subscript denotes the x, y and z components.

Subroutines Required: None

Functions Required:

None

Approximate Deck

470 (octal)

Length:

Discussion:

The output of the start cycle is an array of acceleration vectors at seven times (spaced h seconds apart) and position and velocity vectors for the center point. These numbers will be utilized to construct the leading diagonal required in the Gauss-Jackson integration process as follows

- 1) The six differences of the components of the acceleration vector will be constructed.
- 2) The second sum corresponding to the position for the central value of the acceleration is calculated from:

$$\Sigma_0^2 = \frac{\chi_0}{h^2} - \frac{\ddot{\chi}_0}{12} + \frac{\Delta_0^2}{240} - \frac{31\Delta_0^4}{60480}$$

3) The average value of the first sum corresponding to the velocity for the central value of the acceleration is calculated from:

$$\sum_{0}^{1} = \frac{x_{0}}{h} + \frac{\left(\Delta_{-\frac{1}{2}}^{1} + \Delta_{+\frac{1}{2}}^{1}\right)}{24} - \frac{II\left(\Delta_{-\frac{1}{2}}^{3} + \Delta_{+\frac{1}{2}}^{3}\right)}{I440} + \frac{I90\left(\Delta_{-\frac{1}{2}}^{5} + \Delta_{+\frac{1}{2}}^{5}\right)}{I20960}$$

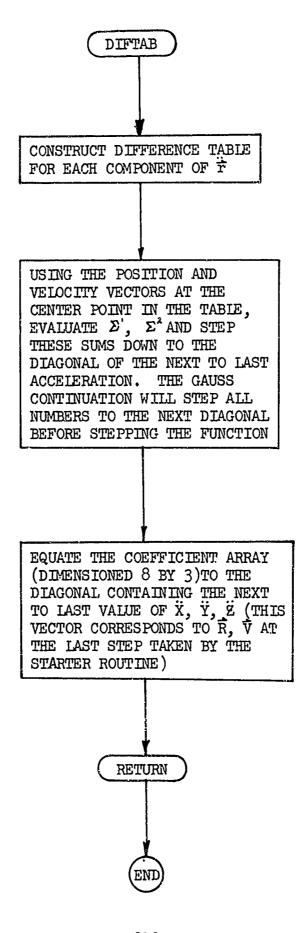
and the corresponding first sum on the proper diagonal in the difference table is

$$\Sigma_{2}' = \Sigma_{0}' + 2 \tilde{\lambda}_{0}'$$

4) The first and second sums are stepped down to the next to last diagonal and the terms along this diagonal are loaded into an array set aside for input into INTEG. (The next to last diagonal was selected since INTEG updates the diagonal before performing the integration).

In order to preserve accuracy in these operations the differencing will be performed in double precision. This procedure has been shown to conserve approximately one significant figure when operating with the IBM 7094.

Computational Logic:



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JTAB0210
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STORE = ARRAY OF ACCELERATION VECTORS ( 7 POINTS )
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                                                                          THIS ROUTINE IS USED IN STARTING AN INTEGRATION
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12/02/85
         IFN(S)
        SOURCE STATEMENT
                          191.*(F(1)*F(2))/120960.
SUM1 +.5* A(4)
SUM2 + SUM1
        FFN
                                                                                           COEF(8,K) = F(2)-F(1)
COEF(7,K) = F(1)
COEF(6,K) = E(2)
COEF(5,K) = O(3)
                                                               A(1+4)
                                                                        SUM2
                                                                                                                                                             SUM2
                                                                                                                                  C (4)
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                                                               SUMI = SUMI + A
SUM2 = SUMI + S
CONTINUE
                                                      DO 300 I=1,2
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SID 65-1203-1

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2.3.1.3.4 Subroutine INTEG

14.

Purpose:

INTEG continues a stepwise integration of the equations of motion in a Gauss-Jackson mode once started by an independent process. The routine employes six differens and is formulated around the backwards difference

concept (no corrections)

Deck Name

INTG

Calling Sequence:

CALL INTEG (SAVE)

Input/Output

I/O	FORTRAN NAME	MATH NAME	DIMENSION	COM/ ARG	DEFINITION
I/O	COEF	Σ ² : Δ ⁶	8,3	WRK(71)	The array containing the diagonal to be utilized in the next integration step em- ploying Gauss' Equation (2 sums, 6 differences, 3 components of acceleration)
I	RDD	Δ̈́r	3	WRK(58)	The acceleration vector defining the motion relative to the reference ellipse (Km/sec2)
I/O	SAVE	Δ̈̈́r,	3	Arg	The acceleration vector at the last integration step (Km/sec ²)
0	RD R	Δ Γ ΔΓ	3	WRK(52) WRK(58)	The incremented position and velocity vectors for the motion relative to the reference ellipse (Km/sec ²)

1/0	FØRTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	STEP	Н	1	WRK(68)	The stepsize for the numerical integration of the eq. of motion (sec)

Subroutines Required:

None

Functions Required:

None

Approximate Deck Length:

330 (octal)

Discussion

The continuation of the intregration will be performed by employing a Gauss-Jackson or double sum formulation. This process is accomplished by mechanizing the following backwards difference formulae

$$\begin{split} \dot{\chi}_{i+i} &= \mathcal{H} \Big(\sum_{i+1/2}^{\prime} + \frac{\ddot{z}}{2} \, i + \frac{5}{12} \, \Delta_{i-\frac{1}{2}}^{\prime} + \frac{3}{8} \, \Delta_{i-1}^{2} \\ &+ \frac{25!}{720} \, \frac{\Delta^{3}}{i^{-3}/2} \, + \frac{95}{288} \, \Delta_{i-2}^{4} \, + \frac{19087}{600480} \, \Delta_{i-\frac{5}{2}}^{5} - \frac{5}{2} \\ &+ \frac{5257}{17280} \, \Delta_{i-3}^{5} \Big) \\ \chi_{i+i} &= \mathcal{H}^{2} \Big(\sum_{i+i}^{2} \, + \frac{\ddot{\chi}}{i2} \, i + \frac{\Delta^{1}}{12} \, i - \frac{1}{2} \, + \frac{12}{240} \, \Delta_{i-1}^{2} \\ &+ \frac{18}{240} \, \Delta_{i-\frac{3}{2}}^{3} \, + \frac{1725}{24192} \, \Delta_{i-2}^{4} \, + \frac{1650}{24192} \, \Delta_{i-\frac{5}{2}}^{5} \\ &+ \frac{15}{240} \, \Delta_{i-3}^{6} \Big) \\ \Sigma_{i+\frac{1}{2}}^{\prime} &= \sum_{i-\frac{1}{2}}^{\prime} + \ddot{\chi} \\ \Sigma_{i+i}^{2} &= \sum_{i}^{2} + \sum_{i+\frac{1}{2}}^{\prime} \\ \Delta_{i-\frac{1}{2}}^{\prime} &= \ddot{\chi}_{i} - \ddot{\chi}_{i-1} \\ \Delta_{i-1}^{2} &= \Delta_{i-\frac{1}{2}}^{\prime} - \Delta_{i-\frac{3}{2}}^{\prime} \end{aligned}$$

This mechanization will be aided by the establishment of a two dimensional array which will be referred to as the coefficient array (COEF) and which will contain the information required by the formula.

$$COEF(I,I) = \sum_{x}^{2}$$

$$COEF(I,2) = \sum_{y}^{2} \dots$$

$$COEF(2,I) = \sum_{x}^{i}$$

$$COEF(3,I) = \Delta_{x}^{i}$$

$$\vdots$$

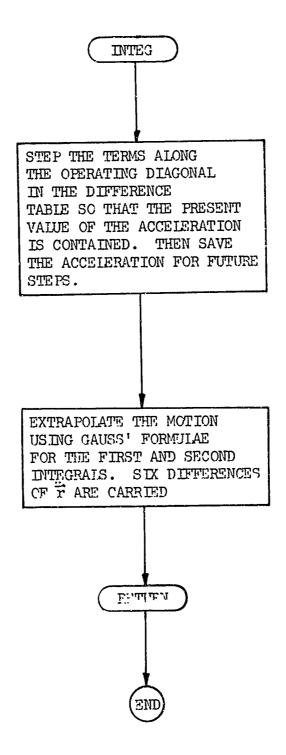
$$COEF(8,I) = \Delta_{x}^{i}$$

(This array is thus seen to contain the terms along the second leading diagonal) Upon entry to INTEG, the diagonal which is stored in COEF will correspond to the last integration step; thus, the first task to be performed will be the updating of COEF according to the definition of its members. This done, the trajectory can be stepped.

Two specific comments are required regarding this process. First, the process is obviously not exact and thus for extreme accuracy a corrector cycle based on central differences should be employed. This type of operation has been avoided by attention to detail in the formulation of the trajectory portion of the program and by careful selection of the stepsize. However, this revision is felt to be advisable if any numerical problems develop during the application of the differential corrections program to the determination of satellite orbits.

The other comment is an observation which pertaines to the fact that two integrations which are performed are both based on the acceleration rather than on the acceleration and velocity. This fact results in the evaluation of the second integral to an accuracy superior to that obtained with the other approach or for that matter, to that obtained for the first integral. This behavior is very desirable for this program since it assures that the major contributives to the acceleration at future points along the trajectory (primarily functions of position) will be well known. Care must be taken, however, in applying this logic to trajectories for which the non-linear effects of drag, etc. are involved since for these cases the accumulative errors in the first integral (X) could drastically effect the predicted path.

Computational Logic:



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STOREZ = SAV(1)

STURE: = RUU(I)

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RETURN ONI 45-1203-1 -219-STD

GAJSS690

5257. *COEF(8,1)/17280.

10 CUNTINUE

GAUSS710

GAUSS720

GAUSS700

00 10 1=1,3

H = STEP H2= H#H

SAV(1) = RUD(1)

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2.3.1.4 THE TRACKING GROUP

TRAK

This group of routines is designed to define the position and velocity of the satellite relative to each of a set of prescribed tracking stations. This task is performed by defining the position vectors for the group of tracking stations as a function of the time, and associating with each, a set of unit vectors describing a topodetic coordinate system. This information is then utilized to determine the range, range-rate azimuth and elevation of the satellite relative to each of the stations.

The operations are performed with the aid of the following routines:

Driver routine for computing the relative position and velocity data for each station GHA Defines the position of the Greenwich meridian

as a function of universal time

UNIT Constructs the position vector for the

tracking station and the topodetic coordinate

system

EQINOX Computes the correction to the computational

coordinate frame of 1950.0 (used for trajectory

definition) to adjust for nutation and

precession

Following the construction of the relative position information for a given station, a check is made to determine whether observation data are available for the epoch under analysis for that station. If not, the checking of the various stations is continued. However, if data are available, transfer is made from this group into the Filter group and a correction to the state vector is computed before continuing the station check process. This link between the two groups is very important and deserves considerable attention.

Subroutine TRAK

Purpose:

mpak is designed to check each of the tracking stations being employed at each point along the trajectory for the purpose of identifying those stations at which the vehicle is visible and to check the data tape to see if data is available at that time before transferring to the data filter.

Deck Marie:

 $\text{TRAC}_{\mathcal{V}}$

Galling Sequence:

Call TRAY (ISTART)

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т/п	FORTPAN Name	Math Mame	Nimension	Common/ Argument	Definition
C	TSTART	-	1	Arg	Index utilized to restart the integration when the next data point has been read into
Т	CUMAS	-	7	CON (11) CON (12)	Conversion factors (days to seconds and degrees to radians)
T	biCilu.	-]	COM (JY)	Outrut tare number
Т	NChECA	-	1.	SAT (16)	Index utilized to check stations for visibility at all times or just at the times for which there is data
T	がいいい	_	í	SAT (17)	Index to limit number of stations checked
т	STATII		でし	STA (1)	Array containing data for the stations to be checked (latitude, longitude, altitude and name)

I/O	FORTRAN Name	Math Mame	nimension	Common/ Argument,	Definition
I	HORCOR	ΔFI	j∩	STA (41)	Horizon corrections for each of the up to 10 stations employed
I	Number	-	1	STA (241)	Motal number of stations being employed
I	ROTATE ROTIPV	PIMT	3 x 3 3 x 3	Mbk (10)	Matrix for transforming the frame of 1950.0 to that of data and its inverse. The MPT50
I	Ем	νì	3 x 3	MUK (19)	Nutation array relating the mean equator of date to the true equator of date. $r_{\rm D} = v_{\rm m}$
τ	TTRANW TTRANF	t∽_¬	l i	WRK (42) WRK (43)	Time of last data point
T :	RVEC, VVEC	r ₅₀ v ₅₀	3 3	MBk (72)	The cartesian resition and velocity vectors of the satellite at the time TW + TF in the reference frame of 1950.0
T	TW, TF	to	1,1	WRK (50) WRK (51)	The two words defining the epoch at which the station rositions are desired (days) relative to 1950.0 (40 2433282.423)
1	TWDATA TFDATA	t _n	1	WRK (61) WRK (62)	Time of next data roint relative to the epoch of 1950.0
T	TTRAK	-	1.	WRK (63)	Station which next senses the vehicle
О	H	h	1	WRK (68)	First approximation to step size for integration to the next time for which there is no data (sec)
т/о	RT	rŢ	3	WRK (95)	The tracking station position vector (Km) in the frame of date

.T/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
1/0	SLAT SION SALT	L λ H	1 1 1	WRY (105) WRK (106) WRK (107)	Tracking station lati- tude, longitude and altitude (rad, rad, Km)
I\0	U E 7	U E N	3 3 3	WRK (108) WRK (124) WRK (127)	Wp, east, north unit vectors at the tracking station being checked
O	RDATE VLATE	r _D Vp	3 3	WR ^K (111) WRK (114)	The instantaneous position and velocity vectors in the true equator of date frame (Km, Km/sec)

(arc tangent) ARKTMS Subroutines Required: (cross product)
(driver for filter chair) CRASS FILTER GHA (Greenwich hour angle) (Station vectors) UMIT STHAT (Static transition matrix) (matrix multiplication) MATMPY (Vector magnitude) Functions Required: AMAG (Arc tangert) ATAN: (Dot product) DOT Approximate Deck 650 (octal)

Length:

Description & Formulation:

Trak is designed to check each of the stations being employed in the tracking network (one to ten) to determine the relative position of the vehicle at that epoch. As a portion of the process the range, range-rate, azimuth and elevation of the vehicle in topocentric coordinates are computed for the purpose of comparison with the actual tracking data in a differential correction of the trajectory itself. The procedure involved is presented below:

Upon defining the position and velocity vectors in the frame of date and computing the Greenwich Hour Angle associated with the time (GHA), the location of each of the stations is computed and a set of unit vectors defining a topocentric (radar Az-EL) coordinate system is constructed (UNIT). At this point the relative position and velocity are computed

$$\vec{\rho} = \vec{r}_{d} - \vec{r}_{t} ; \rho = |\vec{\rho}| ; \dot{\rho} = \frac{\vec{\rho}}{\rho} \cdot (\vec{v}_{d} - \vec{v}_{t})$$

and the elevation and azimuth are defined as follows:

$$\sin E \mathbf{l} = \frac{\vec{p} \cdot \hat{\mathbf{U}}}{P} -90 < E \mathbf{l} < 90$$

$$\cos E \mathbf{l} = +\sqrt{1-\sin^2 E \mathbf{l}}$$

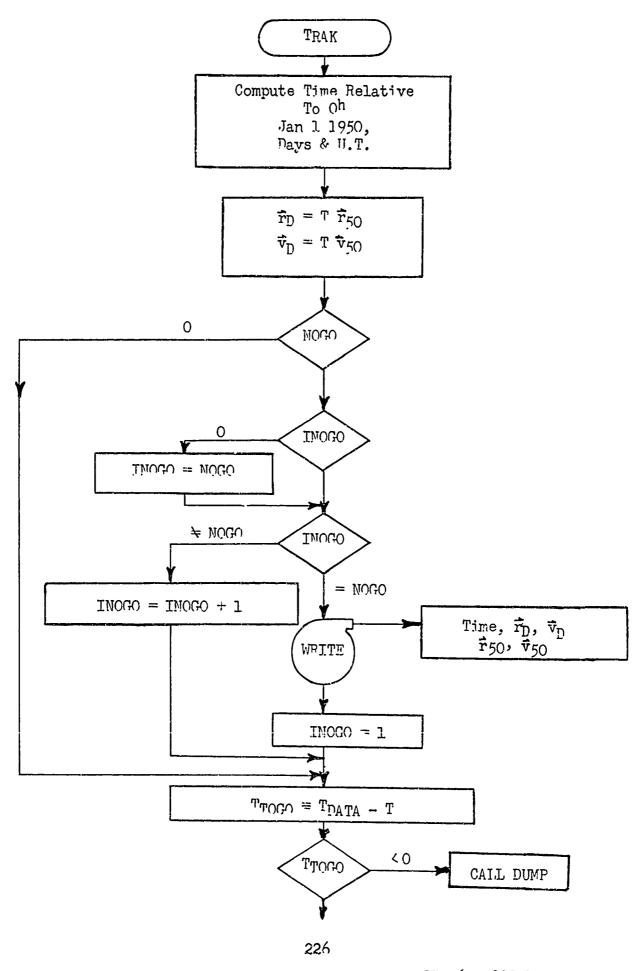
$$\cos a = \frac{\vec{p} \cdot \hat{\mathbf{N}}}{P} = \cos A_z \cos E \mathbf{l}$$

$$\sin b = \frac{\vec{p} \cdot \hat{\mathbf{E}}}{P} = \sin A_z \cos E \mathbf{l}$$

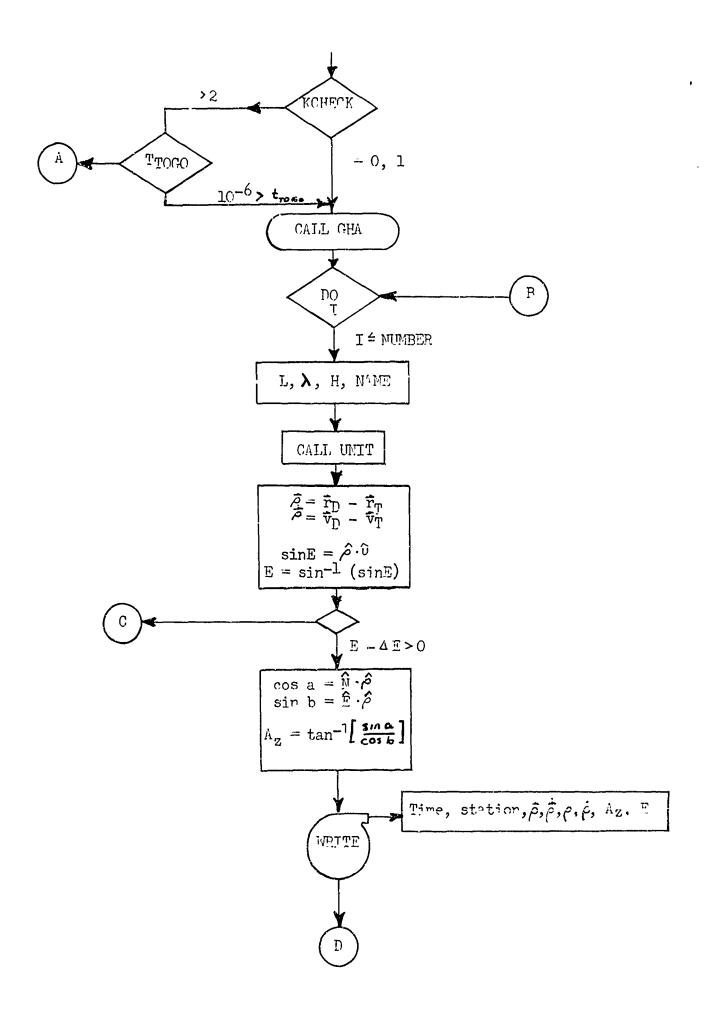
$$\tan A_z = \frac{\vec{p} \cdot \hat{\mathbf{F}}}{\vec{p} \cdot \hat{\mathbf{N}}}$$

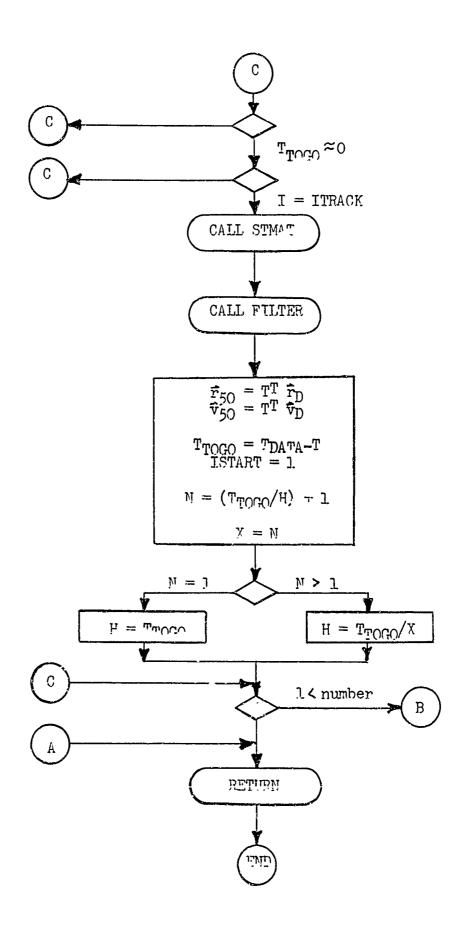
When the data point has been reached (i.e., the time at which data from the tracking stations is available) and associated with the proper station, the FILTER group is called and the data point processed. However, before the solution can proceed and before the trajectory can be stepped, the radius and velocity vectors in the frame of 1950.0 must be defined. This step is necessary due to the fact that subroutine UPSTAT may have adjusted the trajectory discretely in order to correct the tendency for the observed and computed trajectories to diverge.

TRAK is designed in such a manner that the routine can be by-passed in two distinctly different modes. First, if specified in the input data, the stations can be checked at every point along the trajectory (i.e., at every integration step) so as to provide a record of the track or only at those times when data is known to be available. This option drastically improves the general efficiency of the computational logic. Secondly, if desired, a minor efficiency can be effected in that only that station actually recording data at the time of the observation need be checked.



SID 65-1203-1





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SGURCE STATEMENT

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2.3.1.4.7 Subroutine UNIT

: Pozogriid

IMITT computes the position vector defining the location of the tracking stations and evaluates the components of the (IIp. Tast. North) unit vectors at

the station.

Deck Mamo:

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Calling Sequence:

Call INTT (CHA)

Input/Output

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Ţ	GHA.	GHA	I	Arg	Hour Angle of Greenwich relative to the vernal equinox (rad)
T	ਧੜ	P. c	7	70M (1)	rquatorial radius of the earth (rm)
Ţ	रPOI	Pp	1	COT (2)	Polar radius of the earth (Km)
0	ቪካ ሚ	$\dot{\hat{\mathbf{r}}}_{\eta}$	3	M&A (02)	Position vector for the tracking station at this time (Km)
J	STAT	т,	j	WRK (105)	Station latitude (Ceodetic) in radians
Т	SIOM	λ	٦	WW (104)	Station longitude in radians
Т	SAIT	н	١	Msh (104)	Station altitude (Fm)
C	п,т,Z	и, т, п	3,3,3	MBK (152) MBK (157) MBK (108)	Up, East, Morth unit vectors expressed in cartesian coordinates in the true equator of date frame

Subroutines Required:

None

Functions Required:

SIN (sine)

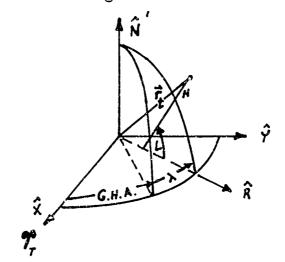
COS (cosine)
SQRT (square root)

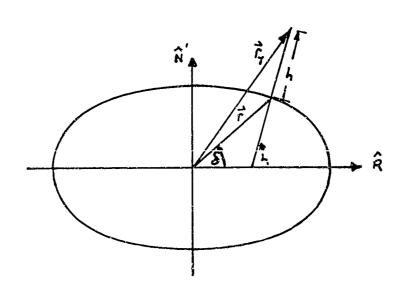
Approximate Deck Length:

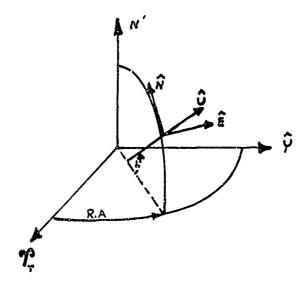
170 (octal)

Formulation.

UNIT computes the components of a set of topocentric unit vectors for each of the tracking stations being checked as a function of the time and the radius vector of the tracking station itself. The unit vectors will be constructed first utilizing the information and definitions presented on the following sketches.







thus

$$\begin{bmatrix} \mathbf{U} \\ \mathbf{E} \\ \mathbf{N} \end{bmatrix} = \begin{bmatrix} \cos \mathbf{L} & \mathbf{O} & \sin \mathbf{L} \\ \mathbf{O} & \mathbf{i} & \mathbf{O} \\ -\sin \mathbf{L} & \mathbf{O} & \cos \mathbf{L} \end{bmatrix} \begin{bmatrix} \cos \mathbf{R} \cdot \mathbf{A} \cdot & \sin \mathbf{R} \cdot \mathbf{A} \cdot & \mathbf{O} \\ -\sin \mathbf{R} \cdot \mathbf{A} \cdot & \cos \mathbf{R} \cdot \mathbf{A} \cdot & \cos \mathbf{R} \cdot \mathbf{A} \cdot & \mathbf{O} \\ \mathbf{O} & \mathbf{O} & \mathbf{I} \end{bmatrix} \begin{bmatrix} \mathbf{N} \\ \mathbf{Y} \\ \mathbf{N}' \end{bmatrix}$$

$$= \begin{bmatrix} \cos \mathbf{L} \cos \mathbf{R} \cdot \mathbf{A} \cdot & \cos \mathbf{L} \sin \mathbf{R} \cdot \mathbf{A} \cdot & \sin \mathbf{L} \\ -\sin \mathbf{R} \cdot \mathbf{A} \cdot & \cos \mathbf{R} \cdot \mathbf{A} \cdot & \mathbf{O} \\ -\sin \mathbf{L} \cos \mathbf{R} \cdot \mathbf{A} \cdot & -\sin \mathbf{L} \sin \mathbf{R} \cdot \mathbf{A} \cdot & \cos \mathbf{L} \end{bmatrix} \begin{bmatrix} \mathbf{N} \\ \mathbf{Y} \\ \mathbf{N}' \end{bmatrix}$$

The vector defining the position of the tracking station is, however, more difficult to construct since it is not found by simple rotation. This construction is, however, simplified by noting that

$$\hat{r} = \hat{r} + h \hat{U}$$

$$= r (\cos \delta \hat{R} + \sin \delta \hat{N}') + h \hat{U}$$

and that the quantity $\{$ can be evaluated by considering the equation of the ellipse in the $(\hat{R}$, $\hat{N})$ plane

$$\frac{\chi^2}{a^2} + \frac{2^2}{b^2} = 1$$

JOM

$$\frac{dZ}{dX} = -\frac{b^2}{a^2} \frac{X}{Z} = -\text{Tan L}$$

and

$$\operatorname{Tan} \ \delta = \ \underline{Z}_{\overline{X}}$$

thus

$$Tan \delta = \frac{b^2}{a^2} tan L$$

But from the polar form of the equation of an ellipse

$$r = \frac{ab}{(a^2 \sin^2 \delta + b^2 \cos^2 \delta)^{\frac{1}{2}}}$$

or

$$r \cos \delta = \frac{a}{(\frac{a^2}{b^2} \tan^2 \delta + 1)^{\frac{1}{2}}}$$

r
$$\sin \delta = \frac{b}{(\frac{b^2}{a^2} \cot^2 \delta + 1)^{\frac{1}{2}}}$$

so that upon substitution

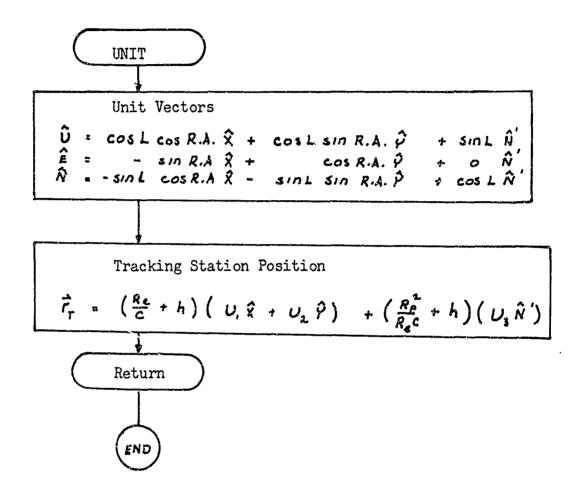
$$\hat{r}_{T} = \left[\frac{a}{(b^{2} \sin^{2} L + \cos^{2} L)^{\frac{1}{2}}} + h\right] (U, \hat{\gamma} + U_{2} \hat{Y})$$

$$+ \left[\frac{b^{2}}{(b^{2} \sin^{2} L + a^{2} \cos^{2} L)^{\frac{1}{2}}} + h \right] U_{3} \hat{N}'$$

where: $a = equatorial radius (R_e)$

b = polar radius (R_p)

Computational logic



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UNITU400
UNITU410
UNITU440
UNITU440
UNITU450
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         SCURCE STATEMENT
                          E(1) = -SLN

E(2) = CLN

E(3) = 0.

Z(1) =-SLA*CLN

Z(2) =- SLA *SLN

Z(3) = CLA

RT(1) = (RE/C +H)*U(1)

RT(2) = (RF/C +H)*U(2)

RT(3) = (RPOL*RPOL/(RE*C) +H)*U(3)

RETURN

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SID 65-1203-1

2.3.1.4.2 Subroutine FQINØX

Purpose:

EQINOX computes the transformation matrices relating

the true equator of data frame of reference to the mean equator of 1950.0 (J.D. 0433082.423) frame.

Deck Name:

enøx

Calling Sequence:

CALL ECINOX (TIME)

Input/Output

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	TIME	t	1	Arg	mean solar days since 1950.0 (J.D. 2433282.428
С	ROTATE	NP	3 X 3	WRK (1)	rotation matrix trans- forming vectors in the frame of 1950.0 to the frame of date
0	ROTINV	PTNT	3 X 3	WRK (10)	rotational transforma- tion to convert vectors in frame of date to frame of 1950.0
0	EN	N	3 X 3	WRK (19)	nutation matrix relating vectors in the mean equator of date frame to those in the frame of date (used in GHA)

Subroutines Required:

MATMPY (matrix multiplication)

Functions Required:

SIN (Sine)

COS

(cosine)

Approximate Deck

Length:

1540 (Octal)

Description and Formulation:

Over 2000 years ago it was discovered that the Verna' Equinox would move from east to west by 50". 2453 every year. This me lon is called precession and is caused by the gravitational attraction of other celestial bodies acting on the equatorial bulge of the earth. If the earth were perfectly spherical and radially homogeneous, it would not experience any deviation from its mean equatorial pole. However, since the earth has an equatorial bulge, it experiences torques from the gravitational attraction of the sun and the moon. Due to the fact that the lunar orbital plane is approximately 50 oblique to the mean ecliptic, both the lunar and solar torques tend to align the equator with the ecliptic. The earth responds to this torque much like a spinning top responds to a torque. It precesses about the mean ecliptic pole. This precession is called luni-solar precession. Since the moon is so much closer to the earth than the sun, its contribution to luni-solar precession is approximately twice as much as that from the sun. The equatorial pole has an obliquity of about 23.50 so at the rate of precession mentioned earlier, the equatorial pole would very nearly trace a right circular cone every 25,800 years.

Just as the sun and moon cause the equatorial pole to precess, so do the planets of our solar system cause the ecliptic pole to precess; however, the magnitude of this planetary precession is very small and will be considered negligible in this discussion.

"Total general precession" is the sum of planetary and luni-solar precession and gives the changes in the mean vernal equinox of date from some epoch. Total general precession amounts to 50". 2453/year and can be considered uniform for practical use. This is the rate of westward rotation of the mean vernal equinox of date.

As the equatorial pole precesses about the ecliptic pole, it also experiences further disturbances known as nutations. Free Eulerian Nutations are those which would occur if the earth were simply set in rotation and left to itself without any disturbing forces. Forced nutations are those which are caused by the changing positions in space of the sun, earth, and moon, which in turn cause variations in their respective gravitational attractions to the earth.

The most significant nutation is the 19 Year Lunar Nutation. This nutation is caused by the precession of the moon's orbit, which is inclined about 5° oblique to the mean ecliptic. The line of nodes associated with these planes precesses with a period of about 18.6 years. The result is to change the direction of the small fluctuations in potential experienced by the earth-moon system.

Other forced nutations include the Semi-annual Solar Nutation and the Fortnightly Lunar Nutation. These phenomena are the result of the decreasing torque that the sun and moon apply to the earth as they approach the passing of the equatorial plane. Due to symmetry, the net torque, as one of these bodies passes through the equatorial plane, is zero.

The earth model that is generally used for the analyses of this motion is a rigid ellipsoid which is later simplified to an oblate spheroid. This model does not account for elasticity, fluidity and other physical properties of the earth; but it is sufficient to use for a fairly complete derivation of precession and nutation. It must thus be noted that the results of an analysis using such a simplified model are not exact.

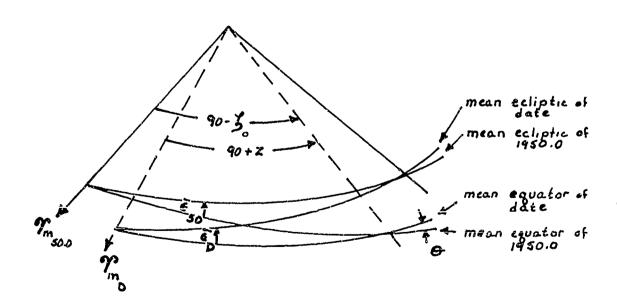
Improvement of the theoretical analysis resulting from the incorporation of observed data in the evaluation of the constants of integration and from the incorporation of more complete models of the earth in the analysis have, however, been effected. The results of these efforts based on formulations presented in the American Ephemeris and Nautical Almanac will be presented in the following paragraphs.

Precession:

Uniform precession is a rotation of the coordinate system defining the mean equator of date and may thus be represented by the matrix equation

$$\vec{r}_m = P \vec{r}_{50}$$

where \vec{r}_{50} denotes the position vector in the standard inertial reference frame (fundamental plane and principal direction are the mean equator of zero hours, January 0, 1950 and the corresponding vernal equinox) and where \vec{r}_m is the position vector in the mean equator of date frame. The problem thus, becomes one of determining the elements of P. This step in turn is accomplished by selecting 3 small parameters which relate the two frames. One such set is shown in the following sketch



The earth model that is generally used for the analyses of this motion is a rigid ellipsoid which is later simplified to an oblate spheroid. This model does not account for elasticity, fluidity and other physical properties of the earth; but it is sufficient to use for a fairly complete derivation of precession and nutation. It must thus be noted that the results of an analysis using such a simplified model are not exact.

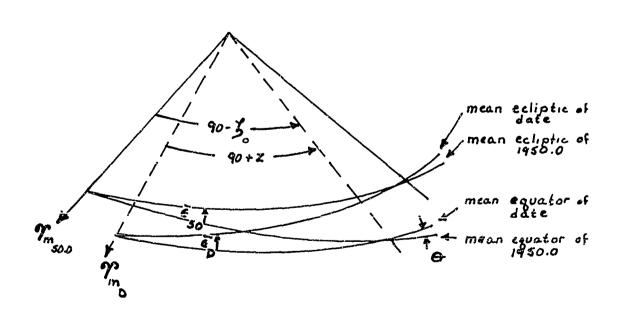
Improvement of the theoretical analysis resulting from the incorporation of observed data in the evaluation of the constants of integration and from the incorporation of more complete models of the earth in the analysis have, however, been effected. The results of these efforts based on formulations presented in the American Ephemeris and Nautical Almanac will be presented in the following paragraphs.

Precession:

Uniform precession is a rotation of the coordinate system defining the mean equator of date and may thus be represented by the matrix equation

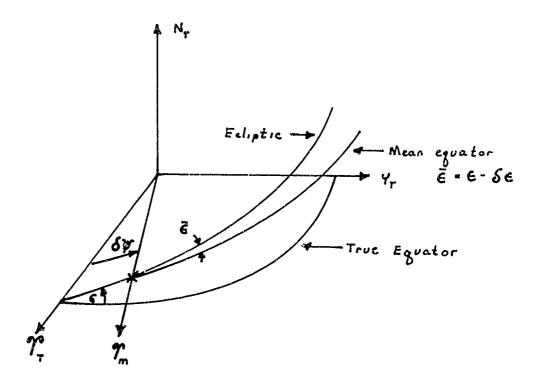
$$\vec{r}_m = P \vec{r}_{50}$$

where \vec{r}_{50} denotes the position vector in the standard inertial reference frame (fundamental plane and principal direction are the mean equator of zero hours, January 0, 1950 and the corresponding vernal equinox) and where \vec{r}_{m} is the position vector in the mean equator of date frame. The problem thus, becomes one of determining the elements of P. This step in turn is accomplished by selecting 3 small parameters which relate the two frames. One such set is shown in the following sketch



Nutation:

The relationship between the mean and true equator of date may be represented in terms of two small parameters as shown in the following sketch



and the small parameters ($\delta \psi$ and $\delta \epsilon$) can be divided into long ($\Delta \psi$ and $\Delta \epsilon$) and short (d ψ and d ϵ) period contributions which can be computed as a function of a set of quantities defined in the Nautical Almanac. These quantities are given in time series as:

$$\Omega = 12.112790 -0.052953922 D +0.0020795T +0.002081T^{2} +0.000002T^{3}$$

$$\Omega = 64.375452 +13.176397 D -0.001131575T -0.00113015T^{2} -0.0000019T^{3}$$

$$T' = 208.84399 +0.11140408 D -0.010334T -0.010343T^{2} -0.000012T^{3}$$

$$T = 282.08053 +0.000047068 D +0.0004553T +0.0004575T^{2} +0.000003T^{3}$$

L = 280.08121 + 0.98564734 D + 0.000303 (T+T²)

where D = Days since reference epoch (1950.0) (J.D. 2433282.423)

T = Julian centuries past reference epoch

Corresponding to these time series the small parameters are:

```
\Delta \psi \times 10^4 = -(47.8927 + .0482T) \sin \Omega
                + .5800 sin 2\Omega - 3.5361 sin 2L - .1378 sin (3L- \Gamma)
                + .0594 sin (L + \Gamma) + .0344 sin (2L - \Omega) + .0125 sin (2\Gamma - \Omega)
                + .3500 \sin (L - \Gamma) + .0125 \sin (2L - 2\Gamma')
    d\psi_{x} 10<sup>4</sup> = -.5658 sin 2 & -.0950 sin (2 ( - \Omega )
                -.0725 \sin (3(-T') + .0317 \sin ((+T'))
                + .0161 \sin (Q - T' + \Omega) + .0158 \sin (Q - T' - \Omega)
                -.0144 \sin (3 G + T^{\dagger} - 2L) -.0122 \sin (3 G - T^{\dagger} - \Omega)
                + .1875 \sin (( -T') + .0078 \sin (2( -2T'))
                +.0414 \sin (( + T' - 2L) + .0167 \sin (2  - 2L)
                -.0089 \sin (4 \% - 2L).
    \Delta \epsilon \times 10^{4} = 25.5844 \cos \Omega - .2511 \cos 2 \Omega
                + 1.5336 \cos 2L + .0666 \cos (3L - T)
                -.0258 cos (L + T ) -.0183 cos (2L - \Omega)
                - .0067 cos (2T' - Ω)
     d \in \times 10^4 = .2456 \cos 2 ( + .0508 \cos (2 ( - .0.))
                +.0369 \cos (3 (-T') -.0139 \cos ((+T'))
                -.0086 cos (( - T' + \Omega) + .0083 cos (( -T' - \Omega))
                + .0061 cos (3 (7 + T' - 2L) + .0064 cos (3 (7 - T' - \Omega))
Now since the mean obliquity of date is given by
           \vec{\epsilon} = 23.4457587 - .01309404T - .00000088T^2 + .00000050T^3
and since
```

- 252 -

 $\epsilon = \tilde{\epsilon} + \delta \epsilon$

the rotational transformation relating the frames (X_m, Y_m, Z_m) and (X_T, Y_T, Z_T) is

$$\vec{r}_T = T_X (-\varepsilon) T_Z (-\delta \psi) T_X (\bar{\varepsilon}) \vec{r}_m$$

$$= N \vec{r}_m$$

where T () denotes a rotational transformation, the subscript denotes the axis of rotation and the term in the parenthesis denotes the angle of rotation. Expansion of this transformation yields N as:

$$n_{11} = \cos \delta y$$

$$n_{12} = -\sin \delta \psi \cos \bar{\epsilon}$$

$$n_{13} = -\sin \delta \psi \sin \bar{\epsilon}$$

$$n_{21} = \sin \delta \psi \cos \epsilon$$

$$n_{22} = \cos \delta \psi \cos \epsilon \cos \tilde{\epsilon} + \sin \epsilon \sin \tilde{\epsilon}$$

$$n_{23} = \cos \delta \psi \cos \epsilon \sin \bar{\epsilon} - \sin \epsilon \cos \bar{\epsilon}$$

$$n_{31} = \sin \delta \gamma \sin \epsilon$$

$$n_{32} = \cos \delta \psi \sin \epsilon \cos \bar{\epsilon} - \cos \epsilon \sin \bar{\epsilon}$$

$$n_{33} = \cos \delta \psi \sin \epsilon \sin \bar{\epsilon} + \cos \epsilon \cos \bar{\epsilon}$$

which upon substitution of $\bar{\epsilon} + \delta \epsilon$ for ϵ may be approximated as

$$N = \begin{bmatrix} 1 & -\delta \psi \cos \bar{\epsilon} & -\delta \psi \sin \bar{\epsilon} \\ \delta \psi \cos \bar{\epsilon} & 1 & -\delta \epsilon \\ \delta \psi \sin \bar{\epsilon} & \delta \epsilon & 1 \end{bmatrix}$$

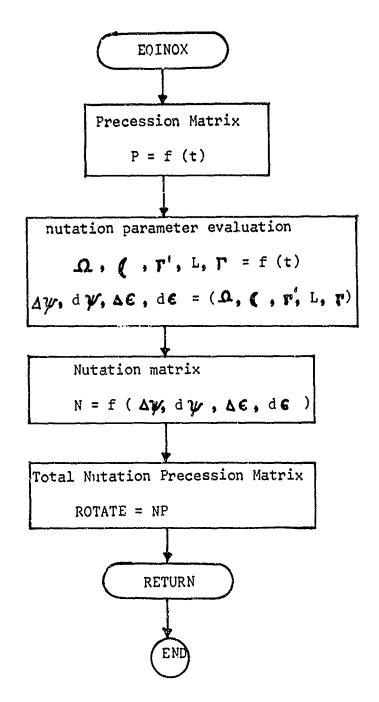
Combined Nutation and Precession:

The true equator of data frame and that corresponding to the mean equator of 1950.0 can now be related by direct substitution of the results of the previous paragraphs.

$$\hat{\mathbf{r}}_{m} = P \hat{\mathbf{r}}_{50}$$

$$\hat{\mathbf{r}}_{T} = N \hat{\mathbf{r}}_{m}$$
or
$$\hat{\mathbf{r}}_{T} = NP \hat{\mathbf{r}}_{50} \equiv [ROTATE] \hat{\mathbf{r}}_{50}$$
and
$$\hat{\mathbf{r}}_{50} = (NP)^{T} \hat{\mathbf{r}}_{D} \equiv [ROTINV] \hat{\mathbf{r}}_{D}$$

Computational Logic:



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THE VECTORS IN THE CROPOLNATE FRAME OF 1950.0 TO THOSE IN THE TRUE FOUNTINE ALSO 14. S POUTINE COMPUTES THE TRANSFORMATION MATRIX WHICH PELATES STARES THE NUTATION MATRIX IN CAMMAN FOR OTHER USES. TIME IS DAYS FROM 1950.0. ネ ** ** ** ** ℀ ℀ 35 35

SURPRUTINE FOINGX (TIME)

DIMENSION CAN(1), SAT(1), SDA(1), WRK(1), STT(1) ** **

CRWEIN DATA

1),(PN), (DATA(16), JAI), (DATA(36), SDA) () ATA(EOUILVAL ENCE

*(DAIA(286),STT), (DATA(391),WRK)

nivensian Rgtate (3,3), A (3,3), FN (3,3), RGTINV (3,3)

FQ':IVAL ENCF

1), RUTATE), (WRK(1C), RUTINV) , (WRK(10), FN (NRK (

÷۶ 4⊱ 4⊱ ł⊦ 36 36 36 * * ** ** ** ** ₩ ₹ ¥ ₹∻ 48 *}

STEP IS THE CONSTRUCTION OF THE MATRIX (A) WHICH DEFINESFNOXOPORTHE FEFFCTS OF PRECESSION ON THE MEAN EQUATOR OF DATE. ENOXOZOC FIRST STEP IS THE CONSTRUCTION OF

T = TIMF/36525.

= -.07234988T - .000006764T2 + .000002218T3 A(i,i) = 1. - . COO29697*T2 - . ODOOO 13*T3 T2 = 57 $1 \times 1 = 21$ A(1,2)

E1*96000000 + 21*40000000 + 1*11416000 = = $= -\Lambda(1,2)$ A(7,1) 1(1,3)

= I. - .; 0.024976#T2 - .0000015#T3 4(0,0)

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01/22/86		ENØXO550 ENØXO560	ENGXO570 ENGXO580 FNGXO590	FNGXO610 FNGXO620 FNGXO630	ENGX0640 ENGX065C ENGX065C ENGX057C ENGX063C ENGX063C	
***** S FNGX - FFN SGURCE STATEMENT - IFN(S) -	A(3,2) = A(2,3) A(3,3) = 1nncc4721*T2 + .ccoocooc*T3 THE SECGND STEP IS TO DEFINE THE EFFECT OF NUTATION OF THE EARTHS SPIN AXIS AND THE DEPARTURES FROM THE MEAN FRAME OF DATE O = TIME CR = 12.112799052953922*D+.002079*T+.002081*T2+.000002*T3 CR = 64.375452+13.176397*D01131575*T00113015*T2+.000002*T3 CR = 64.375452+13.176397*D01131575*T00113015*T2+.000012*T3 CR = 64.375452+13.176397*D01131575*T00113015*T2+.000002*T3 GP = 268.84399+.1114C408*D010334*T010343*T2000012*T3 UL = 260.F8121	(\F + Q) - • 0]	DD = .2456*CMS (2.*CR)+.F598*CMS (2.*CR-MM)+.A360*CMS (3.*CR-GP) 1P139*CMS (CR+GP)C986*CMS (CR-GP+MM)+.9083*CMS (CR-GP-MM) 2 +.FA61*CMS (3.*CR+GP-2.*VL)+.AACMS (3.*CR-GP-MM) AT = -{4.728927+.C482*I}*SIN (AM)+.58*SIN (2.*MM)	3.5361\$SIN (7.*VL)1378\$SIN (3.* .0344\$SIN (7.*VL-04)+.0125\$SIN (3.*	DS =5658*SIN (2.*CR1095*SIN (2.*CR-0M)7725*SIN (3.*CR-GP) 1 +.0317*SIN (CR+GP)+.0161*SIN (CR-GP+0M)+.0158*SIN (CR-GP-0M) 20144*SIN (3.*CR+GP-2.*VL)0172*SIN (3.*CR-GP-0M) 3 +.1875*SIN (CR-GP)+.0778*SIN (2.*CR-6P) 4 +.0414*SIN (CR+GP-2.*VL)+.0167*SIN (2.*CR-2.*VL) 50089*SIN (4.*CR-2.*VL)	Si

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                                                                   FNGX0760
                            FNGX0710
                                            FNGX0730
                                                   FN8X0740
                                                           FN0X0750
                                     ENGX072C
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FR = 23.4457587- C1309474*T-. 0000098*T2+. 0000005*T3

= -DT*CGS (E8) -01*SIN (F3)

-FN(1,2)

1. -0E

= .17453296E-5*(DF+DD) = .17453296E-5*(DI+DS)

FR = FP*. C17453296

FPS11 = EB+NF

FY(1,1) FA (1,2) EN(1,3) FN(2,1) FN(2,2) FN(2,7) E4(2,1)

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FNGX0920

THE TOTAL RATATION MATRIX IS NOW DEFINED BY UTILIZING MATRIX MULTIPLICATION.

-EN(1,3) DE

EN(3+2)

CALL MATMPY (EN, 3, 3, 4, 3, 3, 8 GTATE) Da 100 J=1,3 nr 1-1 1=1+3

RPIINV(I,J)=POTATE(J,I) RFTURN

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2.3.1.4.3 Subroutine GHA

Purpose:

GHA Computes the hour angle of the Greenwich meridian

relative to the true vernal equinox of date in degrees.

Deck Name:

GHAN

Calling Sequence: Call GHA (T, D, GH, DA, OMEGA)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	T	t	1	Arg	Universal time for the selected date at which GH is to be computed (sec.)
I	מ	^D 50	1	Arg	Mean solar days elapsed since O ^h Jan. 1, 1950 (integral number)
0	GH	$m{\eta}_{ ext{T}}^{e}(ext{t})$	1	Arg	Greenwich hour angle in degrees
I	DA	da	1	Arg	Nutation correction to reference GH to true equinox of date
0	OMEGA	ω	1	Arg	Rotational rate of the earth at the selected epoch

Subroutines Required:

None

Functions Required:

Sign

Approximate Deck Length: 160 (octal)

Formulation:

The hour angle of the Greenwich meridian relative to the mean vernal equinox of epoch T is given in the Nautical Almanac as

$$7^{\circ}_{m}(t) = 100^{\circ} .07554260 + 0^{\circ} .985647346d + (2^{\circ} .9015) \times 10^{-13}d^{2} + wt \pmod{360}$$

where $d = the integral number of days past <math>0^h$ 1 January 1950

 $t = time in seconds past <math>0^h$ of the epoch data

$$\omega = \frac{.60 \text{ l.} 17807 \text{ l.} 17}{1 + (5.21) 10^{-13} \text{ d}}$$

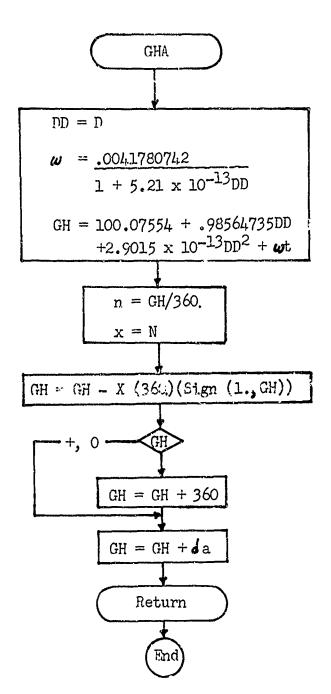
Thus, in order to be consistent with the measure of time in the remaining portion of the program (time reckoned from 1950.0) it was simply required that the whole and fractional number of days (D_{50}) reckoned from 1950.0 be changed by the difference

$$d = D_{50} - .077$$

and that a correction for nutation (da) be applied to compute the hour angle with respect to the true vernal equinox

$$\mathbf{Y}_{T}(t) = \mathbf{Y}_{m}(t) + da$$

Computational Logic:



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GHAN

SUBROUTINE GHA(T, D, GH, DA, DMEGA)

GHA00020

GHA00040 GHA00050 GHA00120 GHA00130 GHA00090 GHA00100 GHA00110 GHA00160 GHAG0170 GHA00030 GHA00060 GHA00070 GHA00080 GHA00140 GHA00150 GHA0018C 3HA00190 GHA00200 ₩

GHA COMPUTES THE HOUR ANGLE OF GREENWICH RELATIVE TO THE MEAN VERNAL EQUINOX OF DATE († IS UNIVERSAL TIME IN SECONDS.)

D IS DAYS SINCE ZERG HRS U.T. 1 JAN 1950) ¥ # ¥ * Ħ * * ₩

OMEGA = .0041780742/(1.+5.21E-13*DD) GH = 100.07554 + .98564735*DD + 2.9015E-13*DD*DD + OMEGA*T N = GH/360. X = N

GH = GH - X*360.*SIGN(1.,GH) IF(GH) 1,2,2

GH = GH + DA*57.295780GH = GH + 360.RETURN

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2.4 The Data Filter Group

The reduction of the data provided by the preprocessor (PROCES) will be accomplished utilizing a minimum variance recursive filter first developed by Dr. R. E. Kalman (the reference and a description of the filter will be presented in KALMAN). However, because there are several distinct operations involved in the process, it has been deemed desirable (from the standpoint of program modifications for other types of data, ease of development and checkout, etc.) to construct the filter in the form of several subroutines. This group of routines is the subject of the discussions which follow commencing with the driver (FILTER) and with the formulation (KALMAN). These routines are discussed prior to all of the remaining routines, since they establish the mathematical framework in which the others can best be understood, and because they establish the notation to be employed.

The interface of the differential corrections program and its preprocesson is also embedded in this group. This interface exists in the form
of a routine (DATAPE) designed to read the specially prepared data tape
and load the smoothed observation vector and identifying information into
memory. The operation of this routine has been checked (as has the operation
of all other routines in the program) to assure compatibility between the
two programs.

2.4.1 Subroutine FILTER

Purpose:

FILTER is designed as the driver for all routines in the Data Filter Group. It also serves the function of computing the observation vector (observed minus computed

residuals).

Deck Name:

FILT

Calling Sequence:

CALL FILTER (NUMB, R, RD, A, E)

Input/Output:

т/о	FORTRAN Name	Math Name	Dimension	Common/ Argument	Description
I	NUMB	-	1	ARG	Number of the station being checked at this time in the routine TRAK
I	R RD A E	A E	1 1 1	ARG ARG ARG ARG	The computed values of range, range rate, azimuth and elevation relative to the tracking station (based) on the optimum estimate of the trajectory at this time (Km, Km/sec, rad, rad)
I	ODATA	-	3	WRK(65)	Observed values of range, range rate azimuth and/or elevation (no more than 3 pieces of this information at a time) (Km, Km/sec, rad, rad)
I	ITYPE	-	1	WRK(64)	The fixed point index which identifies which of the six possible types of data is being processed

Subroutines Required: MEASURE (computes)

ERROR (computes)

KALMAN (computes x and r)

UPSTAT (updates problem)

DATAPE (provides next data point)

MAIN (deck name of main program)

Functions Required: None

Approximate Deck

Length: 205 (octal)

Description:

Subroutine FILTER serves as the driver routine for the complete filter package. It is designed to function in such a manner that all of the information required by KALMAN is available when the call is made. To be specific:

- 1) The first step made is the identification of the type of data being processed and the construction of the ordered set of observed minus computed residuals.
- 2) The next step is the computation of the matrix M^T (OBST = $\frac{2\vec{V}}{2\vec{K}}$) in subroutine MEASUR and the definition of the weighting matrix in subroutine ERROR
- 3) At this point KALMAN is called and the state vector (\overline{X}) and the covariance matrix for the error in \overline{X} are estimated.
- 4) UPSTAT is then entered to determine if the trajectory is known to a degree sufficient to allow-up-dating. If so, new conic elements are computed and written.

Upon return from UPSTAT the problem has been reduced by one of the smoothed data points (7 words - TW, TF, TYPE, STATION, OBSERVATION VECTOR (3)) and DATAPE is entered to determine if additional data are available. If so, the the next data point is read into memory and control is returned to the program. If there is no additional data, exit from the program is accomplished by calling the \$IBFTC name of the main program (MAIN). This sequence is utilized at this time since it allows other cases to be run in a sequential manner, however, it is noted that a modification of this procedure may be required for other systems.

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FILT0080
                                                                                                                                                                                                                                                                                   FILT0120
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                                                                                                                                                                                             THE GBSERVED*MINUS*COMPUTED RESIDUALS FOR THE DATA TYPE
                                                                                                                                                                                                                                         STEP IS COMPLETE THE REMAINING ROUTINES IN THE FILTER
                                                                                                                                                                                                                                                                                  PARTIALS OF THE OBSERVABLES WITH RESPECT TO THE STATE
                                                                                                                                                                      WHICH DATA IS AVAILABLE. THE FIRST STEP IS TO COMPUTE
                                                                                                                                                                                                                                                                                                                                                                       PGINT ( PRIGR TO RETURN ) A CHECK IS MADE TO SEE IF THE
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                                                                                                                             PORTION OF THE PROGRAM. IT IS CALLED FROM SUBROUTINE
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                                                                                                                                                                                                                                                                                                         ERROR COMPUTES THE STATION AND NOISE ERROR MATRIX
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                                                                                                         SERVES AS THE DRIVER ROUTINE FOR THE DATA REDUCTION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           WHEN KOUNT RETURNS A 3, THERE IS NO MORE DATA
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2.4.1.1 Subroutine KALMAN

To obtain the minimum variance estimate of the position Purpose:

and velocity relative to an estimated trajectory and to produce the covariance matrix for errors in the estimate.

Deck Name:

KALM

Calling Sequence:

Call KALMAN (OBVEC, M)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Description
I	OBVEC	Y	М	ARG	The vector composed of observed minus computed residuals (from FILTER)
I	М	-	1	ARG	The dimension of the observation vector
I	PHI	φ(t,t,)	6 X 6	STT(1)	Transition matrix relating errors at two successive data points (from STMAT)
I	OBST	M ^T (t)	6 X 3	STT(37)	Matrix of partials of obser- vations with respect to the state (from MEASUR)
I	Q	Q (ŧ)	3 X 3	STT(55)	Covariance matrix for contri- bution of errors in observa- tions and of errors in station location (from ERROR)
1/0	STATE	X (t)	6	STT(64)	The vector $\left\{ \begin{array}{l} \Delta \vec{r} \\ \Delta \vec{r} = \vec{r} - \vec{r}_0 \end{array} \right\}$ where $\Delta \vec{v} = \vec{v} - \vec{v}_0$ sub o = reference
I/O	P	P (ŧ)	6 X 6	STT(70)	Covariance matrix for errors in the estimated state vector

Subroutines required: TRANSP (matrix transpose) (matrix multiplication) MATMPY MTINY (matrix inverse) SUBMAT (matrix subtraction) (matrix addition) ADDMAT Functions required: None Approximate Deck 1056 (octal) Length:

Formulation:

The theory of Kalman's recursive minimum variance data filter was first presented in a series of papers (e.g. Ref. 1) in which the author developed rigorously the form of the resultant estimate by employing an orthogonal projection lemma derived as a portion of the paper. Since this computational algorithm is utilized in the digital program being discussed, its form must be discussed. However, since complete descriptions of the development are recorded (Ref. 1), only a summary of the steps required will be presented.

The basic assumption of this procedure is that the optimal estimate of the state vector (X) for the system (in this case the vector $\left\{ \stackrel{\Delta_i}{\Delta_i} \right\}$) is of the form. $\hat{\chi}^{\frac{1}{3}} = \sum_{i=1}^{n} \alpha_i y_i$ where Y_i for this discussion are the components of the observed minus computed residuals (Y = IX), where the systems equations are

$$x(t) = \varphi(t, t_o) x(t_o) + u(t_o),$$

where φ (ξ , ξ _o) is an n by n matrix of time-dependent coefficients and where u (t) is an independent Gaussian process (u will not be utilized in the estimation procedures). Lest this assumption be questioned on the grounds that it is excessively restrictive, note is made of the fact that Kalman proved that the results obtained with this model can, in general, be improved a with non-linear estimation only if the errors in the data and/or in the state vector for the system are non-Caussian. Further, to achieve the improvement, at least third-order distribution functions for the errors are required.

Now, attention is turned to the problem of obtaining the optimum estimate of the state $(\hat{\chi}^*(\xi))$ at some time t by utilizing only the last estimate of the state $(\hat{\chi}^*(\xi))$ and the observation at time t. This statement of the problem leads to the basic form of the computation algorithm

$$\widehat{\chi}(\overset{*}{t}) = \varphi(t, t-1) \widehat{\chi}^*(t-1) + K(t) [Y(t)$$

$$-M(t) \varphi(t, t-1) \widehat{\chi}^*(t-1)]$$

$$= \varphi(t, t-1) \widehat{\chi}^*(t-1) + K(t) \Delta \varphi(t)$$

where the first term is the estimate of X(t) obtained utilizing data a quired prior to the last data point but propagated to time t. The second term is a weighted correction which is determined by the difference in the observed and predicted values of the observed minus computed residuals.

The task is now to define the optimum linear gain K(t) (optimum here will be taken to mean in the sense of minimum variance) to be utilized in the algorithm. This task will be accomplished by adopting the notation

$$y(t) = M(t) \times (t) + \epsilon(t)$$

$$x(\xi) = \hat{x}^*(\xi) + \mathcal{N}(\xi)$$

where $\boldsymbol{\xi}$ (t) and $\boldsymbol{\eta}$ (t) are Gaussian errors and where the notation $\boldsymbol{\eta}$ (t) means the error at t based on all data processed prior to t. Expanding these identities

$$\varphi(t) = M(t) \, \varphi(t, t-1) \, \hat{\chi}^*(t-1) \\
+ M(t) \, \varphi(t, t-1) \, \eta(t) + \varepsilon(t) \\
\eta(t) = \left[\varphi(t, t-1) - K(t) M(t) \, \varphi(t, t-1) \right] \eta(t-1) \\
- K(t) \varepsilon(t)$$

and noting that the optimum estimates for X satisfies the conditions that the covariance matrix for q (t) q^r (t) is minimized, or from the referenced lemma, that

$$E(\eta(\xi) Y'(\xi)) = 0 = \text{Expected value of } ($$

yields upon substitution and expansion (after the independence of γ and \hat{X} and of E and \hat{X} are assumed).

$$[\varphi(t,t-1) - K(t)M(t)\varphi(t,t-1)] E[\eta(t-1)\eta^{T}(t-1)]\varphi^{T}(t,t-1)M^{T}(t)$$

$$- K(t) E[\epsilon(t)\epsilon^{T}(t)] = 0$$

At this point in the development, a slight change in the notation is adopted in that

$$P(t-1) = E[\eta(t-1) \eta^{T}(t-1)]$$

$$Q(t) = E[e(t)e^{T}(t)]$$

and it is noted that if P (t-1) is positive definite then the product

$$M(t)\varphi(t,t-1) P(t-1)\varphi^{\tau}(t,t-1)M^{\tau}(t)$$

will also be positive definite provided that the observables (components of y) are linearly independent. Thus, the product is invertable; and the optimum weighting matrix is

$$K(t) = \varphi(t, t-1) P(t-1) \varphi^{T}(t, t-1) M^{T}(t) \cdot$$

$$\left[M(t) \varphi(t, t-1) P(t-1) \varphi^{T}(t, t-1) M^{T}(t) + Q(t) \right]^{-1}$$

$$\equiv P(t) M^{T}(t) \left[M(t) P(t) M^{T}(t) + Q(t) \right]^{-1}$$

Now since the distributions of the errors in the estimates can be prescribed at time zero and since the covariance matrix for the contribution of the stations to the uncertainty can be defined at any given time, the first weighting matrix can be computed. However, to reduce additional data points, the relationship defining the covariance matrix for the errors in the estimate after the reduction of the data point (P (t)) must be defined. This matrix may in turn be evaluated from the definition of P (t)

$$P^{*}(t) = E(R^{*}(t) R^{*T}(t))$$

$$= \varphi^{*}(t, t-i) P(t-i) \varphi^{*T}(t, t-i) + K(t) Q(t) K^{T}(t)$$

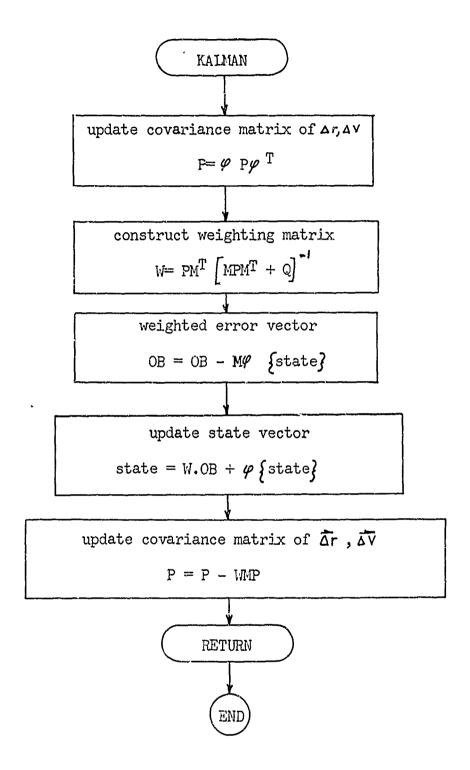
where
$$\varphi'(t,t-1) = \varphi(t,t-1) - K(t)M(t)\varphi(t,t-1)$$

Filter Description (operational characteristics)

The minimum variance formulation presented here is a simplification of the maximum likelihood estimator in that it assumes the errors are normally distributed. This, however, is the only valid objection voiced to the use of this procedure since in its general form the formulation includes most other data filters. (For example; weighted least squares - the simple case where the components of y are uncorrelated). The recursive nature of the filter also provides a distinct advantage since non-linear effects resulting from errors in the equations of motion and from non-precise relation of the errors at various points along the trajectory are minimized by the fact that time required for data accumulation is itself minimized. Further, if the trajectory is updated at each of the data points (assuming that the elements of P (t) are sufficiently small to make this practice feasible) the linear system can predict the behavior of the non-linear system to a very good degree. Finally, due to the recursive nature of the filter, the order of complexity in reducing any number of data points is constant; and problems of loss of numerical significance arising from manipulating large arrays of numbers are drastically reduced.

Ref. 1 Kalman, R. E., "A New Approach to Linear Filtering and Prediction Problems" <u>Journal of Basic Engineering</u> (March 1960.) pages 35-45

Computational Logic:



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                                                                                                                                                                                                                                           TIME THE LAST BBSERVATION DATA WERF PROCESSED . THIS
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                                                                            AND VELOCITY RELATIVE TO THE REFERENCE TRAJECTORY )
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                                                                                                                    FSTIMATF . THIS FORMULATION IS BASED ON AN ORIGINAL
                                                                                                                                                                                FNGINFFRING ** MARCH 1960 ** PAGE 35-45 ) IN WHICH
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                                      THIS ROUTINE COMPUTES THE KALMAN ESTIMATE OF THE STATE VECTOR
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                                                                                                                                        PAPER BY R.E. KALMAN (A NEW APPROACH TO LINEAR
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C.Wales

2.4.1.2 Subroutine STMAT (State Transition Matrix)

Purpose:

to provide the 6 X 6 matrix of partial derivatives o. the state vector at some arbitrary time with respect

to the state vector at an earlier epoch.

Deck Name:

STM

Calling Sequence:

Call STMAT (TIME)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	RTRAN	ř,	3	WRK (36)	radius vector in frame of date at time t
I	VTRAN	₹,	3	WRK (39)	velocity vector in frame of date at time t
I	RDATE	<u>r</u> 2	3	WRK (111)	radius at t ₂
I	VDATE	$\vec{v_2}$	3	WRK (114)	velocity at t2
I	TIME	Δt	1	ARG	t ₂ - t ₁
0	PHI	φ(t ₂ ,t,)	6 x 6	STT (1)	matrix $\left[\frac{\partial \vec{x}_2}{\partial \vec{x}_1}\right]$

Subroutines required:

TRANS

(conic Transition matrix)

INVAO

(analytic transition inverse)

Functions required:

None

Approximate Deck

Length:

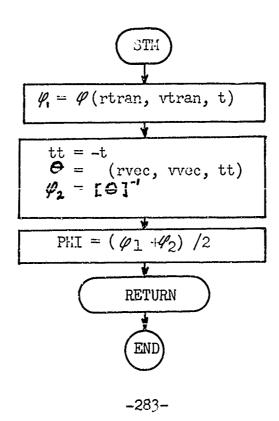
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(octal)

Description:

The trajectories for the vehicles of interest to this study are nearly conic. Thus, partial derivatives evaluated for the nominal conic trajectory will agree well with those obtained from the true trajectory by more elaborate means such as the integration of the adjoint equations. For this reason, the conic representation will be utilized to construct the c X 6 matrix of partial derivatives though two slight modifications will be employed to assure that the conic and true matrices agree as well as possible. The first modification is that the position and velocity vectors used to define the partials will correspond to those of the true trajectory at the time from which the errors are propagating in this case, (the last data point) rather than the corresponding point on the conic references trajectory. The second modification is that the true position and velocity vectors at the time of the present data point will be utilized to obtain the inverse of a second estimate of this matrix by solving the conic problem backward in time. This second matrix will then be analytically inverted, utilizing a special property of this matrix (developed in INVAO) to obtain the desired partials. These two matrices of partials will not be identical because the conic trajectories utilized to define them differed in regard to each of the six constants of integration (the result of oblateness, drag --- forces). Further, they will differ from the true matrix. However, a first-order estimate of the effects of these forces can be included and the agreement with the true solution improved by averaging the two separate solutions for the partials.

Computational Logic:



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2.4.1.2.1 Subroutine TRANS

Purpose:

TRANS computes the matrix of partial derivatives of the state vector at an arbitrary point on a conic trajectory with respect to the state vector at another epoch. The variables utilized in this analysis are well defined for all conic motion.

Deck Name:

TRAN

Calling Sequence:

Call TRANS (R, V, T, PHI)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
ı	R	ř	3	ARG	radius vector in cartesian coordinates at T = o (Km)
I	٧	ν̈́	3	ARG	velocity vector in cartesian coordinates at T = o (Km/sec)
I	T	Δt	1	ARG	time at which partials are desired (relative to point 1)
0	PHI	%(t ₂ ,t ₁)	6 x 6	ARG	matrix $\frac{\partial \bar{\chi}_2}{\partial \bar{\chi}}$
I	GM	щ	1	con(6)	gravitational constant

Subroutines required:

SEARCH

(solve analog of Kepler's equation for position as a function of time)

Functions required:

AMAG (vector magnitude) DOT (dot product) SQRT (square root) COS SIN COSH (hyperbolic sine) SINH (hyperbolic cosine) $(\bar{\delta}_{ij} = 0 \ i \neq j$ DERAQ i = j= 1

Approximate Deck Length: 820 (decimal)

Formulation:

The equations of conic motion in terms of the co-colled universal variables of Dr. S. Herrick will be utilized to develop the partial derivatives of the components of position and velocity at any given time (on the conic section) relative to the components of position and velocity at some other arbitrary epoch. This task will be performed utilizing a formulation valid for a non-rotating coordinate system and will be based on the development presented in the discussion of the reference trajectory. The required expressions for this analysis are:

$$\vec{r} = f \vec{r}_0 + q \vec{s}_0$$

$$\vec{s} = f \vec{r}_0 + q \vec{s}_0$$

where
$$f = 1 - \hat{c}/r_o$$

$$\dot{q} = 1 - \hat{c}/r$$

 $\hat{\mathbf{r}}$ = inertial position vector = $\mathbf{x} \hat{\mathbf{x}}^* + \mathbf{y} \hat{\mathbf{y}} + \mathbf{z} \hat{\mathbf{z}}$

 \hat{s} = normalized velocity vector = $\vec{v}/\sqrt{u} = \dot{x} \hat{x}^* + \dot{y} \hat{y} + \dot{z} \hat{z}$

 $\hat{\chi}^*$ is the X unit vector. This notation is adopted to avoid confusion with a variable to be defined subsequently.

$$\hat{c} = \alpha (1 - \cos x)$$

$$\hat{U} = \alpha^{3/2} (x - \sin x)$$

$$\hat{S} = a^{\frac{1}{2}} (\sin x)$$

$$a = -\frac{1}{\alpha}$$

$$D_o = \vec{r}_o \cdot \vec{s}_o$$

$$\chi = E - E_0$$
 (elliptic motion)

$$x = F - F_0$$
 (hyperbolic motion)
 $\hat{x} = a^{\frac{1}{2}}x$

The first step in obtaining the desired partial derivatives involves differentiation of the equations for \hat{r} and \hat{s} with respect to the components of \hat{r}_0 and \hat{s}_0 . This task will be drastically simplified if full advantage is taken of the similar form of these derivatives at the outset. Thus, a shorthand notation will be adopted in that u and v (\hat{u} and \hat{v}) can assume the values of s, y, and z (\hat{x} , \hat{y} , and \hat{z})

$$\frac{\partial U}{\partial V_{o}} = \hat{f} \delta_{UV} + U_{o} \frac{\partial f}{\partial V_{o}} + \hat{U}_{o} \frac{\partial g}{\partial V_{o}}$$

$$\frac{\partial U}{\partial V} = g \delta_{UV} + U_{o} \frac{\partial f}{\partial \dot{V}_{o}} + \hat{U}_{o} \frac{\partial g}{\partial \dot{V}_{o}}$$

$$\frac{\partial \dot{U}}{\partial V_{o}} = \hat{f} \delta_{UV} + U_{o} \frac{\partial \dot{f}}{\partial \dot{V}_{o}} + \hat{U}_{o} \frac{\partial \dot{g}}{\partial \dot{V}_{o}}$$

$$\frac{\partial \dot{U}}{\partial V_{o}} = \hat{g} \delta_{UV} + \frac{U_{o} \partial \dot{f}}{\partial \dot{V}_{o}} + U_{o} \frac{\partial \dot{g}}{\partial \dot{V}_{o}}$$

where
$$\delta_{uv} = 0$$
 $u \neq v$

Thus, the problem has reduced itself to one of obtaining the derivatives of f, g, f and g with respect to r and s. This task will in turn be simplified if a set of intermediate parameters is selected, since the x...s do not appear explicitly in the equations for f...g. The set to be utilized is suggested by the equation for the magnitude of r in this set of variables.

$$r * r_0 + D_0 \hat{s} + (1 + r_0 \alpha) \hat{c}$$

= $F(r_0, D_0, \alpha)$

Having selected the intermediate variables the next task is the differentiation of f, g, \dot{f} and \dot{g} .

For f
$$\frac{\partial f}{\partial r_0} = \frac{-r_0}{r_0} \frac{\partial \hat{c}}{\partial r_0} r \hat{c}$$

$$\frac{\partial f}{\partial D} = \frac{-1}{r_0} \frac{\partial \hat{c}}{\partial D}$$

For g
$$\frac{\partial g}{\partial r_0} = \frac{-i}{\partial r_0} - \frac{\partial \hat{C}}{\partial r_0}$$
For g
$$\frac{\partial g}{\partial r_0} = \frac{\partial \tau}{\partial r_0} - \frac{\partial \hat{U}}{\partial r_0}$$

$$\frac{\partial g}{\partial D_0} = \frac{\partial \tau}{\partial D_0} - \frac{\partial \hat{U}}{\partial D_0}$$

$$\frac{\partial g}{\partial \alpha} = \frac{\partial \tau}{\partial \alpha} - \frac{\partial \hat{U}}{\partial \alpha}$$
For f
$$\frac{\partial \dot{f}}{\partial r_0} = \frac{-(rr_0)}{r^2} \frac{\partial \hat{S}}{\partial r_0} + S(r + r_0 \frac{\partial r}{\partial r_0})$$

$$\frac{\partial \dot{f}}{\partial D_0} = \frac{-(rr_0)}{r^2} \frac{\partial \hat{S}}{\partial D_0} + \hat{S}(r_0 \frac{\partial r}{\partial D_0})$$

$$\frac{\partial \dot{f}}{\partial \alpha} = \frac{-(rr_0)}{r^2} \frac{\partial \hat{S}}{\partial \alpha} + \hat{S}(r_0 \frac{\partial r}{\partial \alpha})$$
and for g
$$\frac{\partial \dot{g}}{\partial r_0} = \frac{-r \frac{\partial \hat{C}}{\partial r_0} + \hat{C} \frac{\partial r}{\partial r_0}}{r^2}$$

and for g
$$\frac{\partial \dot{q}}{\partial r_0} = \frac{-r \frac{\partial \hat{c}}{\partial r_0} + \hat{c} \frac{\partial r}{\partial r_0}}{r^2}$$

$$\frac{\partial \dot{q}}{\partial D_0} = \frac{-r \frac{\partial \hat{c}}{\partial D_0} + \hat{c} \frac{\partial r}{\partial D_0}}{r^2}$$

$$\frac{\partial \dot{q}}{\partial D_0} = \frac{-r \frac{\partial \hat{c}}{\partial D_0} + \hat{c} \frac{\partial r}{\partial D_0}}{r^2}$$

Now attention turns to the derivatives of \hat{C} , \hat{S} , \hat{U} , Υ etc. with respect to r_0 , p_0 , \propto .

for
$$\hat{C}$$

$$\frac{\partial \hat{C}}{\partial r_0} = \alpha \sin x \frac{\partial x}{\partial r_0} = \hat{S} \frac{\partial \hat{X}}{\partial r_0}$$

$$\frac{\partial \hat{C}}{\partial D_0} = \hat{S} \frac{\partial \hat{X}}{\partial D_0}$$

$$\frac{\partial \hat{C}}{\partial \alpha} = \hat{S} \frac{\partial \hat{X}}{\partial \alpha} + (1 - \cos x) \frac{\partial \alpha}{\partial \alpha} = \hat{S} \frac{\partial \hat{X}}{\partial \alpha} + \hat{C}\alpha$$
for $\hat{U} \frac{\partial \hat{U}}{\partial r_0} = \alpha^{\frac{1}{2}} (1 - \cos x) \frac{\partial x}{\partial r_0} = \hat{C} \frac{\partial \hat{X}}{\partial r_0}$

$$\frac{\partial \hat{U}}{\partial D_0} = \hat{C} \frac{\partial \hat{x}}{\partial D_0}$$

$$\frac{\partial \hat{U}}{\partial \alpha} = \hat{C} \frac{\partial \hat{x}}{\partial \alpha} + \frac{3}{2} (x - \sin x) \alpha^{\frac{1}{2}} \frac{\partial \alpha}{\partial \alpha}$$

$$= \hat{C} \frac{\partial \hat{x}}{\partial \alpha} + \frac{3}{2} \hat{U} \alpha$$

$$for \hat{S}$$

$$\frac{\partial \hat{S}}{\partial r_0} = \cos x \frac{\partial \hat{x}}{\partial r_0}$$

$$\frac{\partial \hat{S}}{\partial \alpha} = \cos x \frac{\partial \hat{x}}{\partial D_0}$$

$$\frac{\partial \hat{S}}{\partial \alpha} = \cos x \frac{\partial \hat{x}}{\partial D_0} + \frac{1}{2} \sin x \alpha^{\frac{3}{2}}$$

$$for T$$

$$\frac{\partial \gamma}{\partial r_0} = 0$$

$$\frac{\partial \gamma}{\partial r_0} = 0$$

$$\frac{\partial \gamma}{\partial r_0} = |+||D_0|| \frac{\partial \hat{S}}{\partial r_0} + C_0|| \frac{\partial \hat{C}}{\partial r_0} + \alpha \hat{C}$$

$$\frac{\partial r}{\partial D_0} = \hat{S} + D_0 \frac{\partial \hat{S}}{\partial D_0} + C_0 \frac{\partial \hat{C}}{\partial D_0}$$

$$\frac{\partial r}{\partial r_0} = D_0 \frac{\partial \hat{S}}{\partial r_0} + C_0 \frac{\partial \hat{C}}{\partial r_0} + r_0 \hat{C} = r_0$$

The final set of partials required is now recognized to be that of with respect to r_{O} , and D_{O} , and α . This set requires the equation for time (analogous to Kepler's equation) be differentiated as follows:

$$\sqrt{a} \ t = T = r_0 \hat{x} + D_0 \hat{c} + (1 + \alpha r_0) \hat{U}$$
for $\frac{\partial \hat{x}}{\partial r_0}$

$$o = \hat{x} + r_0 \frac{\partial \hat{x}}{\partial r_0} + D_0 \frac{\partial \hat{c}}{\partial r_0} + \alpha \hat{U} + (1 + \alpha r_0) \frac{\partial \hat{U}}{\partial r_0}$$

$$= \hat{x} + \alpha \hat{U} + r \frac{\partial \hat{x}}{\partial r_0}$$

$$\frac{\partial \hat{x}}{\partial r_{o}} = -\frac{\hat{s}}{r}$$
for $0 = r_{o} \frac{\partial \hat{x}}{\partial D_{o}} + \hat{C} + D_{o} \frac{\partial \hat{c}}{\partial D_{o}} + C_{o} \frac{\partial \hat{U}}{\partial D_{o}}$

$$\frac{\partial \hat{x}}{\partial D_{o}} = -\frac{\hat{c}}{r}$$
for $\frac{\partial \hat{x}}{\partial c!} = \frac{1}{2} a \gamma = r_{o} \frac{\partial \hat{x}}{\partial \alpha} + D_{o} \frac{\partial \hat{c}}{\partial \alpha} + C_{o} \frac{\partial \hat{U}}{\partial \alpha} + \hat{U}r_{o}$

$$= \hat{U}(r_{o} + \sqrt[3]{2} c_{o} a) + D_{o}(\hat{c} a) + \frac{\partial \hat{x}}{\partial \alpha}(r)$$

$$\frac{\partial \hat{x}}{\partial \alpha} = -\frac{1}{r} \left[\hat{u}(C_{o} a + r_{o}) + \frac{a}{2} \left(D_{o} \hat{c} - r_{o} \hat{x}\right) \right] = -\frac{x_{\alpha}}{r}$$

Now, substituting back into the previous expressions and collecting terms, the derivatives required to compute the partials of f, g, f, g, with respect to the intermediate parameters are:

For
$$\hat{\mathbf{c}}$$
 $\frac{\partial \hat{c}}{\partial r_o} = -\frac{\hat{\mathbf{s}}^2}{r}$

$$\frac{\partial \hat{c}}{\partial D_o} = -\frac{\hat{\mathbf{s}}\hat{c}}{r}$$

$$\frac{\partial \hat{c}}{\partial \alpha} = -\frac{\hat{\mathbf{s}}}{r} \cdot \mathbf{x} + \hat{c}_o = C_o \mathbf{x}$$

$$\frac{\partial \hat{c}}{\partial r_o} = -\frac{\hat{c}}{r} \cdot \hat{\mathbf{s}}$$

$$\frac{\partial \hat{U}}{\partial D_o} = -\frac{\hat{c}^2}{r}$$

$$\frac{\partial \hat{U}}{\partial D_o} = -\frac{\hat{c}^2}{r}$$

$$\frac{\partial \hat{S}}{\partial r_o} = -\cos \mathbf{x} \cdot \frac{\hat{S}}{r}$$

$$\frac{\partial \hat{S}}{\partial D_o} = -\cos \mathbf{x} \cdot \frac{\hat{c}}{r}$$

$$\frac{\partial \hat{S}}{\partial D_o} = -\cos \mathbf{x} \cdot \frac{\hat{c}}{r}$$

$$\frac{\partial \hat{S}}{\partial D_o} = \cos \mathbf{x} \cdot \mathbf{x} \cdot \frac{1}{2} \sin \mathbf{x} \cdot \mathbf{a}^{\frac{1}{2}} = S_o$$

for
$$r = \frac{\partial r}{\partial r_o} = 1 + D_o \left(-\cos \chi \frac{\hat{s}}{r} \right) + C_o \left(-\frac{\hat{s}^2}{r} \right) + \alpha \hat{c} = \frac{r_o}{r} f$$

$$\frac{\partial r}{\partial D_o} = \hat{s} + D_o \left(-\cos \chi \frac{\hat{c}}{r} \right) + C_o \left(-\frac{\hat{s}\hat{c}}{r} \right) = \frac{1}{r} g$$

$$\frac{\partial r}{\partial C} = D_r S_{\alpha} + C_o C_{\alpha} + r_o \hat{c} = r_{\alpha}$$

Finally, the required partials of f, g, f, and g, with respect to r_0 , p_0 , and q are:

For
$$\hat{f} = \frac{\partial f}{\partial r_0} = \frac{\hat{C}}{r_0^2} + \frac{\hat{S}^2}{rr_0}$$

$$\frac{\partial f}{\partial D_0} = \frac{\hat{S}\hat{C}}{rr_0}$$

$$\frac{\partial f}{\partial r_0} = \frac{\hat{S}\hat{C}}{rr_0}$$

$$\frac{\partial f}{\partial \alpha} = -\frac{1}{r_o} C_{\alpha}$$

for
$$\frac{\partial q}{\partial r} = \frac{\hat{S}\hat{C}}{r}$$

$$\frac{\partial q}{\partial D} = \frac{\hat{C}^2}{r}$$

$$\frac{\partial q}{\partial \alpha} = \frac{1}{2} \alpha \left[\gamma - 3 \hat{U} \right] + \frac{\hat{c}}{r} x_{\alpha}$$

$$\frac{\partial \dot{f}}{\partial r_0} = \frac{\hat{S}}{r^3 r_0^2} \left[r^2 + r_0 \left(r \cos x + r_0 f \right) \right]$$

$$\frac{\partial \dot{f}}{\partial D_0} = \frac{1}{r^3 r_0} \left[\hat{s} q + \cos x r \hat{c} \right]$$

$$\frac{\partial \dot{f}}{\partial \alpha} = \frac{1}{r r_o} S_{\alpha} + \frac{\hat{S}}{r^2 r_o} r_{\alpha}$$

$$\frac{\hat{\mathbf{g}}_{-1}}{\hat{\partial}_{0}^{2}} = \frac{1}{r^{3}} \left[r \hat{\mathbf{g}}^{2} + \hat{\mathbf{c}} r_{0} f \right]$$

$$\frac{\partial \dot{q}}{\partial D_0} = \frac{\hat{C}}{r^3} [r\hat{S} + q]$$

$$\frac{\partial \dot{q}}{\partial \alpha} = -\frac{rC_{\alpha} + \hat{C}r_{\alpha}}{r^2}$$

The only remaining steps at this point are thus to provide the derivatives of the intermediate set of parameters with respect to the components of \vec{r}_0 , and \vec{s}_0 , to construct the derivatives of f, g, f and g with respect to \vec{r}_0 and \vec{s}_0 , and to relate the results to the parameters \vec{r} and \vec{v} . The first step is accomplished by referring to the definitions of r_0 , p_0 , and

$$r_{o}^{2} = \sum_{i=1}^{3} \chi_{i}^{2} ; \qquad S_{o}^{2} = \sum_{i=1}^{3} S_{i}^{2}$$

$$\frac{\partial r_{o}}{\partial \chi_{i}} = \frac{\chi_{i}}{r_{o}} ; \qquad \frac{\partial r_{o}}{\partial S_{i}} = 0$$

$$D_{o} = \overline{r_{o}} \cdot \overline{S_{o}}$$

$$\frac{\partial D_{o}}{\partial \chi_{i}} = S_{i} ; \qquad \frac{\partial D_{o}}{\partial S_{i}} = \chi_{i}$$

$$\alpha = \overline{S} \cdot \overline{S} - \frac{2}{r_{o}}$$

$$\frac{\partial \alpha}{\partial \chi_{i}} = \frac{2\chi_{i}}{r_{o}^{3}} ; \qquad \frac{\partial \alpha}{\partial S_{i}} = S_{i}$$

The second step is accomplished through the medium of the chain rule, i.e.,

$$\frac{\partial f}{\partial z_i} = \frac{\partial f}{\partial r_o} \quad \frac{\partial r_o}{\partial x_i} + \frac{\partial f}{\partial D_o} \quad \frac{\partial D_o}{\partial x_i} + \frac{\partial f}{\partial \alpha} \quad \frac{\partial \alpha}{\partial x_i}$$

etc.

and the third and final step is employed to remove the normalization factor applied to the components of the velocity. Since

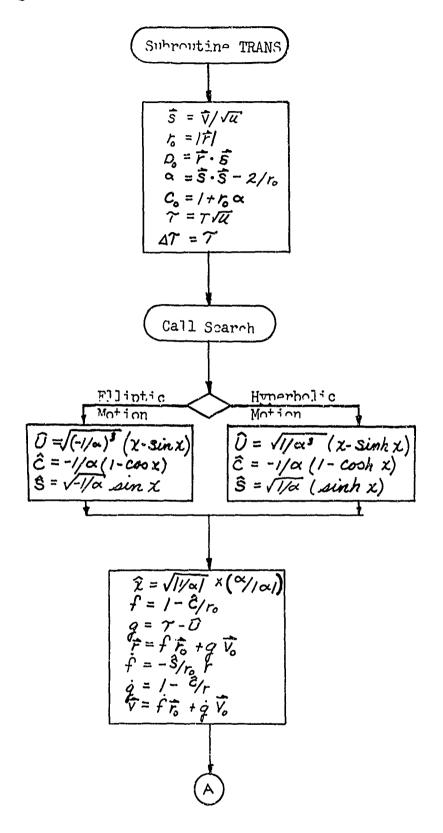
$$\vec{\hat{s}} = \sqrt{\frac{1}{\mu}}$$

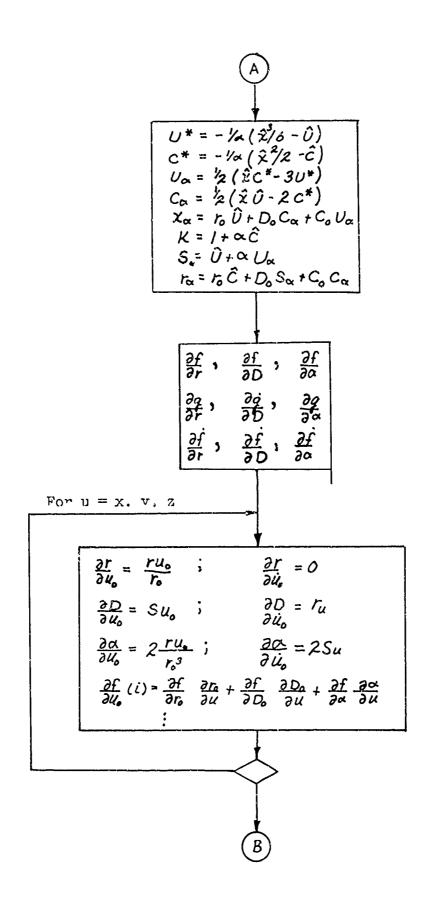
$$d\vec{\hat{s}} = \sqrt{\frac{1}{\mu}} d\vec{\hat{v}} ,$$

the desired matrix is

$$\begin{cases}
d\vec{r} \\
d\vec{v}
\end{cases}
\begin{bmatrix}
\frac{\partial \vec{r}}{\partial \vec{r}_{0}} & \frac{1}{\sqrt{2}} & \frac{\partial \vec{r}}{\partial \vec{s}_{0}} \\
-\frac{1}{\sqrt{2}} & \frac{\partial \vec{r}}{\partial \vec{s}_{0}} & \frac{\partial \vec{s}}{\partial \vec{s}_{0}}
\end{bmatrix}
\begin{cases}
d\vec{r}_{0} \\
\vec{v}_{0}
\end{cases}$$

Computational Logic:





 $\mathcal{P}(i,J) = r_0(i) \frac{\partial f}{\partial u_i}(J) + S_0(i) \frac{\partial g}{\partial u_i}(J) + S_{ij} F$ $\varphi(i, J+3)=(r_o(i)\frac{\partial f}{\partial u_o}(J)+S_o(i)\frac{\partial g}{\partial u_o}(J)+S_{ij}q)/\sqrt{u}$ $\varphi(i+3,\mathcal{I})=(r_o(i)\frac{\partial \dot{f}}{\partial u_o}(\mathcal{I})+S_o(i)\frac{\partial \dot{g}}{\partial u_o}(\mathcal{I})+S_{ij}\dot{f})\sqrt{u}$ $\varphi(i+3,J+3)=r_0(i)\frac{\partial \dot{f}}{\partial \dot{u}_0}(J)+S_0(i)\frac{\partial \dot{g}}{\partial \dot{u}_0}(J)+8$ Nailmda

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2.4.1.2.2 Subroutine INVAO

Purpose:

to produce the analytic inverse of the 6 X 6 matrix of partial derivatives referred to as the state transition matrix (i.e., the matrix $\begin{bmatrix} \frac{\partial x}{\partial x} \end{bmatrix}$ where all vectors are expressed in cartesian coordinates)

Deck Name:

INVA

Calling Sequence:

Call INVAO (AO, AOI)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
Ι	АО	Ψ(<i>ċ,ċ</i> _°)	6 X 6	ARG	the matrix of partial derivatives of the state vector (x) at "t" with respect to the state vector at "to"
0	AOI	φ ⁻¹ (t,t _o) or ψ (t _o ,t)	6 X 6	ARG	the analytically in- verted matrix

Subroutine required:

None

Functions required:

None

Approximate Deck

Length:

160 (octal)

Formulation:

Consider a linear system (expressed in cartesian coordinates) described by the following equation

$$\dot{\vec{X}} = A(t) \ \vec{X}(t) + B(t) \ \vec{F}(t) \tag{1}$$

where $\overline{X}(t)$ is an even-ordered state vector composed of a set of output variables and their derivatives

F(t) is a forcing function (= 0 for the analysis to follow)
A(t) is a coefficient array for the system composed of square, synathes, even-ordered subarrays of the following form

$$A(t) = \begin{bmatrix} o & A_{12} \\ A_{21} & O \end{bmatrix}$$

$$A_{12} = I$$
(2)

$$A_{21} = \frac{2\vec{q}}{2\vec{r}} = \frac{u}{r^3} \left[\Gamma - \frac{3\vec{r} \cdot \vec{r}}{r^2} \right]$$

B(t) is an array relating the sensitivity of the system to the forcing function

and the solution for $\overline{F} = 0$

$$\vec{X}(t) = \varphi(t, t_o) \quad \vec{X}(t_o) = \begin{bmatrix} \varphi_{ii} & \varphi_{i2} \\ -\varphi_{2i} & \varphi_{22} \end{bmatrix} \vec{X}(t_o)$$
(3)

If equations 2 and 3 are substituted back into equation 1, the following identity results

$$\begin{bmatrix} \dot{\varphi}_{1} & \dot{\varphi}_{12} \\ \dot{\varphi}_{21} & \dot{\varphi}_{22} \end{bmatrix} = \begin{bmatrix} O & I \\ \frac{\partial \vec{q}}{\partial F} & O \end{bmatrix} \begin{bmatrix} \dot{\varphi}_{11} & \dot{\varphi}_{12} \\ \dot{\varphi}_{21} & \dot{\varphi}_{22} \end{bmatrix} \tag{4}$$

and equation 4 yields upon expansion

$$\dot{\mathcal{G}}_{II} = \mathcal{G}_{ZI} \tag{5a}$$

$$\dot{\mathcal{G}}_{12} = \mathcal{G}_{22} \tag{5b}$$

$$\dot{\varphi}_{2l} = \frac{\partial \bar{\varphi}}{\partial r} \, \, \varphi_{ll} \tag{5c}$$

$$\dot{\varphi}_{R2} = \frac{\partial \bar{q}}{\partial r} \, \, \varphi_{r2} \tag{5d}$$

Equations 5 may now be operated on to produce an equivalent set of differential equations. This operation is performed as follows:

$$\begin{aligned} \varphi_{2l}^T \dot{\varphi}_{ll} &= \varphi_{2l}^T \varphi_{2l} \\ \dot{\varphi}_{2l}^T \varphi_{ll} &= \varphi_{ll}^T \frac{\partial \vec{q}}{\partial \vec{r}} \varphi_{ll} &= \varphi_{ll}^T \frac{\partial \vec{q}}{\partial \vec{r}} \varphi_{ll} \end{aligned}$$

$$Q_{11}^T \dot{Q}_{21} = Q_{11}^T \frac{\partial \vec{q}}{\partial \vec{r}} Q_{11}^T$$

$$\dot{\varphi}_{11}^{T} \varphi_{21} = \varphi_{21}^{T} \varphi_{21}$$

or

$$\frac{d}{dt} \left(\mathcal{Q}_{2l}^T \mathcal{Q}_{ll} - \mathcal{Q}_{ll}^T \mathcal{Q}_{ll} \right) = 0$$

$$\varphi_{\mathbf{z}_{1}}^{T} \varphi_{1} - \varphi_{11}^{T} \varphi_{1} = C_{1} \tag{6a}$$

similarly

$$\mathcal{L}_{22} \mathcal{L}_{11} - \mathcal{L}_{12} \mathcal{L}_{21} = C_2$$
(6b)

$$\varphi_{22}^{T} \varphi_{12}^{-} - \varphi_{12}^{T} \varphi_{22}^{-} = C_{3}$$
 (6c)

$$Q_{11}^T Q_{22} - Q_{21}^T Q_{12} = C_{41}$$
 (6d)

Finally, the results of the integration can be restated in matrix notation as

$$\begin{bmatrix} \varphi_{22}^T & -\varphi_{12}^T \\ -\varphi_{22}^T & \varphi_{11}^T \end{bmatrix} \begin{bmatrix} \varphi_{11} & \varphi_{12} \\ \varphi_{21} & \varphi_{22} \end{bmatrix} = \begin{bmatrix} C_2 & C_3 \\ -C_1 & C_4 \end{bmatrix}$$
(7)

and the constant arrays resulting from these integrations may now be evaluated by substituting the initial conditions

$$\varphi_{\mu}(o) = \varphi_{22}(o) = I$$

This step produces

and reduces equation 7 to the identity matrix. But, the only matrix which can be utilized to reduce an arbitrary square matrix to I is its inverse. Thus

$$\varphi^{-1}(t,t_o) = \begin{bmatrix} \varphi_{22}^T & -\varphi_{2}^T \\ -\varphi_{21}^T & \varphi_{1}^T \end{bmatrix} \tag{8}$$

Equation 8 is important for general linear systems in that it provides an analytic means of constructing the inverse transition matrix directly from the elements of the known transition matrix by rearrangement of terms and the change of a few signs. It will be utilized in this program in conjunction with a correction to the basic conic transition matrix descirbed in STEAT.

In conclusion, it is noted that the true meaning of the terms A₁₂ and A₂₁ (equation 2) was never employed, and only symmetry is required. Thus, there is an immediate generalization providing that an arbitrary system can be described by equation 2. It is also noted that another approach to the derivation is suggested in Ref. 1, along with a discussion of several related problems.

References

1) Friedlander, A. I., "Inversion Property of the Fundamental Matrix in Trajectory Perturbation Problems." AIAA Journal, Vol. 1, No. 4, pages 771-973(April 1763)

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2.4.1.3 Subroutine MEASUR

Purpose:

To construct the matrix of partial derivatives of the observables with respect to the state vector (i.e., $M = \frac{\lambda T}{\lambda X}$) where the observables may be

1) range

2) range rate

3) azimuth and elevation

4) range and range rate
5) range, aximuth and elevation
6) range rate, aximuth and elevation

Deck Name:

OBSN

Calling Sequence:

CALL MEASUR (M)

Input/Output:

I/0	FORTRAN	Math	70.	Common/	D
1/0	Name	Name	Dimension	Argument	Description
I	ITYPE	-	1	WRK(64)	Fixed point number which identifies the type of data being processed and hence, the type of matrix desired.
I	RVEC	r	3	WRK(lll)	Radius vector in frame of date
I	VVEC	\vec{v}	3	WRK(114)	Velocity vector in frame of date
I	RTRAK	$\vec{\mathbf{r}}_{t}$	3	WRK(95)	Radius vector of tracking station in frame of date
I	X (Y,Z)	U (E,N)	3 (3,3)	WRK(108) WRK(124) WRK(127)	Up (east, north) unit vectors at the tracking station
0	M	-	1	ARG	Fixed point integer which identifies the number of pieces of data in the observation vector (1, 2 or 3)

I/u	FORTRAN Name	liath liao	Dimension	Common/ Argument	Definition
O	CB3/n	m }:-	/ II 3	STT (37)	array of partial beri- vatives of the obser- vations with respect to the state vector
I	OI ETGA	И	1	CON (7)	spin rate of the carth

Subroutines required:

CROSS (cross product)

Functions required:

ANAG (vector magnitude)

DOT (dot product)

SCRT (square root)

Approximate Deck

Formulation:

Length:

Partials for range, range rate, azimuth and elevation with respect to the state vector can be obtained from the following equations:

350

(decimal)

$$R = (\vec{r}_{r} \cdot \vec{r}_{r})^{V_{2}}$$

$$\dot{R} = (\hat{r}_{r} \cdot \vec{V}_{r})$$

$$A_{x} = tan^{-1} \left(\frac{\vec{r}_{r} \cdot \vec{E}}{\vec{r}_{r} \cdot \hat{N}} \right)$$

$$EL = ain^{-1} (\hat{r}_{r} \cdot \hat{N})$$

$$\vec{X} = \vec{r} - \vec{r}_{n}$$

$$\vec{r}_{r} = \vec{r} - \vec{r}_{T}$$

$$\hat{r}_{r} = \vec{v} - \vec{v}_{r}$$

where:

R = range

R = range rate

 $\Lambda_3 = azimuth$

EL = clevation

 $\hat{U},\hat{E},\hat{N} = up$, east, north unit vectors

 \vec{r} = vehicles position in equatorial frame of date

1

 \vec{r}_n = nominal position on reference orbit

 $\vec{r_T}$ = tracking stations position vector

when it is noted that for the purpose of differentiation, the nominal position vector and the tracking station position vector are constant, i.e.,

$$d\vec{x} = d\vec{r}_r$$
.

This set of operations has been performed, and the results of the analysis are presented below:

1) Partials of range

$$R^2 = X_r^2 + Y_r^2 + Z_r^2$$

$$\frac{\partial R}{\partial x} = \left(\frac{\partial R}{\partial r}, \frac{\partial R}{\partial v}\right) = \left(\frac{X_r}{R}, \frac{X_r}{R}, \frac{Z_r}{R}, 0, 0, 0\right)$$

2) Partials of range-rate

$$\dot{R} = \frac{\dot{x}_{r}}{\dot{R}} \dot{X}_{r} + \frac{\dot{y}_{r}}{\dot{R}} \dot{y}_{r} + \frac{\dot{z}_{r}}{\dot{R}} \dot{Z}_{r}$$

$$\frac{\partial \dot{R}}{\partial \dot{X}} = \left(\frac{\partial \dot{R}}{\partial \dot{r}}, \frac{\partial \dot{R}}{\partial \dot{V}}\right) = \left(\frac{\dot{X}_{r}}{R} - \frac{\dot{R}\dot{X}_{r}}{R^{2}}, \frac{\dot{Y}_{r}}{R} - \frac{\dot{R}\dot{X}_{r}}{R^{2}}, \frac{\dot{Y}_{r}}{R}, \frac{\ddot{Z}_{r}}{R}\right)$$

$$\frac{\dot{Z}_{r}}{R} - \frac{\dot{R}\dot{Z}_{r}}{R^{2}}, \frac{\dot{X}_{r}}{R}, \frac{\dot{Y}_{r}}{R}, \frac{\ddot{Z}_{r}}{R}\right)$$

3) Partials of Azimuth

$$S^{2} = (\vec{r}_{r} \cdot \hat{E})^{2} + (\vec{r}_{r} \cdot \hat{N})^{2}$$

$$\frac{\partial A_{3}}{\partial \vec{x}} = (\frac{\partial A_{3}}{\partial \vec{r}}, \frac{\partial A_{3}}{\partial \vec{v}}) = \begin{bmatrix} E_{r}(\frac{\hat{N} \cdot \vec{r}_{r}}{s^{2}}) - N_{r}(\frac{\hat{E} \cdot \vec{r}_{r}}{s^{2}}) \\ -314- \end{bmatrix}$$

$$E_{2}\left(\frac{\hat{N}\cdot\vec{r_{r}}}{S^{2}}\right)-N_{2}\left(\frac{\hat{E}\cdot\vec{r_{r}}}{S^{2}}\right),$$

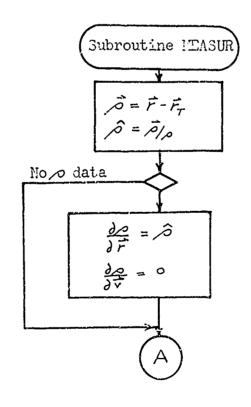
$$E_{3}\left(\frac{\hat{N}\cdot\vec{r_{r}}}{S^{2}}\right)-N_{3}\left(\frac{\hat{E}\cdot\vec{r_{r}}}{S^{2}}\right),$$

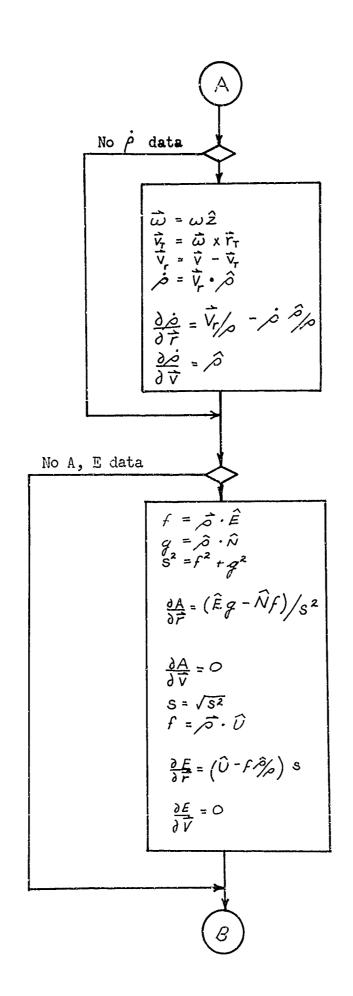
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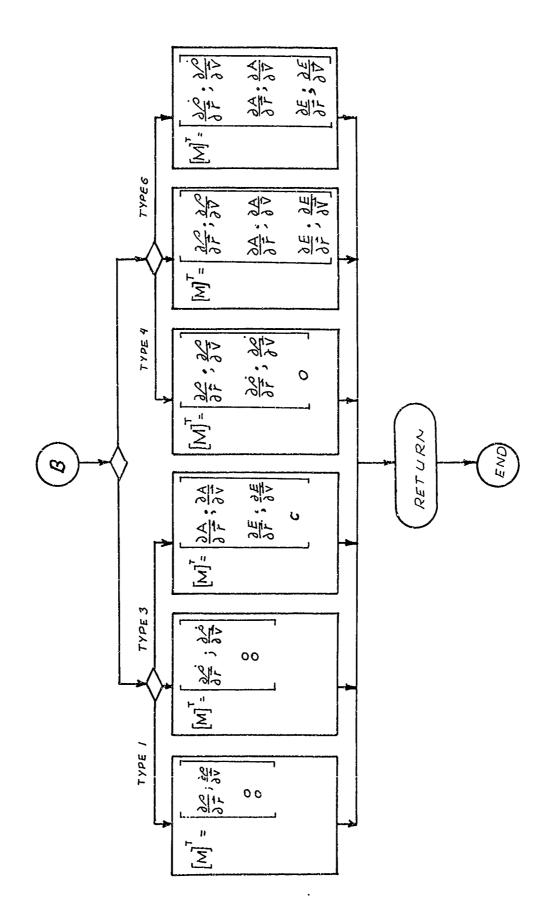
4) Partials of Elevation

$$\frac{\partial EI}{\partial \bar{X}} = \left(\frac{\partial EI}{\partial \bar{F}}, \frac{\partial EL}{\partial \bar{V}}\right) = \left[\frac{U_1}{S} - X_r \left(\frac{\hat{U} \cdot \bar{r}_r}{R^2 s}\right), \frac{U_2 - Y_r \left(\frac{\hat{U} \cdot \bar{r}_r}{R^2 s}\right),}{S}, \frac{U_3 - Z_r \left(\frac{\hat{U} \cdot \bar{r}_r}{R^2 s}\right),}{S}$$

Computational Logic:







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2.4.1.4 Subroutine ERROR

Purpose:

To compute the weighting matrix (Q) for the data point (one of 6 types) from uncertainty data provided pertaining to station locations errors and recording

instrument errors

Deck Name:

EROR

Calling Sequence:

CALL ERROR (NUMB, M)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Description
I	NUMB		1.	ARG	Number of the station - this number corresponds to the sequence established in INPUT (comes from TRAK)
I	М		1	ARG	Number of pieces of information included in the observation vector (from MEASUR)
I	RE	R _e	1	CON(1)	Earth's equatorial radius (Km)
I	RPOL	R _p	ı	CON(2)	Earth's polar radius (Km)
I	OMEGA	ω	ı	CON(7)	Earth's spin rate (rad/sec)
I	STERR	AL, AA, AH	3	SDA(51)	Variance and latitude, longitude and altitude for the station
I	SNOISE	σωρ, σώ, σωλ, σω	M	SDA(141)	Variances on the observed data for the equipment utilized
ı	OBST	M ^T (t)	6 X 3	STT(37)	Output of MEASUR
0	Q	Q (+)	3 X 3	STT(59)	Combined weighting matrix
I	ITYPE	-	1.	WRK(64)	Type of data being processed

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Description
I	SLAT	L	1	WRK(105)	Geodetic latitude of the station (rad)
I	SLON	λ	1	WRK(106)	Longitude of the station (rad)
I	Н	Н	1	WRK(107)	Altitude relative to reference ellipsoid (Km)
I	X (Y,Z)	U (E,N)	3 (3,3)	WRK(108)	Up (East, North) unit vector at station

Subroutines required:

MATMPY TRANSP (matrix multiplication)
(matrix transpose)

Functions required:

SIN

SQRT

Approximate Deck

Length:

627

(octal)

Formulation:

In order to construct the matrix of uncertainty required by the Kalman filter resulting from station position errors and errors in the observations, two assumptions are necessary. The first is that the groups of errors from the two sources under analysis are statistically independent, and the second is that the equations describing the processes are linear. Under these assumptions the resultant uncertainty matrix (Q) is

and attention can be directed to each source independently.

In order to define Q1, it is first necessary to consider the manner in which the specified set of errors affect the problem (consistent with the assumptions previously outlined). This relationship is

$$\Delta (oss) = \left[\frac{\partial (oss)}{\partial L, \lambda, H}\right] \left\{ \begin{array}{c} \Delta L \\ \Delta \lambda \\ \Delta H \end{array} \right\}$$

$$\equiv \begin{bmatrix} COEFF \end{bmatrix} \quad \begin{Bmatrix} \Delta L \\ \Delta \lambda \\ \Delta H \end{Bmatrix}$$

which leads directly to

where σ is specified.

The problem to which this analysis must address itself is thus the construction of the matrix [COEFF] . This development is simplified considerably, since the chain rule can be employed to produce the desired results as follows:

COEFF =
$$\begin{bmatrix} \frac{\partial}{\partial} (\overline{BS}) \end{bmatrix} \begin{bmatrix} \frac{\partial}{\partial X} \\ \frac{\partial}{\partial L} \\ \frac{\partial}{\partial L} \end{bmatrix} = M \begin{bmatrix} \frac{\partial}{\partial X} \\ \frac{\partial}{\partial L} \\ \frac{\partial}{\partial L} \end{bmatrix}$$

$$= \begin{bmatrix} OBS \end{bmatrix} \begin{bmatrix} DERIV \end{bmatrix}$$

where [OBS] T is the output of subroutine MEASUR and where \tilde{X} is the state vector. For this reason, subsequent analyses will be directed to the derivation of the matrix DERIV.

The first steps in relating uncertainties in the position and velocity of the tracking equipment and the corresponding uncertainty in the satellite's position and velocity are the definition of the observed quantities

$$\vec{r} = \vec{r} - \vec{r}$$

$$\vec{v} = \vec{v} - \vec{v}_r$$

where: the subscripts r and t denote relative and tracking station, respectively, and the description of a coordinate system in which the vectors will be defined (in this case the true equator of date frame).

$$\vec{F}_{\tau} = \left(\frac{R_{e}}{c} + H\right) \left\{ \cos L \cos A \hat{x} + \cos L \sin A \hat{Y} \right\}$$

$$+ \left(\frac{Ro^{2}}{R_{e}c} + H\right) \left\{ \sin L \hat{Z} \right\}$$

$$\vec{V}_{T} = \omega \left(\hat{Z} \times \vec{F}_{T}\right)$$

$$\vec{V}_{T} = \omega \left(\frac{R_{c}}{C} + H \right) \left[-\cos L \sin A \hat{x} + \cos L \cos A \hat{Y} \right]$$

$$= -\omega Y_{T} \hat{x} + \omega x_{T} \hat{Y} + O \hat{z}$$

where

R_e = equatorial radius of the oblate spheroid

 R_p = polar radius of the oblate spheroid c^2 = a function of latitude = $\cos^2 L + (R\rho/R_e)^2 \sin^2 L$

I, = geodetic latitude of the station

A = right ascension of the station

= longitude relative to Greenwich (λ) plus sidereal time of the Greenwich meridian

 $\omega = \text{spin rate of the earth}$

 $\hat{\hat{\mathbf{X}}}$ = unit vector toward the vernal equinox $\hat{\hat{\mathbf{Z}}}$ = unit vector along the spin vector of the earth

Now if the vehicle's position and velocity are held constant for the purposes of differentiation, the sensitivity of the state vector to errors in the tracking stations position and velocity can be obtained by computing the partials of the relative \bar{r} and \bar{v} with respect to errors in L, A, and H

$$\frac{\partial \vec{r}}{\partial u} = -\frac{\partial \vec{r}_r}{\partial u} \qquad \qquad U = L, A, H$$

$$\frac{\partial \vec{V}}{\partial u} = -\frac{\partial \vec{V}_r}{\partial u} \qquad \qquad U = L, A, H$$

However, before these derivatives are evaluated, it is noted that since right ascension can be expressed as

and since sidereal time is uncertain to a degree much less than that associated with λ , $dA \approx d\lambda$.

Now

$$\frac{\partial X_T}{\partial L} = -\left(\frac{Re}{C} + H\right) \sin L \cos A + \cos L \cos A\left(-\frac{Re}{C^2}\right) \frac{\partial C}{\partial L}$$

$$\frac{\partial X_T}{\partial \lambda} = -\left(\frac{Re}{C} + H\right) \cos L \sin A$$

$$\frac{\partial X_T}{\partial H} = \cos L \cos A$$

$$\frac{\partial Y_{\tau}}{\partial L} = -\left(\frac{Re}{C} + H\right) \sin L \sin A + \cos L \sin A \left(\frac{-Re}{C^{2}}\right) \frac{\partial C}{\partial L}$$

$$\frac{\partial Y_{\tau}}{\partial \lambda} = \left(\frac{Re}{C} + H\right) \cos L \cos A$$

$$\frac{\partial Y_{\tau}}{\partial H} = \cos L \sin A$$

$$\frac{\partial Z_{\tau}}{\partial L} = \left(\frac{R_{\rho}^{2}}{cRe} + H\right) \cos L + \left(\frac{-R_{\rho}^{2}}{ReC^{2}}\right) \frac{\partial C}{\partial L}$$

$$\frac{\partial Z_{\tau}}{\partial \lambda} = 0$$

$$\frac{\partial Z_{\tau}}{\partial H} = \sin L$$

$$\frac{d}{dH} = \sin L \cos L \left[\frac{-R_{\rho}^{2}}{Re}\right]^{2}$$

where

E FUNCT (in program language)

and

$$\frac{\partial \dot{X}_{T}}{\partial L} = -\omega \frac{\partial Y_{T}}{\partial L}$$

$$\frac{\partial \dot{X}_{T}}{\partial \lambda} = -\omega \frac{\partial Y_{T}}{\partial \lambda}$$

$$\frac{\partial \dot{X}_{T}}{\partial H} = -\omega \frac{\partial Y_{T}}{\partial H}$$

$$\frac{\partial \dot{Y}_{T}}{\partial L} = +\omega \frac{\partial X_{T}}{\partial L}$$

$$\frac{\partial \dot{Y}_{T}}{\partial \lambda} = +\omega \frac{\partial X_{T}}{\partial \lambda}$$

$$\frac{\partial \dot{Y}_{T}}{\partial H} = +\omega \frac{\partial X_{T}}{\partial H}$$

$$\frac{\partial \dot{Z}_{T}}{\partial H} = 0$$

$$\omega = L, \lambda, H$$

With the evaluation of DERIV, the array COEFF is known and Q_1 can be computed once data for the errors in the variables L, λ , and H are specified. Attention thus turns to the second source of errors to be considered; namely, those resulting from observational uncertainties. Assuming that the observation vector for this analysis is ordered in the same fashion

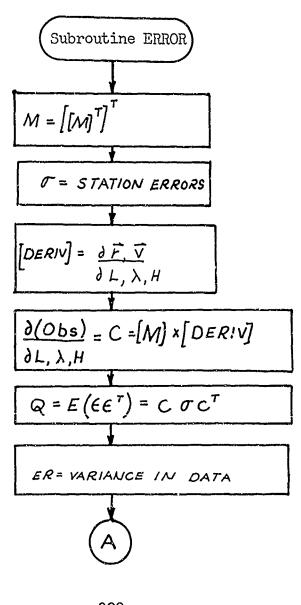
as for the previous analysis, Q_2 is by definition

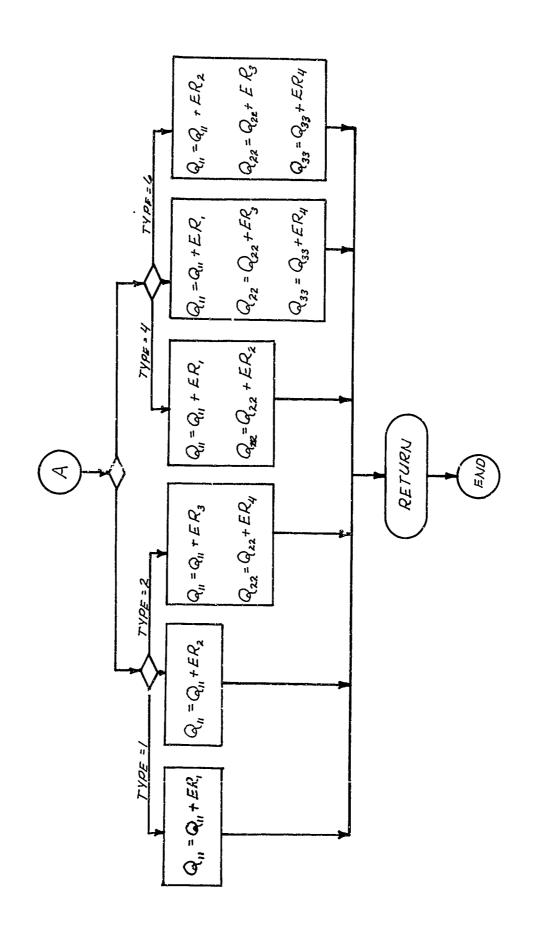
$$Q_2 = E(\epsilon \epsilon^{\tau})$$

and is provided as input data for each station.

For the present, both σ and \mathbb{Q}_2 have been assumed to be diagonal (i.e., the errors involved are uncorrelated); and provision has been made in subroutine INPUT to store only the variances. However, should station calibration and survey indicate that a significant degree of correlation exists between the elements internal to these arrays, other terms must be added. This step requires only the modification of INPUT and ERROR.

Computational Logic:





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STATION ALTITUDE RELATIVE TO ELLIPSGID IN UNITS OF RE, RPOLEROR0120 LOCATION INACCURACIES . IT THEN CONSTRUCTS THE COMPLETE COVARIANCE MATRIX * 0 * OF THE KALMAN FILTER BY ADDING UNIT VECTORS (UP, EAST, NORTH). WITH ORIGIN AT THE STATION THE STATION ERROR MATRIX TO THE COVARIANCE MATRIX FOR THIS ROUTINE IS DESIGNED TO COMPUTE THE COVARIANCE MATRIX FOR THE ERRORS IN THE OBSERVATION MAIRIX DUE TO STATION TRACKING STATION NUMBER (DEPENDS ON ARRANGEMENT OF LATITUDE, LONGITUDE, AND ALTITUDE DATA IN COMMON STA DATA TYPE (SEE ROUTINE MEASUR FOR OPTIONS) DIMENSION CON(1), SAT(1), SDA(1), WRK(1), STT(1) DIMENSIONALITY OF THE OBSERVATION VECTOR AT DATA(51) AND GCING UPTO DATA(92)) NOI SE IN THE MEASUREMENTS. STATION LONGITUDE IN RADIANS STATION LATITUDE IN RADIANS SUBROUTINE ERROR (NUMB, M) * * **₹** THE 35 ITYPE X, Y, Z SLAT SLON NUMB Σ

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EROR1120 EROR1130 EROR1140 EROR1150 EROR1160

EROR1180 EROR1190 EROR1200

EROR1210 ERDR1220 EROR1230 EROR1240

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N SOURCE STATEMENT - IFN(S) -
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### ERUR — EFN SOURCE STAN

GJ TO RO

50 Q(1,1) = FR(1) +Q(1,1)

Q(2,2) = FR(2) +Q(2,2)

GO TO RO

60 Q(1,1) = ER(1) +Q(1,1)

Q(2,2) = ER(3) +Q(2,2)

Q(2,2) = ER(4) +Q(3,3)

GJ TO RO

70 Q(1,1) = ER(2) +Q(3,3)

GJ TO RO

70 Q(1,1) = ER(4) +Q(3,3)

Q(2,2) = ER(4) +Q(3,3)

Q(2,2) = ER(4) +Q(3,3)

Q(2,2) = ER(4) +Q(3,3)

RO RETURN
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SUBROUTINE ERROR

COMMIUN VARIABLES

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LENGTH	Lication 00000 00435 00001 00756 00761 00125	L JCATIJN 01043 01102	LJCATION 01126 91131 01134
00001	SYMBOL CON STT RPJL SLAT X STERR	VAPIABLES SYMBJL ER CJEFT	VAŘÍABLES SYABÜL SLA CLA CIN
	F >	PROGRAM V TYPE R R	PRCCRAM V TYPE I R R R R
ORIGIN	LOCATION 00000 00043 00000 00705 01004 00501	DIMENSIONED LOCATION 01032 01071	UNDIMENSIONED LOCATION 01125 01133 01133 01133
//	SYMBOL DATA. SDA RE ITYPE H Z OBST	SYMBOL SIGMA COEFF	SYMBOL J. SLN AOC. FUNCT
COMMUN ULICK	► αααααα σ π	7 Y P F R R R R R	77 77 8 8 8 8
YUKWOO	LUCATIUN 1000 00017 0056 00757 01001 00257	LOCATION 61010 01047 01113	LUCAT FUN 01124 01127 01132 01135
	SYMBOL OATA SAT WRK OYEGA SLGN }	SYMBOL DERIV OBS DUMMY	SYMBOL I CLA C RATIO

ENTRY POINTS

ERRJR

SID 65 1203-1 -335-

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PAGE			SECTION			LOCA	012	015	015	1 1 1	
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	336		r- v)	<i>3</i> ,		N III	~	10	40	70	DECK

2.4.1.5 Subroutine UPSTAT

Purpose:

To determine if the uncertainties in the estimate of the state of the system are sufficiently small to justify updating the position (velocity) by adding the state vector to the position and velocity vectors on the nominal trajectory and to write the results of

the data reduction problem.

Deck Name:

UPST

Calling Sequence:

CALL UPSTAT

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Description
I/O	STATE	<u>Χ</u> (₹)	6	STT(64)	The state vector for the system (Km, Km/sec.)
I	P	P(t)	6 X 6	STT(70)	Covariance matrix for estimation errors in \overline{X} (+)
I	ROTINV	_	3 X 3	WRK(10)	Matrix relating coordinate frame of date to frame of 1950.0
0	RCONIC	\vec{r}_c, \vec{v}_c	3,3	WRK(28) WRK(31)	Position and velocity vectors for new conic reference trajectory (Km, Km/sec.)
0	TCONW TCONF	t _c	1,1	WRK(34) WRK(35)	Time in days at which rectification of reference conic occurred (days relative to 1950.0)
0	RTRANS VTRANS	\vec{r}_{o}, \vec{v}_{o}	3,3	WRK(36) WRK(39)	Position and velocity vectors in frame of date on true tra- jectory at data point just reduced (Km, Km/sec.)
0	TTRANW, TTRANF	tt	1,1	WRK(42) WRK(43)	Time from which errors will propagate for next pass through filter (days relative to 1950.0)

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Description							
I	TW, TF	t	1,1	WRK(50) WRK(51)	Whole and fractional part of the present day relative to the epoch of 1950.0 (J.D. 2433282.423)							
т/о	RDATE, VDATE	1r1v	3 3	WRK(111) WRK(114)	Position and velocity vectors in the frame of date (Km, Km/sec.)							
I	RE GM	R. GM	1	CON(1) CON(6)	Equatorial radius and gravitational constant for the Earth (Km, Km ³ /sec ²)							
I	NOUT	-	1	CON(14)	Output tape number							

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Subroutines required: MATMPY (matrix multiplication)
ELEMEN (computes conic elements)
Functions required: DOT (dot product)

Approximate Deck 704 (octal)
Length:

Discussion:

UPSTAT (Update State Vector) is designed to determine whether the uncertainty in the estimate of the state vector is sufficiently small to allow the trajectory to be discreetly changed by adding the state vector to the position and velocity vectors on the integrated trajectory. This test is made to assure that large uncertainties in the estimate early in time will not produce the degenerate solution which is possible if noisy estimates of the state are allowed to be introduced directly into the system along with the desired results of the filtering and corrections for the non-linear nature of the problem.

In order to produce this test, however, it is necessary to define a comparison function and specify a measure of error which is considered acceptable as a threshold for updating. This process, quite arbitrarily, has been performed as follows:

$$F = \sum_{i=1}^{3} \left[\left(\frac{\Delta r_i}{r} \right)^2 + \lambda \left(\frac{\Delta V_i}{V} \right)^2 \right]$$

and the weighting factor has been established so that the sensitivity of the semi-major axis to errors in radius and velocity for a circular orbit are equal, i.e.,

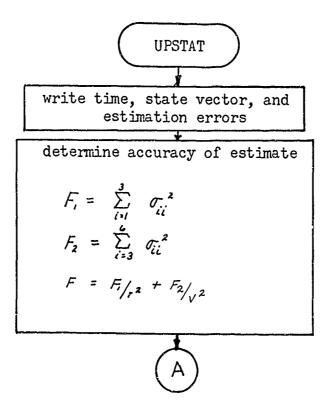
$$\frac{\Delta a_i}{a} = 2 \frac{a}{r} \frac{\Delta r}{r} = 2 \frac{\Delta r}{r}$$

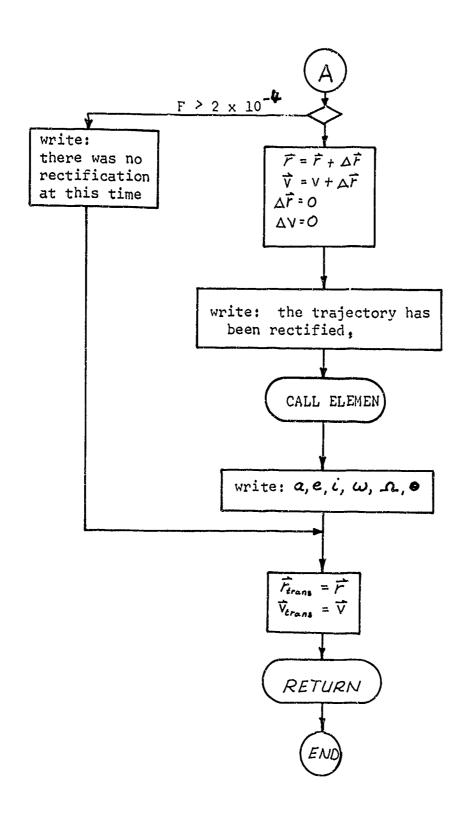
$$\frac{\Delta a_2}{a} = 2\left(2\frac{a}{r}-1\right)\frac{\Delta V}{V} = 2\frac{\Delta V}{V}$$

Thus, for this criteria, the two ratios in question should be weighted equally. That is, $\lambda = 1$. The threshold for this function has been set at 2×10^{-4} .

Upon entry into UPSTAT, the covariance matrix for the errors in the state vector is examined; and the elements along the principle diagonal (trace) are extracted and utilized as Δr_i (or ΔV_i) in the construction of the comparison function. The test is then made to determine whether updating will be accomplished; if not, the position and velocity vectors at this time are stored for future computation of the transition matrix, and control is returned to the calling routine. However, if updating is practical, it is performed, the conic reference trajectory is rectified, the state vector is zeroed, and the "classic" elements of the osculating conic trajectory are computed for reference (these variables are not utilized in the program due to problems of indeterminancies as e and ω approach zero). Operation from this point is identical to the case where the test was failed.

Computational Logic:





SUBROUTINE UPSTAT UPSTOADSO STATE VECTOR IS KNOWN TO REASONABLE PRECISSION. IT IS ALSO DESIGNED TO WRITE GUT THE STATE INFORMATION AND TO BYSTOADSO STATE VECTOR IS KNOWN TO REASONABLE PRECISSION. IT IS UPSTOADSO STATE VECTOR IS KNOWN TO REASONABLE PRECISSION. IT IS ALSO DESIGNED TO WRITE GUT THE STATE INFORMATION AND TO BYSTOADSO PATAL REPOLITION AND VECTOR AND STATE THAN STATE THE GW UPSTOADSO MATRICES.CAN BE COMPUTED. * * * * * * * * * * * * * * * * * * *			
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SIGNE HE POSITION AND VELUCITY ARRAYS AT THE TIME OF UPSTOON HATRICES CAN BE COMPUTED. * * * * * * * * * * * * * * * * * * *		SØ DESIGNED IG WRITE GUI THE STATE INFORMATION AND I	010010
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* * * * * * * * * * * * * * * * * * *		IRICES CAN BE COMPOIED.	01010 01010
DIMENSIGN CGN(1), SAT(1), SDA(1), WRK(1), STT(1) UPSTO12 UPSTO13 CGMM3N DATA EQUIVALENCE ('DATA(1),CGN), ('DATA(16),SAT), ('DATA(36),SDA) UPSTO16 DIMENSIGN RGTINV(3,3),RCGNIC(3),RTATE(6),PTGA(36),SDA) UPSTO17 DIMENSIGN RGTINV(3,3),RCGNIC(3),RTATE(6),PTGA(6) UPSTO18 DIMENSIGN RGTINV(3,3),RCGNIC(3),RR(3) LOYTOZO LOYTOZO LOYTOZO CGN(14),NGU 1),RR 1, (CGN(6),GM 1) UPSTO2A CGN(14),NGU 1), (WRK(50),TW 1) UPSTO2A LOYTOZO CON(14),NGU 1), (WRK(51),TF 1) UPSTO2A LOYTOZO LO	₩	**********************	ST011
DIMENSIAN CON(1), SAT(1), WRK(1), STT(1) UPSTO14 COMMON DATA (COMMON DATA (COMMON DATA (DATA(286),STT), (DATA(16),SAT), (DATA(36),SDA) (DPSTO15 DIMENSION RGTINV(3,3),RCONIC(3), NTRANS(3) (DPSTO18 DIMENSION RGTINV(3,3),RCONIC(3), NTRANS(3) (DPSTO20 COMMON RGTINV(3,3),RCONIC(3), NTRANS(3) (DPSTO20 COMMON RGTINV(3,3),RCONIC(3), NTRANS(3) (COMMON RGTINV(3,3),RR(3), NTRANS(3) (COMMON RGTINV(3,3),RR(3), NTRANS(3) (COMMON RGTINV(3,3),RR(3),RR(3),RR(3),RR(3) (COMMON RGTINV(3,3),RR(3),RR(3),RR(3),RR(3),RR(3),RR(3),RR(3) (COMMON RGTINV(3,3),RR(ST012
CGMM3N DATA CGMM3N DATA CGMM3N DATA (DATA(286),STT), (DATA(16),SAT), (DATA(36),SDA) DIMENSION RGIINV(3,3),RCGNIC(3),VCGNIC(3),RTRANS(3) DIMENSION RGIINV(3,3),RCGNIC(3),VCGNIC(3),RTRANS(3) DIMENSION RGIINV(3,3),RCGNIC(3),RR(3) SAME AND ATE(3),RCGNIC(3),RR(3) SAME AND ATE(3),RCGNIC(3),RR(3) CGNIC AND ATE(3),RR(3) CGNIC AND ATE(3),RR(3) CGNIC AND ATE(3),RR(3) CGNIC AND AND ATE(3) CGNIC AND ATE(3),RR(3) CGNIC AND ATE(3),RR(3) CGNIC AND ATE(3) CGN	0.1	CGN(1), SAT(1), SDA(1), WRK(1), STT(ST013
CGMM3N DATA CGMM3N DATA (DATA(18, CGN), (DATA(16), SAT), (DATA(36), SDA) UPSTO15 (DATA(286), STT), (DATA(391), WRK) DIMENSIGN RGIINV(3,3), RCONIC(3), VCGNIC(3), RTRANS(3) UPSTO19 DIMENSIGN RGIINV(3,3), RCONIC(3), VCGNIC(3), RTRANS(3) UPSTO20 2, VTRANS(3), RDATE(3), VCGNIC(3), RR(3) (MPSTO21) B. (CRN(11), RR(3)), RR(3) (MPSTO22) CGNI (14), NGUT), (WRK(51), TF) UPSTO22 COUIVALENCE (WPK(50), RUT), (WRK(51), TF) UPSTO22 COUIVALENCE (WPK(50), RUT), (WRK(51), TF) UPSTO22 COUIVALENCE (WPK(50), RUT), (WRK(51), TF) UPSTO22 COUIVALENCE (WPK(50), RUT), (WRK(114), VOATE) UPSTO22 COUIVALENCE (WPK(50), TWPRNT), (WRK(111), RNATE), (STT(60), P) UPSTO33 COUIVALENCE (SO), TWPRNT), (WPKK (70), TFRNT) COUIVALENCE (WPK(50), TWPRNT), (WPKK (70), TFRNT) COUIVALENCE (WPK(111, VOATE), (STT(64), STATE), (STT(70), P) UPSTO33 WRITF(6,1) TW, TF TWPRNT, TFPRNT FORMAT(1H1, 2X, 27HFPGCH (REL. TG 1950.0)) =, 2F17.8, 1X, 12H(DAYS, DAUPSTO35)			ST014
EQUIVALENCE (7ATA(1),CON), (DATA(16),SAT), (DATA(36),SDA) 2 3, (DATA(286),STT), (DATA(391),WRK) DIMENSION RGTINV(3,3),RCGNIC(3),YCGNIC(3),RTRANS(3) 9, VRANS(3),RDATE(3),VCGND(3),RR(3) 9, VRANS(3),RCGNIC(3),YCGND(3),RR(3) 1, RCGND(3),YCGND(3),YCGND(3),RR(3) 1, RCGND(3),YCGND(3),YCGND(3),RR(3) 1, RCGND(3),YCGND(3),YCGND(3),RR(3) 1, RCGND(3),YCGND(3),YCGND(3),RR(3) 1, RCGND(3),YCGND(3),RR(3),YCGND(3) 1, RCGND(3),YCGND(3),RR(3),YCGND(3) 1, RCGND(3),YCGND(3),RR(3),YCGND(3) 1, RCGND(3),YCGND(3),RR(3),YCGND(3) 1, RRK(31),YCGNIC),RRK(32),YCGNN),RRK(35),YCGND(3) 1, RRK(31),YCGNIC),RRK(31),YCGND(3),RRK(35),YCGND(3) 1, RRK(31),YCGNIC),RRK(31),YCGND(3),RRK(35),YCGND(3) 1, RRK(31),YCGNIC),RRK(31),YCGND(3),YCGND(3) 1, RRK(31),YCGNIC),RRK(31),YCGND(3),YCGND(3) 1, RRK(31),YCGNIC),RRK(31),YCGND(3) 1, RRK(31),YCGNIC),RRK(31),YCGND(3) 1, RRK(31),YCGNIC),RRK(31),YCGND(3) 1, RRK(31),YCGNIC),RRK(31),YCGND(3) 1, RRK(31),YCGNIC),RRK(31),YCGNIC) 1, RRK(31),YCGNIC),RRK(31),YCGNIC) 1, RRK(31),YCGNIC),RRK(31),YCGNIC) 2, RRK(31),YCGNIC),RRK(31),YCGNIC) 2, RRK(31),YCGNIC),RRK(31),YCGNIC) 2, RRK(31),YCGNIC),RRK(31),YCGNIC) 3, RRK(31),YCGNIC),RRK(31),YCGNIC) 4, YCGNIC,RRK(31),YCGNIC) 5, RRK(31),YCGNIC),RRK(31),YCGNIC) 6, RRK(31),YCGNIC) 1, R	C G	DAT	ST015
EQUIVALENCE (7ATA(1),CGN), (DATA(16),SAT), (DATA(36),SDA) UPSTO18 2			ST016
2 , (DATA(286),STT), (DATA(391),WRK) DIMENSION RGIINV(3,3),RCGNIC(3) ,VCGNIC(3) ,RTRANS(3) UPSTO20 2,VTRANS(3),RDATE(3) ,VDATE(3) ,YCGNIC(3) ,P(6,6) UPSTO22 3 ,B(4) ,RCGND(3) ,VCGND(3) ,RR(3) ,VV(3) UPSTO22 5 ,CGN(1),RF), (CGN(6),GM) UPSTO22 5 ,CGN(1),RF), (CGN(6),GM) UPSTO22 6 ,CGN(1),RF), (WRK(51),TF) UPSTO22 7 ,(WRK(31),VCGNIC), (WRK(34),TTRANF) (WRK(31),ROATE) UPSTO22 7 ,(WRK(31),VCGNIC), (WRK(34),TTRANF) (WRK(111),ROATE) UPSTO23 7 ,(WRK(34),TTRANF), (WRK(111),ROATE) (WRK(114),VOATE) UPSTO23 7 ,(WRK(69),TWPRNT), (WRK(111),ROATE) (WRK(114),VOATE) UPSTO33 8 , x x x x x x x x x x x x x x x x x x	Ē	(DATA(1), CON), (DATA(16), SAT), (DATA(36), SD	ST017
DIMENSION RGIINV(3,3), RCONIC(3) , VCONIC(3) , RTRANS(3) UPSTO20 3 ,6(4) , RCOND(3) , VCOND(3) , STATE(6) , P(6,6) UPSTO20 3 ,6(4) , RCOND(3) , VCOND(3) , RR(3) , VV(3) UPSTO20 5 (CON (1), RF), (CON (6), GM) UPSTO22 5 (WFK (50), ROTIND) (WFK (50), RTRANS) UPSTO22 6 (WPK (31), VCONIC) (WPK (50), ROTIND) (WFK (42), RTRANW) UPSTO23 7 , (WRK (31), VCONIC) (WPK (32), VTRANS) (WFK (32), TTRANW) UPSTO23 7 , (WRK (36), RTRANS) (WFK (37), VTRANS) (WFK (42), TTRANW) UPSTO23 7 , (WFK (43), TTRANS) (WFK (111), RDATE) (WFK (114), VDATE) UPSTO23 7 , (WFK (69), TWPRNT), (WFK (70), TFPRNT) (WFK (111), VDATE) UPSTO33 8 * * * * * * * * * * * * * * * * * * *		, (DATA(286), STT), (DATA(391), W	ST018
DIMENSION RGTINV(3,3), RCGNIC(3) , RTRANS(3) UPSTC20 2,VTRANS(3), RDATE(3) , VOATE(6) , P(6,6) UPSTC21 3,8(4) , RCGND(3) , VCGND(3) , RR(3) , VV(3) UPSTC22 2			STu19
2,VTRANS(3),RDATE(3) ,VDATE(3) ,STATE(6) ,P(6,6) UPSTO21 3,8(4) ,RCGND(3) ,RR(3) ,VV(3) UPSTO22 6(UIVALENCE (CGN(1),RF), (CGN(6),GM) UPSTO25 7 (WPK (51),TF), (WRK (51),TF) UPSTO25 7 (WPK (51),TW), (WRK (51),TF) UPSTO27 2 ,(WRK (31),VCGNIC), (WRK (10),RGTINV), (WRK (28),RCGNIC) UPSTO27 3 ,(WRK (36),RTRANS), (WRK (111),RDATE), (WRK (42),TTRANW) UPSTO27 4 ,(WPK (43),TTRANS), (WRK (111),RDATE), (WRK (114),VDATE) UPSTO37 5 ,(WRK (69),TWPRNT), (WPK (70),TFPRNT) UPSTO37 8 ,(WRK (69),TWPRNT), (WPK (70),TFPRNT) UPSTO37 8	OI	RGTINV(3,3), RCONIC(3) , VCONIC(3) , RTRANS(STOZO
3 ,8(4) ,RCGND(3) ,VCGND(3) ,RR(3) ,VV(3) UPSTO22 UPSTO23 (CGN(14),NGUT) (CGN(6),GM) UPSTO24 UPSTO25 ,(CGN(14),NGUT) (WRK(51),TF) UPSTO25 (WFK(50),TW) (WRK(28),RCGNIC) UPSTO27 (WRK(31),VCGNIC), (WPK(10),RGTINV), (WRK(35),TCGNF) UPSTO27 (WRK(36),TWPRNT), (WPK(11),RDATE), (WRK(114),VDATE) UPSTO28 (WRK(69),TWPRNT), (WPK(70),TFPRNT) (WRK(114),VDATE) UPSTO31 (WRK(69),TWPRNT), (WPK(70),TFPRNT) (WRK(114),VDATE) UPSTO31 (WRK(69),TWPRNT), (WPK(70),TFPRNT) (WRK(114),VDATE) UPSTO31 (WRK(69),TWPRNT), (WPK(70),TFPRNT) (WRK(114),VDATE) UPSTO33 (WRK(69),TWPRNT), (WPK(70),TFPRNT) (WRK(114),VDATE) UPSTO33 (WRK(69),TWPRNT), (WPK(70),TFPRNT) (WRK(114),VDATE) UPSTO33 (WRK(69),TWPRNT,TFPRNT) UPSTO34 (WRTF(64),TTWPRNT,TFPRNT) UPSTO34 (WRTF(64),TTWPRNT,TFPRNT) UPSTO34 (WRTF(64),TTWPRNT,TFPRNT) UPSTO34 (WRTF(64),TTMPRNT,TFPRNT) UPSTO34 (WRTF(64),TTMPRNT) UPSTO34 (WRTTF(64),TTMPRNT) UP	2, <	RDATE(3) , VDATE(3) , STATE(6) , P(6,6	ST021
UPSTO23 EQUIVALENCE , (CGN(11),RF), (CGN(6),GM) UPSTO24 LOND TO25 (WFK(57),TW), (WRK(51),TF) UPSTO25 (WFK(30),TW), (WRK(10),RGTINV), (WRK(28),RCGNIC) UPSTO27 (WPK(31),VCGNIC), (WRK(110),RGTINV), (WRK(42),TTRANW) UPSTO27 4, (WPK(43),TTRANF), (WRK(111),RDATE), (WRK(114),VDATE) UPSTO29 5, (WRK(69),TWPRNT), (WRK(111),RDATE), (WRK(114),VDATE) UPSTO39 EQUIVALENCE (STT(64),STATE), (STT(70),P) UPSTO33 * * * * * * * * * * * * * * * * * *	w	.RC@ND(3) , VC@ND(3) , RR(3) , VV(3	ST022
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2	w	ENCE (CAN(1), RF), (CAN(6), G	ST024
FOUIVALENCE (WFK(50),TW), (WRK(51),TF) UPSTO26 FQUIVALENCE (WPK(10),RGTINV), (WRK(28),RCGNIC) UPSTO27 WRK(31),VCGNIC), (WRK(34),TCGNW), (WRK(35),TCGNF) UPSTO28 WRK(36),RTRANS), (WRK(111),RDATE), (WRK(114),VDATE) UPSTO30 WRK(69),TWPRNT), (WRK(111),RDATE), (WRK(114),VDATE) UPSTO30 WRK(69),TWPRNT), (WRK(111),RDATE), (WRK(114),VDATE) UPSTO30 WRTGENCE (STT(64),STATE), (STT(70),P) UPSTO33 * * * * * * * * * * * * * * * * * *		, (CGN(14), NGUT)	ST025
FQUIVALENCE (WPK(10), RGTINV), (WRK(28), RCGNIC) UPSTO27 7	FID	ENCE (WPK(50), TW), (WRK(51), TF	ST026
2 *(WRK(31),VCGNIC), (WRK(34),TCGNW), (WRK(42),TTRANW) UPSTC28 3 ,(WRK(36),RTRANS), (WPK(39),VTRANS), (WRK(42),TTRANW) UPSTC29 4 ,(WPK(43),TTRANF), (WRK(111),ROATE), (WRK(114),VDATE) UPSTC30 5 ,(WRK(69),TWPRNT), (WPK(70),TFPRNT) UPSTC30 EQUIVALENCE (STT(64),STATE), (STT(70),P) UPSTC31 UPSTC32 * * * * * * * * * * * * * * * * * * *	w	ENCE (WPK(10), RGTINV), (WRK(28), RCGNI	ST027
3 , (WRK(36), RTRANS), (WRK(111), RDATE), (WRK(114), VDATE) UPST030 4 , (WPK(43), TTRANF), (WRK(111), RDATE), (WRK(114), VDATE) UPST030 5 , (WRK(69), TWPRNT), (WPK(70), TFPRNT) UPST031 EQUIVALENCE (STT(64), STATE), (STT(70), P) UPST031 * * * * * * * * * * * * * * * * * UPST033 WRITF(6,1) TW, TF, TWPRNT, TFPRNT UPST035 FORMAT(1H1, 2X, 27HFPGCH (REL. TØ 1950.0)) =, 2F17.8, 1X, 12H(DAYS, DAUPST035)), VCGNIC), (WRK(34), TCBNW), (WRK(35), TCB	STr28
4 , (WPK(43), TTRANF), (WRK(111), RDATE), (WRK(114), VDATE) UPSTG30 5 , (WRK(69), TWPRNT), (WRK(70), TFPRNT) EQUIVALENCE (STT(64), STATE), (STT(70), P) UPSTG31 * * * * * * * * * * * * * * * * * * *		", RTRANS), (WPK(39), VTRANS), (WRK(42), TTR	ST029
5 , (WRK(69), TWPRNT), (WPK(70), TFPRNT) EQUIVALENCE (STT(64), STATE), (STT(70), P) UPST031 * * * * * * * * * * * * * * * * * * *		",TTRANF), (WRK(111),RDATE), (WRK(114),VDA	51030
EQUIVALENCE UPST031 * * * * * * * * * * * * * * * * * * *		", TWPRNT), (WPK(70), TFPR	STEAN
UPST032 * * * * * * * * * * * * * * * * * * *	C	IVALENCE (STT(64), STATE), (STT(70),	ST031
* * * * * * * * * * * * * * * * * * *			ST032
UPSTO34 WRITF(6,1) TW,TF,TWPRNT,TFPRNT UPSTO35 FORMAT(1H1,2X,27HFPGCH (REL. TØ 1950.^) =,2F17.8,1X,12H(DAYS,DAUPSTO35		*****************	PST033
UPSTO35 WRITE(6,1) TW, TF, TWPRNT, TEPRNT FORMAT(1H1,2X,27HFPOCH (REL. TO 1950.^) =,2F17.8,1X,12H(DAYS,DAUPSTO35			PST034
FORMAT(IH1,2X,27HFPGCH (REL. TØ 1950.^) =,2F17.8,1X,12H(DAYS,DAUPST?35	α 3	1) TW, TF, TWPRNT, TFPRNT	ST035
		.H1,2X,27HFPGCH (REL. TG 1950.^) =,2F17.8,1X,12H(DAYS,	UPST035

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SID 65 1203-1

01/22/86

SUBRGUTINE UPSTAT

VARIABLES
COMMON

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SID 65 1203-1

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UPST

SUBROUTINES CALLED DOT SECTION 6 -UNO6. SECTION 9 -FFIL. SYSLOC SECTION 12 EFN IFN CORRESPONDENCE FFN IFN CORRESPONDENCE 100 124 01433 2 4 FORMAT 01157 10 76A 11 62A 01572 40 76A 30 101A 01723 21 FORM	SUBRGUTINES CALLED DOT UNO6. SECTION SECTION SECTION SECTION 12 FFN IFN CORRESPONDENCE IFN CORRESPONDENCE FORMAT 01157 1001A 011723 21			STORAGE	AGE MAP	01/22/86	86	PAGE
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		ù1162	30	101A	01723		FORM	⊢ ∀

2.4.1.5.1 Subroutine ELEMEN

Purpose:

to compute the classical conic elements (for the purpose of user convenience) at those times when estimation of the state vector has been performed (providing that tolerances established in UPSTAT for the estimation

errors are satisfied).

Deck Name:

ELEM

Calling Sequence:

CALL ELEMEN (R, V, GM, REQ, A, E, P, THETA, OMEGA, OMEGAW,

OINC, OMDOT, WDOT)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	R	ř	3	ARG	radius vector (cartesian) Km
I	v	Ÿ	3	ARG	velocity vector (cartesian)
I	GM	u	1	ARG	km/sec gravitational constant for central body (km3/sec2)
I	REQ	R _e	1	ARG	equatorial radius (km)
0	A	a	1	ARG	semimajor axis (km)
0	E	е	1	ARG	eccentricity
0	Р	p	1	ARG	semilatus rectum (km)
0	THETA	Θ	1	ARG	true anomaly of epoch (rad)
0	OMEGA	<u>.</u>	1	ARG	right ascension of ascend- ing node (rad)
0	OMEGAW	ω	1	. ARG	argument of periapse (rad)
0	OINC	i	1	ARG	orbital inclination (rad)
0	OMDOT	ΔΩ	1	ARG	secular change in Λ due to earths oblateness (rad/rev)
0	WDOT	Δω	1	ARG	secular change in ω due to earths oblateness (rad/rev)

Subroutines required:	CROSS	(cross product)
Functions required:	AMAG DOT ATAN SQRT SIN	<pre>(vector magnitude) (dot product) (arc tangent) (square root)</pre>
Approximate Deck Length:	640	(octal)

Formulation:

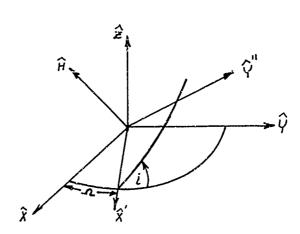
The paragraphs which follow present a summary of the equations which are mechanized in the routine and other information required to resolve ambiguities in quadrant, etc. This approach to the formulation assumes a degree of familiarity with the equations of conic motion in terms of the "classic" elements; thus, should questions arise, a discussion similar to that of Ref. 1 should be reviewed.

The first step to be performed is the definition of the plane of motion. This set of computations will be accomplished through consideration of the angular momentum vector (per unit mass) and will assume that the position and velocity vectors exist in a cartesian format in some selected frame of reference (the main program operates in the true equator of date frame).

$$\vec{h} = \vec{r} \times \vec{\nabla}$$

$$\hat{H} = \vec{h}/|\vec{h}|$$

The orientation of \hat{H} can now be obtained in terms of the orbital inclination and the right ascension of the ascending node by two simple rotational transformations



$$\begin{cases} \hat{\mathbf{x}}' \\ \hat{\mathbf{y}}' \\ \hat{\mathbf{z}}' \end{cases} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos i & \sin i \\ 0 & -\sin i & \cos i \end{bmatrix} \cdot \begin{bmatrix} \cos \Omega & \sin \Omega & 0 \\ -\sin \Omega & \cos \Omega & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} \hat{\mathbf{x}} \\ \hat{\mathbf{y}} \\ \hat{\mathbf{z}} \end{pmatrix}$$

and

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$$\hat{H} = \sin i \sin \Omega \hat{X} - \sin i \cos \Omega \hat{Y} + \cos i \hat{Z}$$

Now equating the two expressions for \widehat{H} yields the desired information:

$$cooi = H_3 \qquad 0lil180$$

$$sin \Omega = H_1/sin i$$

$$coo \Omega = -H_2/sin i$$

The next step is the computation of the energy of the conic (or its equivalent the semimajor axis) and the eccentricity. This computation involves both the energy and angular momentum equations

$$\frac{-\mathcal{U}}{2\alpha} = \frac{\sqrt{2} - \mathcal{U}}{2\sqrt{r}}$$

$$\rho = \left| \vec{h} \right|^{2} / \mathcal{U}$$

$$e = \sqrt{1 - P_{\alpha}}$$
a < 0 Hyperbolic motion
$$a > 0$$
 Elliptic motion

The final step is the computation of the argument of periapse (ω) and the position in the orbit at the given time (θ = true anomaly of epoch) (see sketch)

β γ perigee

This evaluation is accomplished as follows:

$$\varphi = \cos^{-1}\left[\frac{\hat{\mathbf{x}}' \cdot \dot{\mathbf{r}}}{|\dot{\mathbf{r}}|}\right]$$

 φ = angle from ascending node = $\theta + \omega$

$$0 < \varphi < \pi \qquad r_3 > 0$$

$$\pi < \varphi < 2\pi \qquad r_3 < 0$$

$$\Theta = coo^{-1} \left[\frac{\rho - r}{re} \right]$$

$$0 < \theta < \pi \qquad \overrightarrow{r} \cdot \overrightarrow{v} > 0$$

$$\pi < \theta < 2\pi \qquad \overrightarrow{r} \cdot \overrightarrow{v} < 0$$

The routine concludes with the computation of the secular perturbations in the right ascension of the ascending node (Ω) and in the argument of periapse (ω) resulting from the first coefficient of the potential function (J_2)

$$\Delta \Omega = -3 \pi J_2 \left(\frac{Re}{P}\right)^2 \quad \cos i \qquad \text{rad/rev}$$

$$\Delta \omega = 3 \pi J_2 \left(\frac{Re}{P}\right)^2 \left(2 - \frac{5}{2} \sin^2 i\right) \qquad \text{rad/rev}$$

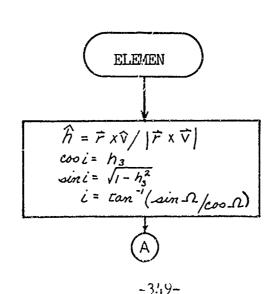
where: R_e = the equatorial radius of the oblate spheroid

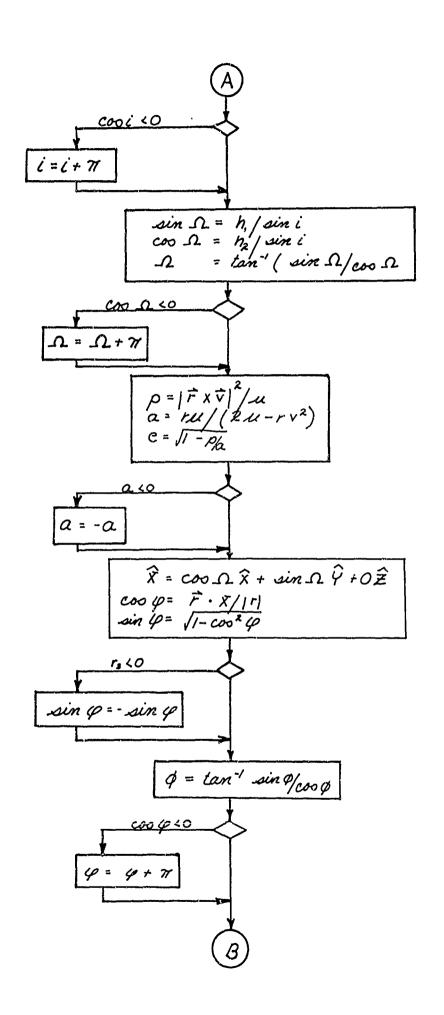
References

1) Townsend, G. E., "Orbital Mechanics" in the Orbital Flight Handbook, Volume 1, Part 1, Chapter 3 NASA - SP-33, (1963).

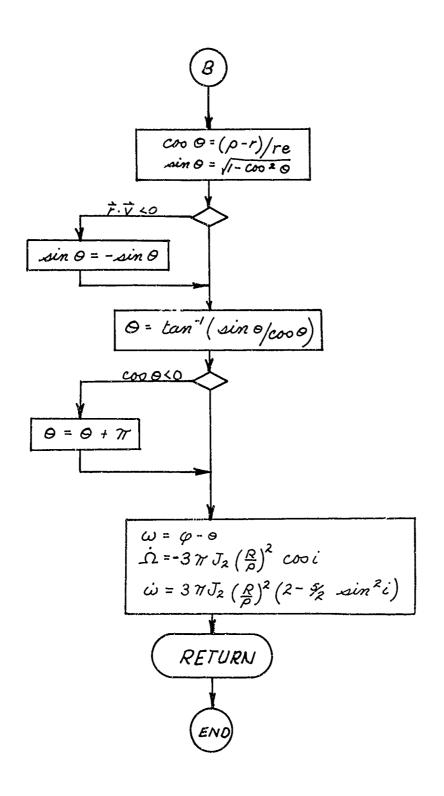
Computational Logic:

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PHI=0.		LEM076	
60 10 1		LEM077	
PHI = SURT (1		LEM078	
1) 111,112,111	•	LEMO79	
1.5707963		LEM080	1
IF(R(3)) 113,250,250		LEM081	
÷.7123889		LEM082	1
09		LEM083	
4		LEM084	
SPHI		LEM085	
ATAN (SPHI/C		LEM086	
IFICPHI) 200,250,25		LEM087	
PHI =PHI + 3,141592		LEM088	i
D-RMAGI/(KMAG *E		LEM089	! !
IF (ABS(CT)-1.) 62,6		LEMD90	
		LEM091	
60.1		LEM092	
JRT (1 LT*C		LEM093	
IF (DOT(R,V))	•	LEM094	1
ST =-ST	1	LEM095	
IF(CT) 31,41,3		LEM096	
=1.570	•	LEM097	
IF(ST) 42,33,33		LEM098	
=4.71238	1	LEM099	
33		LEM10C	;
= ATAN (LEMIDI	
32,33,33		LEM102	
= THETA +		LEM103	
I = PHI - I	,	LEM104	
(UMEGAW) 35,37	•	LEM105	
MEGAW = 6.283185	,	LEM10	
		LEM107	
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SID 65 1203-1 -355-

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SID 65 1203-1 -357-

2.4.1.6 Subroutine DATAPE

Reads a specially generated magnetic tape containing smoothed and ordered coordinate data. Purpose:

DAPE Deck Name:

CALL DATAPE (KOUNT) Calling Sequence:

Input/Output:

ziipao/ (·		
I/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Description
0	TW TF	T _{DATA}	1	WRK(61) WRK(62)	The whole and fractional part of the number of days relative to 1950.0 at which the next observation will occur (1950.0 = J.D. 2433282.423)
0	ISTN	_	1	WRK(63)	The number for the observ- ing station
0	ITYPE	-	1	WRK(64)	The type of data: 1, Range 2, Range-Rate 3, Azimuth, Elevation 4, Range, Range-Rate 5, Range, Azimuth, Elevation 6, Range-Rate, Azimuth, Elevation
0	ODATA		3	WRK(65)	The components of the observation vector
1/0	KOUNT		. 1	ARG	Control indicator. Code: 1, Do not return next point (INPUT) 2, Return next point (INPUT) 3, No more data points on tape (OUTPUT)

Subroutines Required:

None

Functions Required:

None

Approximate Storage Required:

650 (octal)

Restrictions:

Requires that the input data tape to be generated by FS4-305A be mounted on logical

tape drive unit 9.

Nomenclature:

FØRTRAN Name	Dimensions	Description
A	7,37	Buffer array containing a single logical tape record.
IFIRST		First pass indicator
IGP		Logical record counter, IGP=1, NGPS
NGPS		Number of logical data records on tape.
NPERGP		Number of points per logical record, excluding final record.
NPREM		Number of points per final record.
npøint		Buffer array point index, NPØINT=1, (NPERGP or NPREM)
XJDREF		Program reference Julian date.**

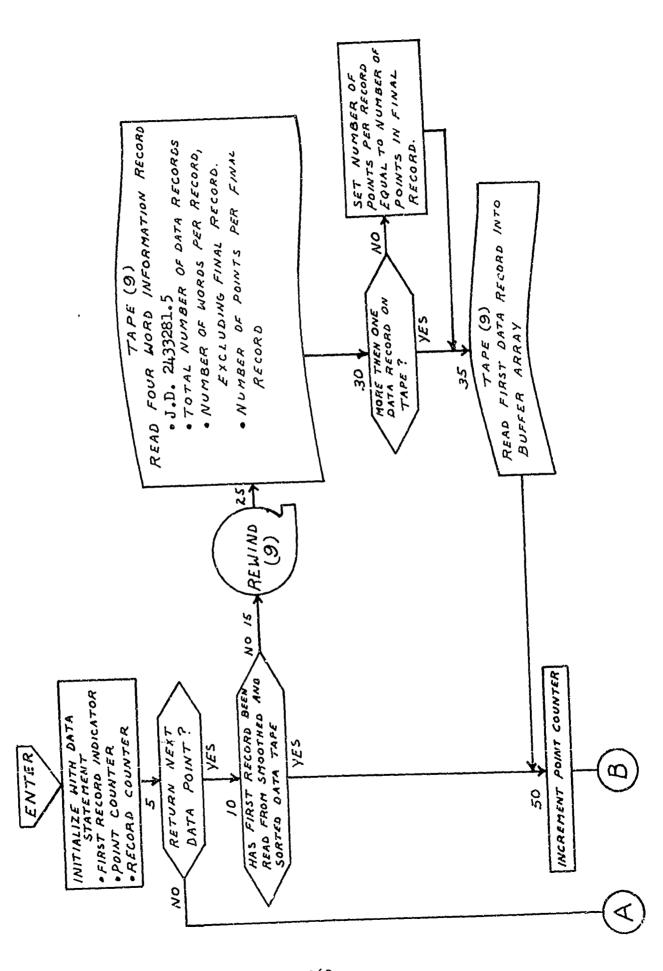
Method:

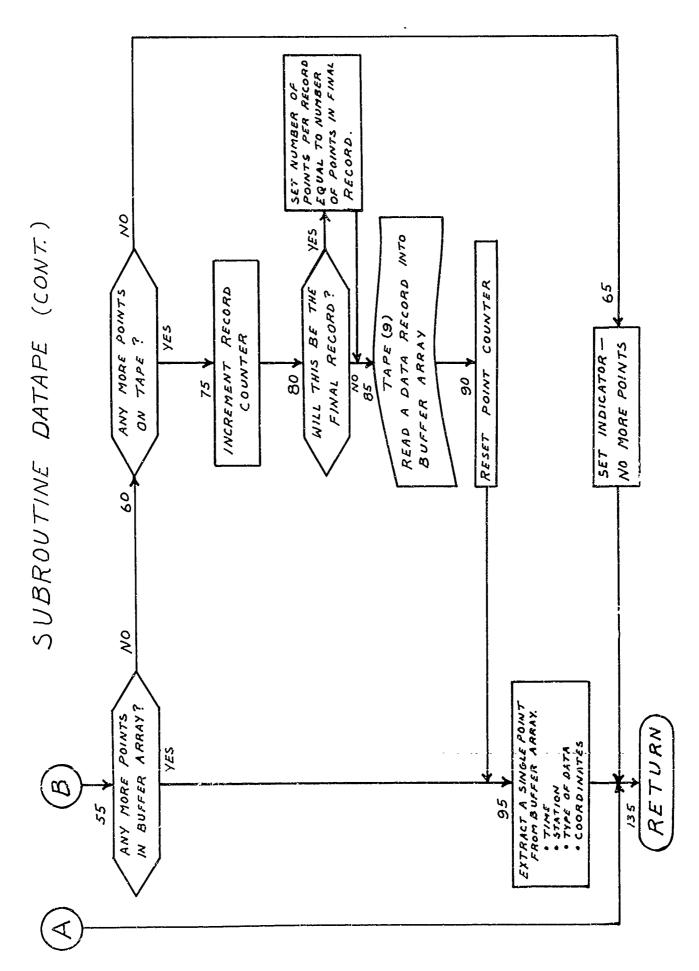
The first CALL statement to this subroutine mechanizes the input data tape prepared by the preliminary processor program. An information record containing J.D.2433281.5 (unused in this program), the number of logical records, and the number of data points* per record is read into the program. The first logical data record is then read into the buffer array A and, after extracting the first data point from the buffer, control is returned to the calling routine. Subsequent CALL statements extract single points sequentially from the buffer. After the final point within the buffer has been extracted, the next logical record is read in and the procedure is repeated until all data has been read from the tape at which time the count index (KOUNT) is set equal to 3 and control is returned to the norm program.

*A data point is defined as the ordered set TW, TF, ISTN, ITYPE, ØDATA. ***JD (24) 33282.423

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01/21/86 DAPEON2N DAPEON30 DAPEO040	0APE0050 0APE0060 0APE0070 0APE0080	DAPE 0090 DAPE 0100 DAPE 0110 DAPE 0120	DAPEO140 DAPEO150	0APE0160 0APE0170 0APE0180	0APE0190 0APE0200 0APE0210	0APE0220 0APE0230 0APE0240	DAPEn250 DAPE0260 DAPE0270 DAPE0280 DAPE0290	DAPF0310 DAPE0320	4 P P P P P P P P P P P P P P P P P P P	APEQ
SUBPOUTINE DATAPE(KOUNT)	*** FS4-305 *** PURPUSE,	RFADS A SPECIALLY GENERATED MAGNETIC TAPE CONTAINING SMOOTHED AND ARDERED OBSERVATION VECTORS AS FUNCTIONS OF TIME AS THE PRIMARY ARGUMENT	TW , TIME. INTEGER DAYS FROM 1950.0 (JD 2433282.423)	TF , TIME. FRACTIONAL DAY. (U.T.) ISTN , STATION FROM WHICH DATA WAS RECIEVED. ITYPE, INDICATES TYPE OF DATA IN ODATA.	1, RANGE 2, RANGE RATE 3, AZIMUTH, FLEVATION	4, RANGE,RANGE RATE 5, RANGE,AZIMUTH,FLEVATION 6, RANGE RATF,AZIMUTH,FLFVATION	DATA. DICATGR. T RETURN NEXT POINT. (INPUT) N NEXT PJINT (INPUT) RF DATA POINTS ON TAPE.(OUTPUT)	METHØD,	LOGICAL DATA RECORDS ARE READ FROM TAPE INTO THE BUFFER ARRAY A. SINGLE DATA POINTS ARE THEN SEQUENTLY EXTRACTED GF FROM THE BUFFER BY EACH CALL OF DATAPE.	65-1203-1

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DAPE0410 OAPPO300 DAPF0420 DAPEC430 DAPE0440 DAPF0450 DAPECAGO DAPE0400 泸 В П ₩ REQUIRES THAT THE INPUT DATA TAPE GENERATED BY FS4-305A # ***** * 46 ¥ CAN(1), SAT(1), SDA(1), WRK(1), STT(1) ₩ ķ ₹ MUUNTED ON LOGICAL TAPE DRIVE UNIT 9. ¥ ¥ 46 ¥⊱ * * * ₩ **⊰**⊱ ¥ ₩ 46 ₩ ⋠⊱ ***** ₩ DIMENSION ₩ 长 *

C.GMMGN DATA

(), CON). (DATA(16), SAT), (DATA(36), SDA) , (DATA(286), STT), (UATA(391), WKK) (DATA(EQUIVALENCE

DAPE0520

DAPF0470

DAPE1480

DAPE0490 NAPE0500 DAPEG519 DAPENSSC

DAPERSTO DAPE0580 **NAPEN590** DAPERAN DAPEO610

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DAPF0560

DAPF0540

DAPEN530

4 A (1, 37) GD4TA(3) DIMENSION

651, GDATA), (WRK(62), TF), (WRK(), (WRK(64), ITYPE (WRK(61), TW , [WRK(63), ISTN EQUIVALENCE

IFIRST, NPGINT, IGP / 3*0 DATA

GG TG 135 K GUNT . EQ. 1 1 1 1

חל) GG TO IFIRST.NE.O

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IFIRST = 1 REWIND 9 15 ω

READ (9) XJOREF, NGPS, NPERGP, NPREM IF (NGPS, EQ. 1) NPERCP = NPREM 25 30

RFAD (9) (14(J,1), J=1,7), I=1, NENP) C 4

SID 65-1203-1 -363-

NEND = NPERGP l = d9135

INCREMENT BUFFER PRINT CRUNT.

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DAPF0650 DAPF1660

FIRST PASS, READ INFORMATION

AND FIRST DATA RECOOD.

DAPFO670 DAPECERO DAPEN690 DAPFO700

DAPE0630 DAPF1640

DAPFO620

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DAPFA710

DAPEN720 DAPFO730 DAPE0740

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       POINT HAS BEEN EXTRACTEDDAPECT60
                 FROM THE BUFFER, READ NEXT RECO. DAPE0770
                             DAPE0780
                                       DAPE0790
                                                 DAPE0800
                                                            DAPE0810
                                                                       DAPEOR20
                                                                                 DAPE0830
                                                                                            DAPEC840
                                                                                                      DAPE0850
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                                                  MORE DATA, SET KOUNT EQUAL
                                                                                                                                                           EXTRACT POINT FROM BUFFER.
                                       READ NEXT LOGICAL RFCORD.
                                                             AND RETURN.
         IF FINAL
                                                                                                                                       PFAD (9) ((A(J,I),J=1,7),I=1,NEND)
                                                                                                                             IF( IGP.EQ.NGPS ) NEND = NPREM
                              IF ( NPGINT.LE.NEND ) GO TO 95
                                                                         10
                                                                                                                                                                      A(1,NPGINT)
                                                                                                                                                                                 A(2,NPGINT)
                                                                                                                                                                                           A(3, NPOINT)
                                                                                                                                                                                                                         A(6,NPGINT)
                                                                                                                                                                                                    A(4, NPGINT)
                                                                                                                                                                                                                A(5, NPGINT)
                                                                                                                                                                                                                                    A ( 7 , NP GINT )
                                                                         IF ( IGP.NF.NGPS ) GO
 +
= NPGINT
                                                                                                                   16P = 16P + 1
                                                                                                                                                                                            П
                                                                                   KOUNT = 3
                                                                                             GØ TØ 135
                                                                                                                                                  NPGINT =
                                                                                                                                                                                                                                     GDATA(3)
                                                                                                                                                                                                                 GDATA(1)
                                                                                                                                                                                                                           GDATA(2)
                                                                                                                                                                                                                                               CONTINUE
 NPGINT
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ЕМАР	VAR I ABL ES		7 X X X I	PRGGRAM V.	TYPE	PRGGRAM VA	TYPE R I	PGINTS		SUBROUTINES CALLFD	3N N 6
STØRAGE SUBRGUTINE DATAPE	CGMMGN VA	ORIGIN	LGCATION 00000 00043 00702 00705	DIMENSIONFD	LOCATION	ND I MENS I GNED	LGCA110N 01316 01321 01324	FNTRY		SUBROL	SECTION SECTION
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2.5 Matrix and Vector Algebra Group

The routines of this group are general purpose algebraic routines for vectors and matrices, and there are no inherent limitations in the formulations or codings which restrict application (though there are fixed dimensions in some cases which should be altered to provide expanded coverage). Accuracy is assured in those cases where single precision arithmetic may produce loss of significances by employing double precision.

2.5.1 Subroutine MATMPY (Matrix Multiplication)

Purpose:

MATMPY is designed to multiply any two conformable single precision matrices (with less than 70 elements each) to obtain the single precision product. All operations interior to the routine are performed in double precision to control roundoff and loss of significance.

Deck Name:

MX PY

Calling Sequence: CALL MATMPY (C, I, K, D, K, J, CD)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	c	С	I (rows) K (columns)	Arg	Array of numbers to be used in the premultiplication of D by C.
I	D	D	K (rows) J (columns)	Arg	Array of numbers to be premultiplied by the matrix C.
I	CD	CD	I (rows) J (columns)	Arg	Product array.

Subroutines Required: None

Functions Required:

None

Approximate Deck

Length:

700 (decimal)

1300 (octal)

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2.5.2 Subroutine MTINV (Matrix Inverse)

Purpose:

MTINV computes the inverse of a nonsingular square array (of up to 36 elements) using the theorem which states that if a sequence of row operations will reduce a matrix to the identity matrix, then the same series of operations performed on the identity matrix will produce the inverse. (Error control is maintained internal to the routine with double precision arithmetic though input and output are single precision).

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Deck Name:

INV

Calling Sequence: CALL MTINV (B, ES, N)

Input/Output:

I/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	В	В	NXN	Arg	The N X N array of numbers to be inverted. (single precision)
0	ES	B-1	NXN	Arg	The N X N inverse of B. (single precision)
I	N	N	1	Arg	The dimension of B

Subroutines Required: CHOOSE (Check for singular B)

Functions Required:

None

Approximate Deck

Length:

500 (decimal)

740 (octal)

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                                                 N MATRIX , B, USING THE
                                                                                       OPERATIONS WILL REDUCE THE IDENTITY MATRIX TO THE INVERSE.
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                                       SUBRGUTINE MTINV (B, ES, N )
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2.5.2.1 Subroutine CHOOSE

Purpose:

CHOOSE is utilized in conjunction with MTINV to determine if the matrix (of order less than 6) is sufficiently nonsingular to allow the inverse to be constructed without

excessive numerical difficulty.

Deck Name:

CHSE

Calling Sequence: CALL CHOOSE (A, E, M, N)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	A	A	ихи	Arg	The array of numbers which is being reduced to the identity matrix.
I/0	E	E	NXN	Arg	The inverse being con- structed from A.
I	М		1	Arg	A row counter for the operations being performed on A.
I	N		1.	Arg	Order of the square array A.

Subroutine Required: None

Functions Required: None

Approximate Deck

Length:

200 (decimal) 270 (octal)

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SUBRGUTINE CHGGSE(A,E,M,N) IF THE DIAGGNAL ELEMENT,A(M,M), OF THE MATRIX TO BE INVERTED IS ZERO, THE ROW WITH THE MAXIMAL ELEMENT IS CHOSEN AND INTERCHANGED WITH ROW M.	RECISION A(6,6),E(N) 10 ,5 ,10	(A (N, 1)	M1 = M + 1 $DG 30 I = M1, N$	ABSEL= ABS (A(1,M)) [F(EMAX-ABSEL) 20, 30, 30	20 EMAX = ABSEL 180W = 1	30 CONTINUE	IF(FMAAIU-30/40, 30, WRITE (6,45)	45 FORMAT (28HOSINGULAR MATRIX, NO INVERSE) RETURN	50 DG 60 I=1,N	$B = A(M_1)$	3W•I) = 8	= E(M, I)	m(M,I)		END

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FS305 CHSE		SYMBØL EMAX I RØW		СНОВSE		. FWRD.		EFN 10 70 50	DECK LENGTH

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2.3.5 Subroutine ADDMAT

Purpose:

ADDMAT is designed to add two arbitrary vectors or

matrices of the same order

Deck Name:

ADDM

Calling Sequence:

CALL ADDMAT (A, I, J, B, C)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	А, В	А, В	I (rows) J (columns)	Arg	Two arrays of numbers which are to be added
0	С	C	I (rows) J (columns)	Arg	Matrix containing the sum of A and B

Subroutines Required: None

Functions Required:

None

Approximate Deck

Length:

1

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ADDMO07C ADDMO080 SUBRGUTINE ADDMAT(A,I,J,B,C)

THIS ROUTINE ADDS ADY TWO MATRICES OR VECTORS OF SIMILAR DIMENSIONADDMO020

ADDMO030

DIMENSION A(I,J),B(I,J),C(I,J)

ADDMO040

DO I K=1,I ADDM0C60 ADDMOC90 C(K+L) = A(K+L) + B(K+L) RETURN DG 1 K=1,1 DG 1 L=1,J GNU

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PAGE 172		TYPE							LGCATIGN
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2.5.4 Subroutine SUBMAT

Purpose:

SUBMAT subtracts the I by J array of numbers B from another array (A) of the same order $\,$

Deck Name:

SUBM

Calling Sequence:

CALL SUBMAT (A, I, J, B, C)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	А, В	А, В	I (rows) J (columns)	Arg	A is an arbitrary array to be reduced by a second array of the same dimension (B)
0	С	С	I (rows) J (columns)	Arg	C = A - B

Subroutine Required:

None

Functions Required:

None

Approximate Deck

Length:

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SUBROUTINE SUBMAT(A,1,J,B,C)
THIS RGUTINE SUBTRACTS TWO MATRICES OF SIMILAR DIMENSION

DIMENSION A(1, J), B(1, J), C(1, J)

DG 1 K=1,1 DG 1 L=1,J

C(K,L) = A(K,L) - B(K,L)
RETURN
END

u.	FS305 SUBM			SUBR	STOSUBLE STO	STØRAGE SUBMAT	МДР	11/23/85		PAGE 173
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2.5.5 Subroutine TRANSP (Matrix Transportation)

Purpose:

TRANSP constructs the transpose of an arbitrary array of

numbers

Deck Name:

TRSP

Calling Sequence: CALL TRANSP (A, N, M, B)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	A	A	N (rows) M (columns)	Arg	Array to be transposed.
0	В	ΑT	M (rows) N (columns)	Arg	The array containing the transpose.

Subroutines Required: None

Functions Required:

None

Approximate Deck

Length:

80 (decimal) 140 (octal)

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388			SYMAGL		Ä		Ś		FFN 1 DECK 1

2.5.6 Subroutine CROSS

Purpose:

CROSS constructs the vector product of two arbitrary vectors A and B (in the following order $C = A \times B$)

Deck Name:

CROSS

Calling Sequence:

CALL CROSS (A, B, C)

Input/Output:

1/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	A B	A B	3 3	Arg	The two vectors to be multiplied in the sense A X B
0	С	С	3	Arg	The vector product

Subroutines Required:

None

Functions Required:

None

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CRBS

SUBRGUTINE CROSS (A, 15, C)

DIMENSION A(3), B(3), C(3) C(1) = A(2) * B(3) - A(3) * B(2) C(2) = A(3) * B(1) - A(1) * B(3) C(3) = A(1) * B(2) - A(2) * B(1) RETURN END

390

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						EFN	DECK

2.5.7 Subroutine DOT

Purpose:

DOT computes the scalar product of two 3-vectors

Deck Name:

DOT

Calling Sequence: DOT (A, B)

Input/Output:

I/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	A, B	А, В	3, 3	Arg	The two 3-vectors to be utilized in constructing the scalar product.
0	DOT	А, В		-	The scalar product.

Subroutines Required: None

Functions Required:

None

Approximate Deck

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	3at			SYMBØL F.OOOC		DGT		SYSLAC		EFN	DECK LENGTH IN OCTAL

2.5.8 Subroutine AMAG

Purpose:

AMAG constructs the scalar length of a vector

Deck Name:

AMAG

Calling Sequence: AMD: (A)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	A	A	3	Arg	The 3-vector (in cartesian coordinates) for which the length is desired.
0	AMAG	A	1	-	Vector magnitude.

Subroutines Required: None

Functions Required:

DOT (Scalar product)

Approximate Deck

30 (decimal)

Length:

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SOURCE STATEMENT

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FUNCTION AMAG(A)
DIMENSION A(3)
AMAG = SQRT (DOT(A,A))
RETURN
END

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SID 65-1203-1

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2.6 General Purpose Math Group

In addition to the functions and routines required for algebraic manipulation of vectors and matrices (as presented in the preceding discussions), there are several mathematical functions which are utilized in conjunction with the conic motion formulation (and the related state transition formulation) and in conjunction with the definition of azimuth of the vehicle relative to the tracking station which must be discussed. These routines, due to their general nature and the fact that they are employed at several points in the program, do not logically fall in one of the other main groups. They have, thus, been presented in a separate section on the following pages (no formulation or computational logic due to their simple form).

2.6.1 Subroutine SINH

Purpose:

SINH computes the hyperbolic sine of a single precisio. argument expressed in radians.

Deck Name:

SINH

Calling Sequence:

SINH (X)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I.	Х	X	1	Arg	Single precision argu- ment (expressed in radians) for which SINH is to be evaluated.
0	SINH	sinh	1	_	Hyperbolic sine.

None Subroutines Required:

Functions Required:

None

Approximate Deck Length:

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                                  SINHOC10
                                          SINHOG20
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                                SINH(XIN)
                                                IF(ABS (X)
IF(ABS (X)
       SINHM
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NIX = X

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10 9 SINHOG30 SINHOG40 SINHOD50 SINHOD51 SINHO100 SINHO110 SINHOC 90 S INH00 70 SINHOG80 SINHOG60 (X ** 7)/ 5040. + X - 88.028)10,10,200 - 34657359)20,20,40 ** 31/6. + (X ** 5)/120.0 * (EXP (X) - EXP (-X)) AMOD (X,88.028) SINH = (X ** 3)/6. 1+ (X**9) / 362880. 3

X = AMG GG TG 10

200

END

G0 TG 3C

36 RETURN SINH

40

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2.6.2 Subroutine COSH

Purpose:

COSH computes the hyperbolic cosine of a single precision

argument expressed in radians

Deck Name:

COSH

Calling Sequence: COSH (X)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	Х	Х	1	Arg	Single precision argument (expressed in radians) for which COSH is to be evaluated.
C	COSH	cosh	1	-	Hyperbolic Cosine.

Subroutines Required: None

Functions Required:

None

Approximate Deck

Length:

1.00 (decimal)

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COSHM

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FUNCTION COSH(XIN)

NIX = X

IF(ABS (X) - 88.028) 10,1C,200 10 [F(ABS (X) - .34657359)2C,20,40 20 CGSH = 1. + (X ** 2)/ 2. + (X ** 4)/24. + (X ** 6) / 720. SBURCE STATEMENT

* (EXP (X) + EXP (-X)) 1+ (X**8) / 4032C.

٠ در 11 GØ TØ 30 30 RETURN 4C COSH

AMOD (X,88.028) ., 36 . x = AM6 . GG TG 10 . END 20C

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2.6.2 Subroutine COSH

Purpose:

COSH computes the hyperbolic cosine of a single precision

argument expressed in radians

Deck Name:

COSH

Calling Sequence: COSH (X)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	Х	Х	1	Arg	Single precision argument (expressed in radians) for which COSH is to be evaluated.
0	COSH	cosh	1	_	Hyperbolic Cosine.

Subroutines Required: None

Functions Required:

None

Approximate Deck

Length:

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FS305 C0SHM	FUNCTION COSH(XIN) X = XIN IF(ABS (X) - 88.02 10 IF(ABS (X)3465 20 COSH = 1. + (X ** 1+ (X**8) / 4032C. 30 RETURN 4C COSH = .5 * (GO TO 30 20C X = AMOD (X,88.C GO TO 10 FND

SID 65-1203-1 -403-

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2.6.3 Subroutine ARKTNS

Purpose:

ARKTNS computes the single precision arc tangent (when given the sine and cosine of the angle) and assigns the

angle to the proper quadrant $(-\pi \angle \theta \angle \pi)$ or $o \angle \theta \angle 2\pi$

Deck Name:

ATAM

Calling Sequence:

ARKTINS (N, X, Y)

Input/Output:

I/O	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	N		1	Arg	Fixed point number to identify the range of the are tangent N = 180 -180 \(\text{\Left} \)
I	х	cose	1	Arg	Cosine of angle
I	Y	sin <i>e</i>	1	Arg	Sine of angle
0	ARKTNS	0	1	-	Arc tangent (Y/X)

Subroutine Required:

None

Functions Required:

ATAN (arc tangent function)

Approximate Deck

Length:

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PAGE 23
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SID 65-1203-1 -407-

2.6.4 Subroutine DERAQ

Purpose:

DERAQ is intended to represent the Kronecker delta (i.e., δ_{ij}) and as such has the value of 1.0 or 0.0 depending on the arguments I and J

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Deck Name:

DERQ

Calling Sequence: DERAQ (I, J)

Input/Output:

I/0	FORTRAN Name	Math Name	Dimension	Common/ Argument	Definition
I	I, J	i, j	1, 1	Arg	Two fixed point variables defining the value of.
0	DERAQ		1	-	Kronecker delta.

Subroutine Required: None

Functions Required:

None

Approximate Deck

Length:

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DRAQ0090 DRAQC100 DRAQ0110

DRAQCO10 DRAQCO20 DRAQCO30 DRAQCO40 DRAQCO50 DRAQCO60 DRAQCO70

00000

DERAG IS THE KRONECKER DELTA FUNCTION

FUNCTION DERAG(1, J)

= J NOT EQUAL TO J

0 =

DERAQ = C IF(I-J)

DERAQ = RETURN END

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FS305 DRAQ

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		FUNCTION	I GN DERAQ	TYPE	œ		
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3.0 Accuracy Tests

The program logic has been checked numerically against three precision programs.

- 1) APIIO A general purpose trajectory program prepared for the Apollo program and employing an Encke formulation and an Adams integration logic.
- 2) SPACE A JPL single precision cowell trajectory program employing a 4th order Runge-Kutta integration logic.
- 3) ITEM A Goddard trajectory program employing an Encke formulation.

The results of these tests indicate that agreement can always be obtained through the sixth digit (frequently through the seventh) for integrations covering several orbits of the earth providing that the constants of the programs are compatible. This level of agreement is considered as a proof of the program logic. This conclusion is strengthened when it is observed that the basic logics of the three programs are somewhat different and that in no case could the agreement be expected through the eighth digit due to the restricted word length employed in single precision on the IBM 7094.

4.0 SAMPLE PROBLEM

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4.1 SAMPLE PROBLEM DISCUSSION

Punched paper tapes with tracking data recorded by the Floyd Terminal for passes 6069 and 6070 of ECHO II were provided for the purpose of demonstrating the operation and accuracy of the differential corrections program described on the previous pages. Thus, the discussions which follow will enumerate the procedures involved in construction and solution of this sample problem.

4.2 ORBIT PARAMETERS

Passes 6069 and 6070 of ECHO II occurred on 27 April 1965. Thus, published data for this satellite was searched to determine an estimate of the position and velocity at some epoch prior to this date. This procedure was required to assure that the trajectory could be generated accurately so that the differential corrections process can converge to the desired trajectory.

The Goddard Space Flight Center on 30 April 1965 issued the following information pertaining to 1964 O4-A (ECHO II) in TWX NR 054/301-474-4911 (the true equator of data frame of reference).

Epoch OhOs UT, 20 April 1965

semimajor axis	7528.31 Km
eccentricity	0.02447
inclination	81.450°
Mean Anomaly	113.092°
argument of periapse	34.156°
right ascension of	31.202°
ascending mode	

Accordingly, this information was resolved into the corresponding position and velocity vectors. (Using subroutine POSVEL) the result was:

Epoch OhOs UT, 20 April 1965

```
Radius Vector = -5915.9438 - 2918.1582 3783.0742 (Km)
Velocity Vector = -2.74,44510 - 2.7299969 - 6.0748353 (Km/sec)
```

At this point, this information was updated to an epoch just prior to 6069 by employing the general perturbations program described in SID 1203-3. (The elements themselves could have been updated employing only the secular changes in $\boldsymbol{\omega}$ and $\boldsymbol{\Omega}$. However, this approach was discarded to avoid introducing the slight errors associated with such a process.) The results of this process are:

Epoch 27.63865740, April 1965

Radius Vector = 4952.3943 1406.9609 -5362.9226 Km Velocity Vector = 4.4573218 2.9062537 5.0928345 Km/sec

4.3 REDUCTION OF THE RAW DATA

4.3.1 RAW DATA TAPE

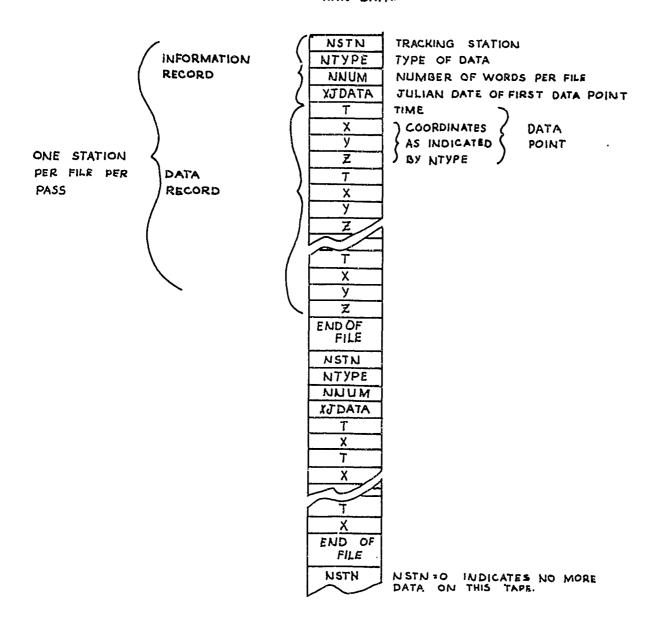
Input data for the sample problem consists of two paper tapes recorded by the Floyd tracking facility containing the following observations for the ECHO II satellite passes 6069 and 6070; elevation and azimuth in degrees, doppler reading in kilo-cycles, a lock-on indicator, and universal time in seconds. Since the IBM 7094 computing system utilized does not have a paper tape input capability, a short IBM 1401 program was written to transfer the data directly to magnetic tape with the format shown in Figure 1 (one physical file per pass). The leading information record for each data file contains the following indicators.

SYI4BOL	DESCRIPTION	PASS 6 06 9	PASS 6 07 0
NS TN	Code indicating the tracking station recording the data (Floyd, see input)	1	1
NTYPE	Code Indicating the type of observed data (range rate, azimuth, elevation)	6	6
MUM	Total number of words per file. (This was determined by the 1401 program in transcribing the data from punched paper tape)	3564	3392
XJDATA	Julian date (zero hour UT) of the first observation for each file. (27 April, 1965)	(24)38877.5	(24) 38877.5

A third file containing NSTN equal to zero indicates to the program that all data has been read from the tape.

Graphical representation of the raw data is presented in Figure 2 through 7 (the broad line apparent in these figures is in reality a series of points or plotting symbols). Examination of Figure 6 will disclose random irregularities of azimuth observations being recorded 360 degrees out of phase, especially prevalent for angles approaching 360 degrees (e.g., +354° recorded as -6°). These points were adjusted in the preliminary processor immediately prior to smoothing the data segment to assure that a consistent convention is employed in recording the observed and computed values of the data.

INPUT TAPE FORMAT RAW DATA.



- . FORTRAN I
- . BINARY MODE
- · MULTI PHYSICAL FILES
- LOGICALLY PACKED TIME AND COORDINATE DATA

This figure also serves to illustrate a data format which is not generally acceptable to the program. Although most of the data are observed to be sequenced chronologically, a few recording errors of the time are evident. At this time no attempt has been made to determine if such errors exist. Rather, it is considered to be the user's responsibility to assure that such errors have been eliminated.

Fortunately for this problem these errors do not affect the solution due to the manner employed in smoothing the raw data over short intervals of time. However, this circumstance exists only because the erroneous time values did not occur at the midpoint of a 20 consecutive point strip of data (see subroutine FIT in the preprocessor SID 65-1203-2). Since such fortuitous arrangement of errors cannot be guaranteed, remedial steps should be taken in recording the data.

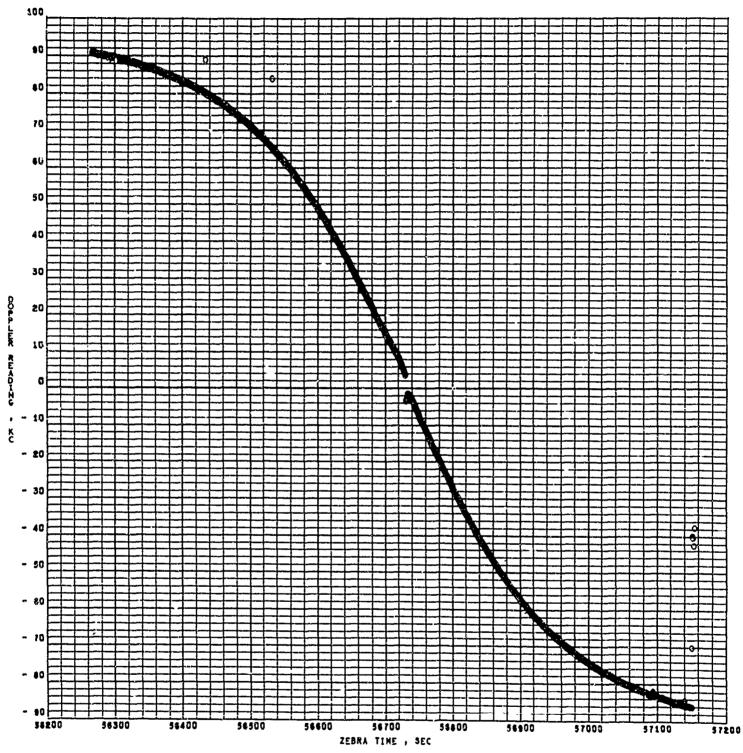


Figure 2 FIRST RAW DATA FILE
DOPPLER READING VS TIME
(Echo II, pass 6069)

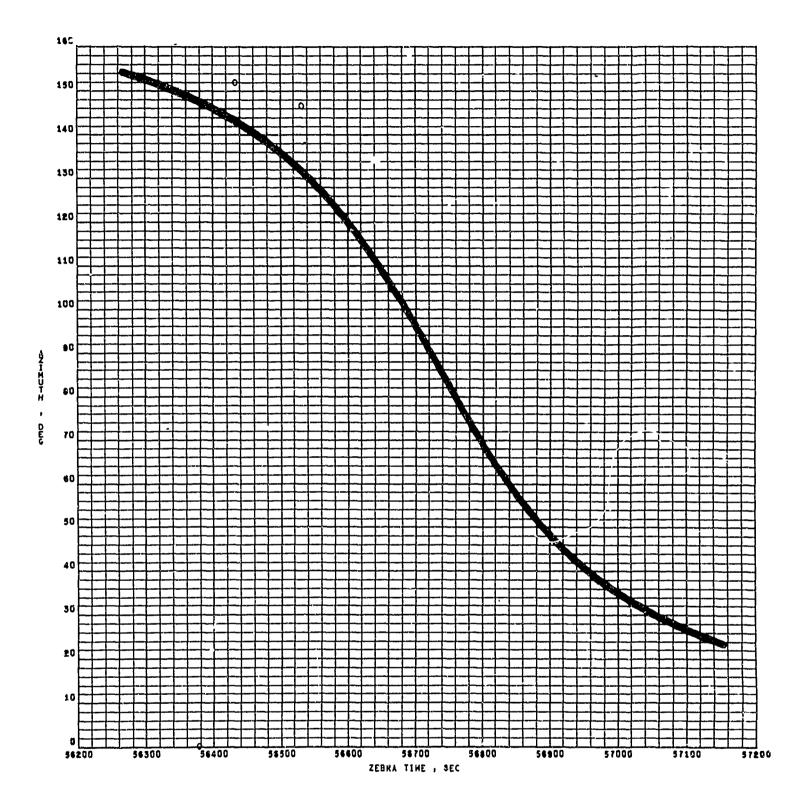


Figure 3 FIRST RAW DATA FILE AZIMUTH VERSUS TIME (Echo II, pass 6069)

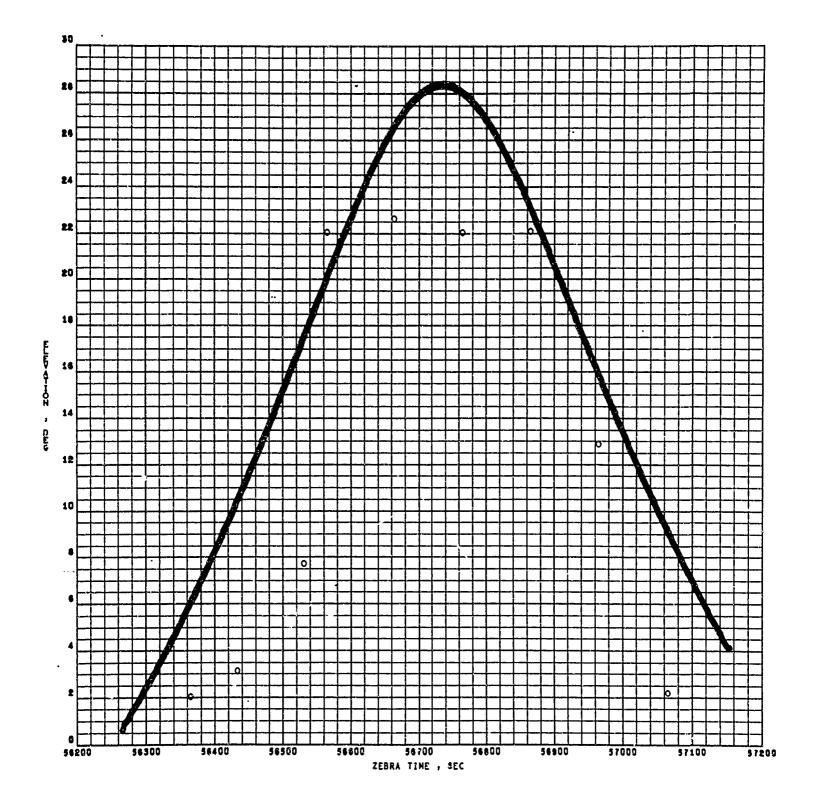


Figure 4 FIRST RAW DATA FILE
ELEVATION YERSUS TIME
(Echo II, pass 6057)

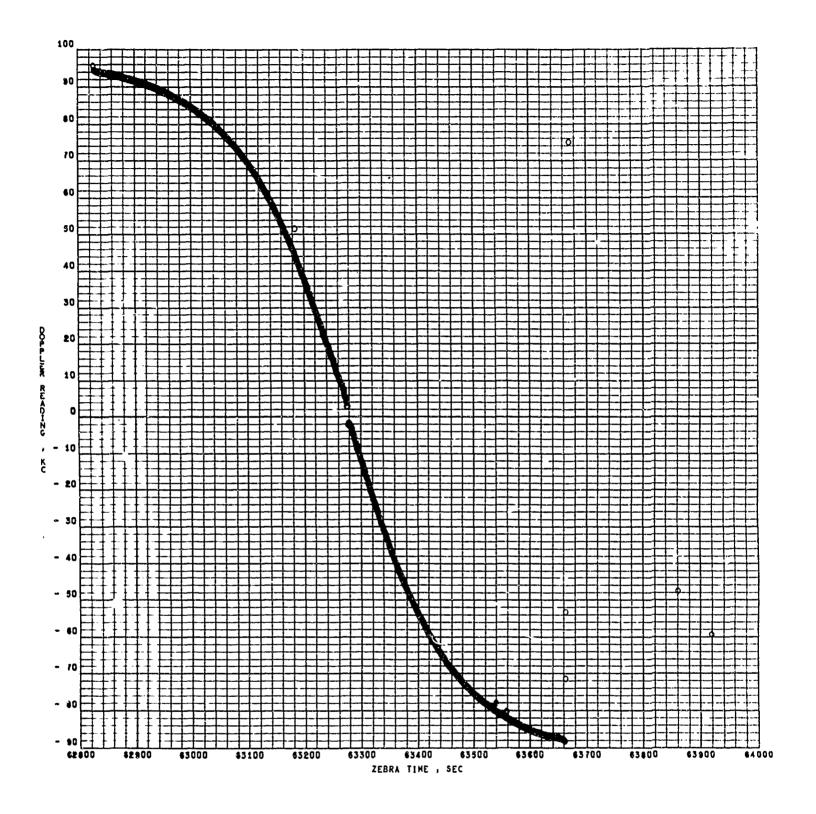


Figure 5 SECOND RAW DATA FIVE DOPPLER READING VERSUS TIME (Echo II, page 6070)

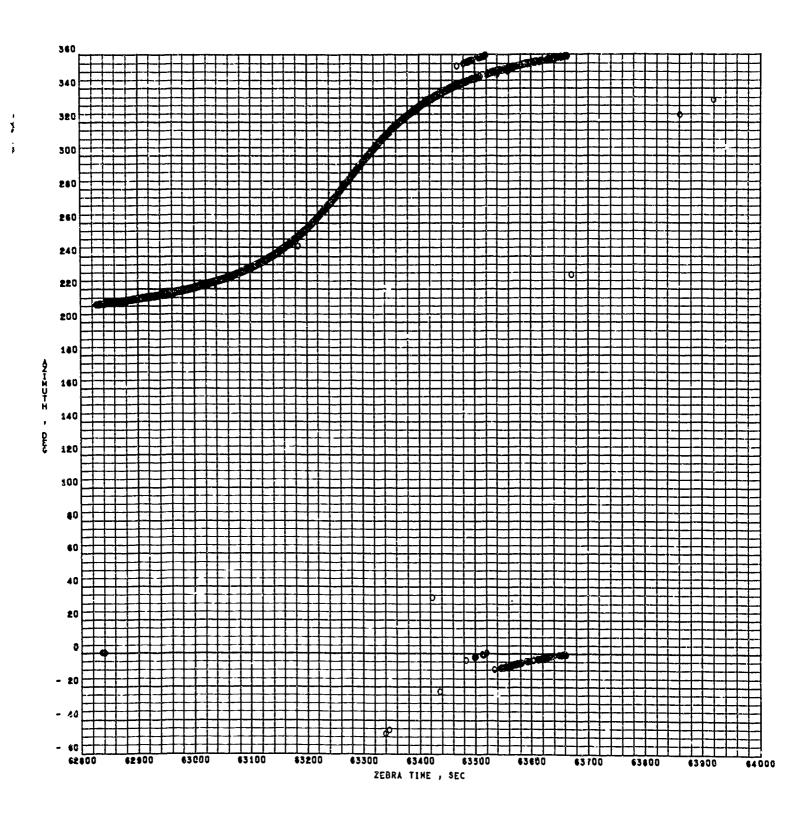


Figure 6 SECOND RAW DATA FILE

• ANIMUTH VERSUS TIME

(Echo II, pass 6070)

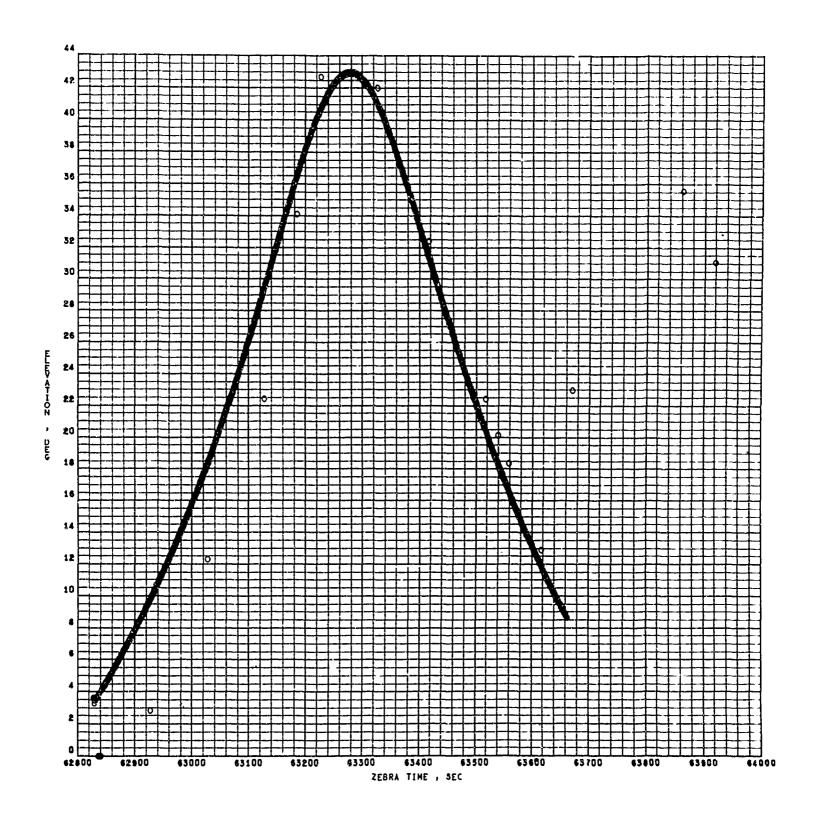


Figure 7 SECOND RAW DATA FILE ELEVATION VERSUS TIME (Echo II, pass 6070)

4.3.2 Variable Dimensions for Preprocessor

The required values for the variable dimensions were determined by the procedure outlined below. (See "Variable Dimensions" and "Storage Limitations" in the "Program Operation" section of SID 65-1203-2)

AA(4, MAXAA): This array must be large enough to hold the smoothed points corresponding to a single raw data file. The largest raw data file contains 3564 words. The number of words per information record is 4, and there are 4 words per data point (time, doppler reading, azimuth, elevation.) Thus, the number of raw data points per file is (3564-4)/4 = 890. Now the smoothing routine reduces 20 raw data points to a single smoothed point, therefore, since 890/20 45, MAXAA was dimensioned by 50.

A(6, MAXA): The primary purpose of this array is to receive the smoothed data from the AA array. Since MAXAA was set to 50 and there are two files of data, MAXA was set to $2 \times 50 = 100$. If there had been storage limitations, MAXA could have been reduced (the smoothed points would then be temporarily stored on tape). However, this array must be large enough to hold the smoothed points corresponding to a single raw data file.

STN (6, MAXSTN): The usual criterion for dimensioning this array is number of raw data points per file. The sample problem has MAXSTN = 1000.

This procedure is outlined here since more demanding tasks will undoubtedly be presented to the program during its period of use. The sample, in no way taxes the capability of the program. Before passing it is noted that these variables can be assigned large values to assure operation for most problems and that should these limits ever be violated a message will be printed as to the nature of the problem and steps required to correct it.

4.3.3 Input Data Load Sheet for the Preliminary Processor

DATA
DECIMAL
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0
FIXED
FORTRAN

	DECK NO. DATA P	PROGRAMMER J. DOE	DATE PAGE/of/JOB_NO
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4.3.4 Preprocessor Output

Primary output of the preprocessor is a magnetic tape read directly by the differential corrections program (a format shown in Figure 8). However, several print options exist (see SID 65-1203-2). These options include

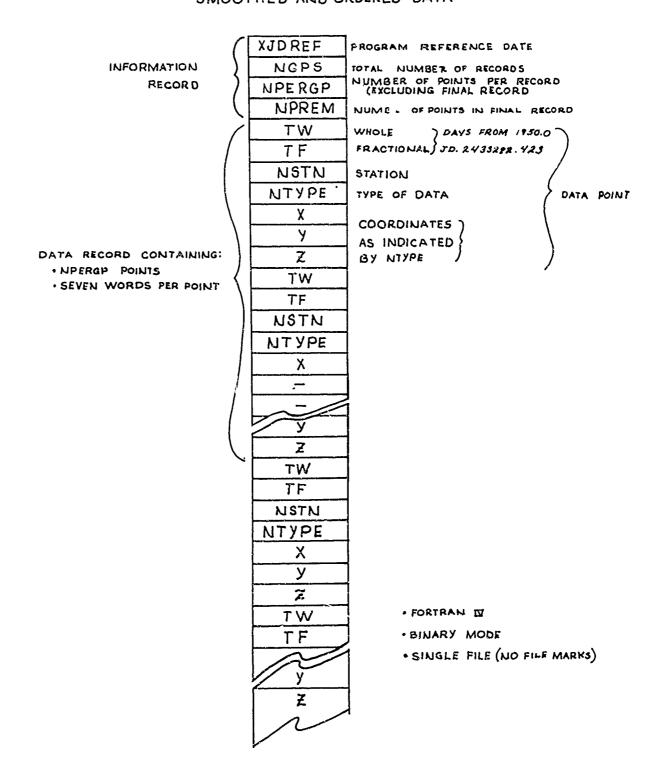
printing of the raw data printing of smoothed data

Since the raw data were provided in graphical form on revious pages, the first option was not mechanized. The second option was however employed.

Accordingly, smoothed and sorted data corresponding to the curves presented earlier are presented in the following table.

FIGURE 8

FS4-305 A OUTPUT TAPE FORMAT SMOOTHED AND ORDERED DATA



	001	10000		
7	.2042582 .3745499 .5596453	. 1 160617 7E . 1 1891 939 6E . 1 6143 649 E	.1845920 .2088303 .2335594 .2591801 .2851926	0.36429025E 0.38977195E 0.43683925E 0.45874582E 0.47298806E 0.48529038E 0.495264039E 0.49512568E 0.49512568E 0.49512568E 0.49512568E 0.43529823E 0.43529823E 0.43529823E 0.33960551E 0.33960551E 0.26361281E
>	.26872827E 0 .26688221E 0 .26493267E 0	.262590393E 0 .26066798E 0 .25825329E 0 .25546699E 0	.24952876E 0 .24613850E 0 .24243607E 0 .23834637E 0 .23388626E 0 .22894212E 0	0.21759135E 01 0.21759135E 01 0.20397824E 01 0.19625130E 01 0.18795771E 01 0.16992925E 01 0.16037576E 01 0.16037576E 01 0.15069345E 01 0.14105670E 01 0.12258930E 01
×	.59763414E 0 .59238771E 0 .58662044E 0	.57199250E 0 .57199250E 0 .55289957E 0 .55197529E 0	0.52724449E 0 0.51208623E 0 0.49402078E 0 0.47447134E 0 0.4524100E 0	-0.35670021E 01 -0.35670021E 01 -0.29186757E 01 -0.29186757E 01 -0.20506103E 01 -0.15723250E 01 -0.15723250E 01 -0.15468145E 00 0.15468145E 00 0.15468145E 00 0.21524288E 01 0.21524288E 01 0.30042937E 01 0.37062306E 01 0.37063770E 01 0.48898364E 01 0.46992580E 01 0.46992580E 01
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OM REF DATE) FRAC	.72833095 .72856221 .72879396	. 72902522 . 72925649 . 72948823 . 72973142	.73019443 .73042569 .73065696 .73088870 .73111997	0.73181472E 0.73204599E 0.73250899E 0.73250899E 0.73297200E 0.73343501E 0.73343501E 0.7345929E 0.73486103E 0.73482404E 0.735281259E 0.73528132E 0.73598132E 0.73544433E 0.735444433E 0.735444433E
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	0.58365851E 00 0.55149679E 00 0.47070983E 00 0.47070983E 00 0.47070983E 00 0.47070983E 00 0.41334471E 00 0.37050498E 01 0.37214869E 01 0.37214869E 01 0.37291791E 01 0.37391791E 01 0.3785956E 01 0.38899242E 01 0.38899242E 01 0.40661716E 01 0.40661716E 01 0.42834608E 01 0.42834608E 01 0.42834508E 01 0.43715566E 01 0.4371526 01 0.43785511E 01 0.45997658E 01 0.5560537E 01 0.5560537E 01	0 3/00006/6•
×	0.50347922E 01 0.51708542E 01 0.52970178E 01 0.52970178E 01 0.553998458E 01 0.56384577E 01 0.47999006E 01 -0.61606917E 01 -0.61606917E 01 -0.59120244E 01 -0.59120244E 01 -0.59120244E 01 -0.59120244E 01 -0.59120244E 01 -0.59120246E 01 -0.59120246E 01 -0.5912026E 01 -0.5912026E 01 -0.5912026E 01 -0.5912026E 01 -0.591203812E 01 -0.5912026E 01 -0.5912026E 01 -0.50108971E 01 -0.30108971E 01 -0.30108971E 01 -0.30108971E 01 -0.30108971E 01 -0.31154039E 01 0.20561499E 01	• 324451
TYPE		0
STN		•
REF DATE	0.73690734F 00 0.73737035E 00 0.73740162E 00 0.73760162E 00 0.737806462E 00 0.73809589E 00 0.73809589E 00 0.80430303E 00 0.80455766E 00 0.80502067E 00 0.80502067E 00 0.80571494E 00 0.80571494E 00 0.80571494E 00 0.805714996 00 0.80571996 00 0.80571996 00 0.80571996 00 0.805729E 00 0.805729E 00 0.805729E 00 0.805729E 00 0.805729E 00 0.80647896E 00 0.80647896E 00 0.80647896 00 0.80647896 00 0.80647896 00 0.80918727E 00	• 81 080 / 56E
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L INE	SID 65-1203-1 -42	

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E IS 2433282.4	7	.5406530	.5168388	.4764578	.4374830	.4002951	.3659490	330	.2996550	.2696790	.2411121	.2152528	.1884328	.1638856	.1512624	.1508330	
REFERENCE DAT	>	8274211E 0	.58652009E.0	.59266864E 0	.59959253E 0	.61105295E 0	.62233641E 0	0.61067523E 01	.61381948E 0	.61675483E 0	.61941655E 0	.62182120E 0	.62402965E 0	.62601354E 0	*62716799E 0	.62730221E 0	
O_AND_SØRTED DATA_**	×	376059E	.41232708E_0	.44255949E 0	.46824166E 0	.48986638E 0	.50924568E 0	3E 0	.53777257E 0	.54960118E 0	.55948447E 0	.56793135E 0	.57369688E 0	.57772977E 0	.47101759E 0	.35057233E 0	
W.	TYPE	9	9	9	9	ó	9	9	9	9	9	9	9	9	9	9	
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	FROM	04	04	24	74	74	74	94	74	04	74	74)4) 4)4)4	
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28	L INE							81									DUMP

4.4 Sample Differential Correction Program Input

The input for the sample problem will be discussed in relation to the significance of the data and its location in the fundamental data array. All quantities which can be readily changed will be discussed though some, as will be noted, will not be changed from their preprogrammed values.

Reference to the map of the fundamental array (Appendix 1) will varify the DATA locations given in the following pages.

4.4.1 Physical Constants for Math Model

Equatorial Radius	DATA (1)	As	Programmed
Polar Radius	DATA (2)	As	Programmed
Coefficient J	DATA (3)	As	Programmed
H	DATA (4)	As	Programmed
D	DATA (5)	As	Programmed
GM for the Earth	DATA (6)	As	Programmed
Spin Rate for the Earth	DATA (7)	As	Programmed
GM for the Moon	DATA (8)	As	Programmed
QM for the Sun	DATA (9)	As	Programmed
The astronomical Unit	DATA (10)	As	Programmed

4.4.2 Satellite Data for ECHO II

Mass (assumed) Area (assumed) Drag Coefficient (") Reflectivity (") Position Vector X Y Z Velocity Vector X Y Z	DATA (16) DATA (17) DATA (18) DATA (19) DATA (20) DATA (21) DATA (22) DATA (23) DATA (24) DATA (25)	1.0 100.0 2.0 1.0 4952.3943 1406.9609 -5362.9226 4.45732].8 2.9062537
-	Time Relative to 1950.0	5.0928345

Oh April 27 1965 = 2438877.5 Epoch = .63865740 J.D. of Epoch 2438878.13865740

Reference Epoch 2433282.423 5595.71565740 days

TW	DATA (26)	5595. days
TF	DATA (27)	.71565740 days

4.4.3 Control Options

WINDEX	DATA (28)	1.
CHECK	DATA (28) DATA (29) DATA (30)	1.
GONO	DATA (30)	1.
CODUMP	DATA (31)	1.

4.4.4 Station Identification Card (SIC)

Station one (Floyd) will be utilized Stations two through ten will be deleted

4.4.5 Station Data*

(rad)	DATA (36)	.75393225
(rad)	DATA (37)	4.96824718
(Km)	DATA (38)	.17927
	DATA (39)	As Programmed
ection	DATA (77)	As Programmed
Latitude	DATA (87)	As Programmed
Longitude	DATA (88)	As Programmed
Altitude	DATA (89)	As Programmed
Range	data (176)	As Programmed
Range-rate	DATA (177)	.Ol **
Azimuth	DATA (178)	As Programmed
Elevation	DATA (179)	As Programmed
	(rad) (Km) ection Latitude Longitude Altitude Range Range-rate Azimuth	(rad) DATA (37) (Km) DATA (38) DATA (39) DATA (77) ection DATA (77) Latitude DATA (87) Longitude DATA (88) Altitude DATA (89) Range DATA (176) Range-rate DATA (177) Azimuth DATA (178)

COVARIANCE MATRIX FOR ERRORS IN $\hat{\mathbf{r}}$ AND $\hat{\mathbf{v}}$ 4.4.6

The data for the elements imply that estimates of the errors in these parameters are approximately:

3
$$G_{AC}$$
 = .1 km
3 G_{AC} = .0001
3 G_{AC} = $\frac{0.01}{57.3}$ rad
3 G_{AM} = $\frac{0.01}{57.3}$ rad
3 G_{AM} = $\frac{0.01}{57.3}$ rad
3 G_{AM} = $\frac{0.01}{57.3}$ rad
or
$$G_{AC}$$
 = 1 x 10⁻³

$$G_{AC}$$
 = 1 x 10⁻⁹

$$G_{AC}$$
 = .35 x 10⁻⁸

$$G_{AM}$$
 = .35 x 10⁻⁸

$$G_{AM}$$
 = .35 x 10⁻⁸

See subroutine INPUT and Appendix 1.

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From conversations with RADC personnel it was learned that the Doppler data from which R was computed were not as precise as had been assumed earlier. No firm estimate of variance was available, however.

Now, since this set of errors is relatable directly to the set of errors $d\vec{r}$ and $d\vec{v}$ in rotating coordinates by the matrix equation of Table 1, and since the rotating and inertial coordinates are relatable by a linear transformation, the covariance matrix for $d\vec{r}$ and $d\vec{v}$ can be evaluated as follows:

$$\left\{ \Delta X \right\} = A \left\{ \Delta E \right\}$$

$$\left\{ \Delta X' \right\} = T \left\{ \Delta X \right\} = TA \left\{ \Delta E \right\}$$

$$\mathcal{E}(\Delta X' \Delta X'^T) = TA \mathcal{E}(\Delta E \Delta E^T) \Delta^T T^T$$

where $\Delta X = \left\{ \begin{array}{c} d \, \overline{r} \\ d \, \overline{v} \end{array} \right\}$ rotating coordinates

 $\Delta x' = \left\{ \begin{array}{c} d \stackrel{?}{r} \\ d \stackrel{?}{V} \end{array} \right\}$ cartesian coordinates

A = matrix of Table 1

$$\Delta \mathbf{E} = \left\{ \begin{array}{c} \Delta \alpha \\ \Delta \mathbf{e} \\ \vdots \end{array} \right\}$$

7 = Transformation from rotating to inertial coordinates

$$\Delta M = -\sqrt{\frac{M}{\alpha^3}} \Delta t_P$$

But $\mathcal{E}(\Delta X'\Delta X'')$ is not the matrix required because it is valid for the initial epoch rather than the updated epoch. Thus, one final transformation is required

$$\Delta X_2' = \varphi(t_2, t_1) \Delta X_1'$$

and

$$\boldsymbol{\mathcal{E}}(\Delta X_{2}^{\prime} \Delta_{2}^{\prime T}) = \varphi(t_{2}, t_{1}) \boldsymbol{\mathcal{E}}(\Delta X_{1}^{\prime} \Delta X_{1}^{\prime T}) \varphi^{T}(t_{2}, t_{1})$$

where $\varphi(t_2, t_1)$ is the state transition matrix. For the present purposes $\varphi(t_2, t_1)$ can be assumed to be adequately approximated using a conic reference trajectory (see subroutine TRANS).

Table 1

POSITION - VELOCITY SENSITIVITIES FOR ELLIPTIC ORBITS

	ab	G D	م ط به	., p	a p	વ p
	0	0	g 500 7 5001	0	0	-VsINLSINZB
	0	٤.	0	0	0	0
FOSTITON - VELOCATI SENSTITYLIAES FOR EDATITION ONDITS	0	0	rainil ctn'i ctn' 3-1]	0	0	-y cos Alsini + ctni sin B
4 001111111110 .	-a2en SINE	- pan r(1-e²)12	0	ualen sin E r3 V	-Va2n(1-e2)2B	•
FORTITON - APPOCE	-a cos E + a2e SIN E	a SINE (1+P/r)	0	40 cos E - 402 sinte	-avcosou + ev r tan 8 + tan 8(1-e2)	0
	Z - BacksinE	-3 PM 2 [1-82]4	0	= -V + 3 Ea M L SINE 2a Z r3V	-3 Vam (1-e2) 2 B	0
	ر م ا	rdę	rd स्	- 20	۸۹ ه	βРЛ
				-433-		

-433-

SID 65-1203-1

i = inclination

• = true anomaly

E = eccentric anomaly
a = semi-major axis
e = eccentricity
p = semi-latus rectum

v = velocity δ = flight path angle β = azimuth

 $\mathbf{B} = l - \mu / r v^2$ L = latitude

M=A(t-tp)

r = radius

Adopting the notation T_X () etc. to mean a positive rotation about the X axis through the angle \propto , the transformation of position errors becomes

$$d\vec{r}' = \frac{T_Z(-e)}{T_Z(-e)} \frac{T_Z[-(\theta+\omega)]}{T_Z[-(\theta+\omega)]} d\vec{r}$$

$$= R(\Omega, i, \varphi) d\vec{r}$$

similarly

$$d\vec{v}' = T_2(-\Omega) T_2(-\lambda) T_2[-(\theta+\omega)] T_2(-90+\delta) d\vec{v}$$

$$= R(\Omega, \lambda, \overline{\lambda}) d\vec{v}$$

where

thus, T becomes

$$T = \begin{bmatrix} R(e,i,\varphi) & o \\ o & R(e,i,\Xi) \end{bmatrix}$$

Therefore, in successive steps, the matrix A is

.00000000E-38 .00000000E-38 .55403090E 04 .000000000E-38 .000000000E-38
.000000006-38 .73450973E 04 .000000006-38 .000000006-38
.19037164E-01 .00000000E-38 .74557372E 01 .00000000E-38 .00000000E-38 -47498852E 04 .18864880E-04 .00000000E-38 .17980426E-03 .00000000E-38
-19037164E-01 -74557372E 01 .000000006-38 .18864880E-04 -17980426E-03
-74851830E 04 -15902172E 04 -000000000E-38 -74174433E 01 -79840893E 00 -000000000E-38
.96791741E 00 730336841E 01 .00000000E-38 748750563E-03 73161020E-04

The matrix T is

-84584028E 00 .14867248E 00		8896 E 3251E	8 20	8 6	.00000000E-38
.51229940E 00	.76966985E 00	-38099555E 00	.00000000E-38	.00000000E-38	.0000000E-38
.00000000E-38	.00000000E-38	.000000000E-38	.14867248E 00	*85463445E 00	Φ.
.0C000000E-38	.00000000E-38	.0000000E-38	:84584028E 00	₹37052683E 00	₹38374998E 00
.00000000E-38	.00000000E-38	.00000000E-38	.51229940E 00	-36374413E 00	7139

The matrix φ (t2, t1) is

	90 =				
.34866917E	.30287280E	602591	12960317	71533289	522150
05	90	90	03	03	6
.16155360E	.13640126E	2259	8357696	2316204	871777
05	90	90	03	03	C
.16161649E	.13796138E	34	35202	40901	44926
02	03	03	00	00	00
-19915249E	316	-90303723E	.73079533E	.40339436E	-22275929E
02	03	03	00	00	00
.16143082E	18317	.69946113E	≈56555799E	-31196560E	.17163150E
02	03	04	01	00	00
43679	6864938	S	70	3281701	.34813951E

SID 65-1203-1

The covariance matrix for the initial $(t=t_1)$ errors in the inertial coordinate system is:

- 23945993E-07 -34567335E-04 .387284165-04 .39491969E-07 .51824178E-07 -22894314E-04 .23823809E-06 - 2394593E-07 -,64302088E-05 -13488413E-06 -,80932066E-04 .10635378E-03 .29521933E-04 -72766497E-04 .23561947E-04 .89978761E-07 - 13488413E-06 .39491969E-07 .17717868E 00 .23561947E-04 -64302088E-05 .38728416E-04 .47253023E-01 .26999317E-01 -72766498E-04 .16503310E 00 .10635378E-03 -34567335E-04 .26999316E-01 -43109424E-01 .29521933E-04 -80932066E-04 .10150787E 00 - 22894314E-04 .47253023E-01 -, 43109424E-01

= t2 and the covariance matrix for the errors in the inertial coordinate system for t

.23150944E 00 -10318048E-03 -18713211F-03 ,58000710E-04 .43026154E-02 .43270175E-01 -. 78504921E-02 -41270284E 00 -. 771361 JOE-01 33342622E-03 .18400949E-03 -10318049E-03 00 00 .60501508E-03 .33342621E-03 -18713211E-03 -14051295E-01 -14017666E -74853903E 03 00 .17489094E .17336036E .92633961E -41270283E .23150944E -74853902E 01 02 03 -14017667E 00 -,77136103E-01 .43270178E-01 ,32695791E .17336038E .31658305E 00 01 02 -, 78504923E-02 -. 14051295E-01 .43026156E-02 .17489095F .45852944E .31658304E

These data must be read into the differential corrections program column-wise. (The digital computer stores elements of A_{ij} in a single subscripted array $a_{11}, a_{21}, a_{31} \cdots a_{n1}; a_{12}, a_{22}, a_{32} \cdots a_{n2}$; etc.), thus

P₁₁ = DATA (355) P₂₁ = DATA (356) P₃₁ = DATA (357) P₄₁ = DATA (358) P₅₁ = DATA (359) P₆₁ = DATA (360) P₁₂ = DATA (361)

4.4.7 Input Data Load Sheets for the Sample Problem

As was noted in the discussion of subroutine IMPUT, most of the data required for program operation can be prerecorded (in fact data for a check network is presently provided within the program). As was also noted in the discussion of IMPUT and REED, these data will not be affected by inputting the desired data unless new data are assigned to the locations presently occupied by these numbers in the common array (see Appendix 1). Thus, only the following data are required (the load sheets are in the proper format and should be copied).

FIXED 10 DIGIT DECIMAL DATA FORTRAN

DATE PAGE / of 4 JOB NO.	DESCRIPTION DO NOT KEY PUNCH	This card (The SIC) must	he the first card in the	data deck after the system	control card identifying the data	for the sample This card indicates	that only the FLOYD terminal is operative	locations of first piece of data on cards in the data array	assumed mass of satellite (Kg)		assumed drag coefficient	80 assumed reflectivity		location	Y component of position (Km)	Y companent of position (Km)	7 compenent of position (Km)			location	i component of velocity (Km/sec)	y component of velocity (Km/sec)	F component of velocity (Km/sec)			
MMER	IDENTIFICATION					73	DATA					7.3	DATA					73 80	D. A. T. A 3					73	D. A. T. A.	
DECK NO. PROGRAMMER		0 7 8	0	C	O			9 /	0 /	.00/	2	0 /		20	4664.3825	1223.8631	2			23	4.7481037	2.9870220	4.7656496			
1	÷38	لتا	2	52	37	ê.	اقا		<u></u>	25	37	\$	لقا	لتا	<u>r</u> S	ID 6	5-1:	\$03 -	<u>5</u>		<u>=</u>	52	31	<u>6</u>	<u></u>	

FORTRAN FIXED 10 DIGIT DECIMAL DATA

	DECK NO PROGRAMMER	MMER	DATE 2 PAGE 4 of JOB NO.
	NUMBER	IDENTIFICATION	DESCRIPTION DO NOT KEY PUNCH
	2.6		10ca +,on
<u> </u>	5 5 9 5		TW (days from 2433282.423
<u>શ</u>	7/568888		TE Fraction of Day
[34	/		WINDEX (C, V = cartesian)
<u>\$</u>		73.80	CHECK "Check tracking stations at each pant on Ingectory
لق		DATAS	GONO (write r. V each time)
<u>[-]</u> [35,5		7
<u>r</u>	45852944700		Ry Km²
<u>3</u>	31658304701		
31	17489095102		
<u>\$</u>][-14051295-01	73	
9	- 78504923-02	0 4 7 4 6	
ا لـــا 3	360		
TD 6	43026156-02		B. Km2/5RC
	31668305+01		
	32695791102		
	17336038103	73	
19	-14017667400	0.4.7.47	
انا	365		0
	1-77136103 01		Pez Km²/sec
<u>প্র</u>] [39-	13270178-01		Pez Km²/sec
	17489094+08		
\$	17336036+03	73	
Ē	92633961703	DATA. B	
	Form 114-C-17 Rev. 7-58 (Vellum)	4	

DATA
DECIMAL
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0
FIXED
FORTRAN

DECK NO.	PROGRAMMER	MMER	DATE	PAGE 3 of 4 JOB NO.
NUMBER	ER	IDENTIFICATION	DESCRIPTION	DO NOT KEY PUNCH
	370		lacation	
-74853	902700		Pr.	Km 2/Sec
-41270	283+00		200	Km2/sec
23.150	944 + 00		23	Km 2/5ec
-14051	295-01	73	Pue	K m 2/sec
-14017	666+00	DATA. 9	P34	Km²/sec
	375		location	
- 74853	903700		2.4	Kn2/sec
60501	508-03			Km 2/3 # c 2
33342	621-03			Km2/sec2
-18713	211-03	73.		Km2/sect
-78504	921-02	DATA 10		Km2/5ec
	380		location	
-77136	10-001			Km2/sec
-41270	284400			Km2/52c
33342	622-03			Kn 2/ sec 2
18200	9 + 9 - 03	73.	Per	Km²/sec²
-10318	049-03	D.A.T.A. 1.1		Km 2/36L2
	385		7	
430261	154-02			Km2/sec
43270	175-01		P24 ,	Km2/5ec
23150	944+00			Kn 2/5cc
- 18713	211-03	73.		Km2/sec ²
-1.03.1.8.	048-03	0 A T A 1.2		Km2/sec2
or 111-5-17 Sev. 7-58 (Vellum)				

Form 111.-C-17 Gev. 7-58 (Vellim)

FORTRAN FIXED 10 DIGIT DECIMAL DATA

DATE PAGE 4 of 4 JOB NO.	DESCRIPTION DO NOT KEY PUNCH	location	Pub Km2/sec2				Control Card to indicate that numerical	data are complete and to initiate input	of station name data				Control Card to indicate that all data	have been provided									
MMER	IDENTIFICATION				73 80	DATA 13					73	DATA 14					73	D.A.T.A. 15				73	
DECK NO. PROGRAMMER	NUMBER	3.9.0	25 58000710-04	37	2	(19	6 6 6	13	25	37		19	6 6 6 6	13	25	37	49	19	- 144 E-1	25	37	49	19

Form 114-C-17 Rev. 7-58 (Vellum)

Five notes are worthy of attention before this discussion ends.

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- 1) The SIC must be the first physical card in the data deck.
- 2) The 999 control card must follow all numerical data.
- 3) The 9999 control card must follow the station name data even if there are no changes (as in the case of the sample).
- 4) The order of the cards following the SIC and preceding the 999 card can be arbitrary since a location is provided with each group of data.
- on the exception of the locations and data provided on the SIC, all numbers are floating point. These floating point numbers can be expressed with a decimal point (as on card 2) or without (as on cards 6-13). However, in the latter case, a decimal is assumed to be located between the first two locations of the field (i.e. before the first digit) and the last 3 locations of the field must contain the exponent of 10 which properly defines the number in question.

4.4.8 Program Output

The differential corrections program was utilized in conjunction with the data of the preceding pages to compute the orbit of ECHO II. The results of this effort will be presented in their entirety to facilitate checkout on other systems and to demonstrate program operation.

However, before presenting these data, it is felt advisable to discuss several problems which were encountered. First, the trajectory as computed from the data provided, checked the Goddard estimate of this time with negligible error and the observed values of azimuth and elevation to within one-half of a degree after seven days of prediction. This fact implied again a good level of accuracy. But, the computed values of range-rate failed to show this level of agreement. This fact was not considered entirely unreasonable at the time.

Second, reference to the raw data disclosed that the range-rate as recorded exhibited a discontinuity of approximately 2.6 Kc at the time the doppler changed signs. This jump corresponds to approximately 0.172 Km/sec, and thus could explain the range-rate disagreement which was experienced if it could be ascertained how this correction should be applied; (i.e., is the positive segment of doppler correct, the negative correct, or are both in error?). Regardless, however, the data are in error and will affect the results in two distinct ways:

- Since the data are biased, the filter process as coded, is not correct (biases are assumed to have been subtracted from the observed data).
- 2) Since the data are to be processed with the biases included, an oscillatory nature of the solution is to be expected (under the assumption that neither branch of the doppler curve is correct).

Third, since the range-rate data was assumed to be in error, a call was placed to RADC (in the person of Mr. Frank Braddley) to ascertain the level of accuracy previously obtained by RADC in range-rate measurements. No precise information was obtained, though it was indicated that the accuracy was subject to question. For this reason, reference was again made to the raw data to determine whether variance data earlier assumed for range-rate data were reasonable. The results of this review indicated that these earlier data should be replaced with an estimate of variance on the order of .0001 Km²/sec². Therefore, these modifications to the data enumerated in the previous sections have been made.

At this point, refer to the sample problem presented on subsequent pages (pass 6069 of ECHO II) and note that

1) All data utilized in the program are printed for reference during checkout.

- 2) The operation of the trajectory, integration and tracking groups is demonstrated.
- 3) The behavior of the filter is demonstrated.

Now, note that after the trace of the covariance matrix for estimation errors has been reduced (the initial errors are quite large since they have propagated for approximately 8 days) and orbital elements begin to be printed for the rectified (corrected) orbit (U.T. = 56616. sec), there is a steady change in the elements "a" and "e." The first printed values lie somewhat below those predicted by Goddard (about 1% in semi-major axis and 10% in eccentricity), but as subsequent points are processed the solution is attained, passed, attained again, and finally passed for the second time.

As is apparent, the process is tending to converge, though the rate of convergence is less than originally anticipated. The observed rate of convergence is believed to be affected by two distinct factors. First, the nature of the doppler data itself will preclude exact convergence and may introduce an oscillatory motion in the solution. Second, the "memory" of the system is slight. In the way of explanation, the history (effect) of all previous data points is carried in the covariance matrix for the estimation errors. This matrix in turn was allowed to "deteriorate" for almost eight days following the last "fix" on the satellite in the sample problem though, in reality, more recent estimates of this matrix probably existed. Thus, while the trajectory itself could be updated with reasonable accuracy from the prescribed epoch of 20 April 1965, it is unlikely that a "true" data reduction problem would be subjected to errors as large as those utilized in the sample except for the initial phases of the problem (i.e., immediately following injection). Rather, it is expected that the estimation errors at the epoch of 27 April 1965 were probably similar to those constructed for the epoch of 20 April 1965. This change in the sample problem would reduce terms in the assumed covariance matrix by terms ranging from 103 to 104, and would reduce the effect of the differences in the observed and computed values of the data by the same factors, thus allowing the trajectory of ECHO II to be corrected with precision. To illustrate this conclusion, the reduced data for an epoch near the final data point is presented in the following table for this variation of the sample problem.

TABLE 2

FLLIPTIC CRBIT ELFMENTS

SEMIMAJOR AXIS	(KM)	=	0.75307251F 04
ECCENTRICITY		=	0.24977477E-01
TRUE ANOMOLY DATE	(DEG)	=	0.14263121F 01
R ASC OF ASC NODE	(DFG)	=	0.24846007E 02
APG OF PERIAPSE	(DEG)	=	0.14930505E 02
ORBIT INCLINATION	(DFG)	=	0.81473733E 02
DEL NODE PER REV	(RAD)	=	-0.10861821E-02
DEL APSF PER REV	(RAD)	=	-0.32604282E-02

As is also apparent in the sample problem, the limit of the convergence process is not identical to the Goddard data. This fact is not alarming under the circumstances, due to the gross nature of the assumptions regarding the statistics of the problem, the poor quality of some of the data, and the small number of points processed. (The entire pass was reduced to approximately 45 points.) It is fully expected that a more complete sample problem involving more precisely reduced raw data will converge to the desired solution.

TIVE LIGHT

	-0.53629226E 04	3928345E
0.71565740E 00		0.29062537E 01
0.5595C000F C4	0.49523943E 04	0.44573218E 01
0ATE(1450) =	RADIUS VEC. =	VELOCITY VEC=

INITIAL COVARIANCE MATRIX

0.45ee7u44E 00	0.31658305F 01	0 17489095	0 1/051206		
	J へつ へ こ へ の 4 へ 4 つ			プローロ アクサ のいひ ア・コー	0・4の000104110
0.3165F304F 01	0.32695791E 02			-0.77136100E-01	43270175F-0
0.174~50958 02	0.17336038E 03		-0.74853903E	ı	23150944F
-0.14(>1295F-01	-0.14017667E 0C	-0.74853902E 00	0.60501508E	33347677F-	19713711F-
-0.785345235-02	-0.77136103E-01		0.33342621E	- 1	0.10318048F
0.4302415602	0.43270178E-01	.23150944E	-0.18713211E	- 1	. I ⊢ա
SATELLITE					
	0.1000000ce 01				•

THE ECLIPMENS STATIONS WILL BE CONSIDERED

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	0.398	- - -	,14	0.715	• 00		9	•	9 6		00	00.	.00	• 00	.00	• 00	• 00	• 00	• 00	00.	00.	00.	00.	00.		0,000	00.	• 30	.40	.00	.00	.00	.00	• 00		
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i ;	-0.2050C0C0E-05		.10C00000E 0	0.50928345E 01	.10000000E 0		1 330,00000	2/3/00/00/00		- COOOCOCE-3	.0000000E-3	.00000000E-3	.00000000F-3	.00000000E-3	.1000000E-1	.00000000E-3	.000000000-3	.000000000.	.0000n000E-3	· 0000000000·	.000000E-3	.0000000E-3	.000000000.	*0000000E-3	.0000C000E-3	0.0000000000000000000000000000000000000	.0000000E-3	. 000000000-3	.10000000E-0	.00000000E-3	.000000000-3	.0000000E-3	*-3000000000.	-9000000000.		
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	0.53781630E 04 0.77921165E-04	.00000001E-3	0.100000000E 01	•53629226E 0	*10000000E 0	.00000000E-3	753032255	6 3733.777.*	K-400000000	•0000000E-3	.000000000.	.000000ce=3	.000000c0E-3	.0rcnocooe-3	. COCOOOOE-3	.0000000E-3	• CC000000E-3	*0000000E-3	. COCCOCCE-3	• 00000000F-3	.0000000E-3	• 00 00 00 0 e - 3	6-3000000000000000000000000000000000000	- 1 0000000E-3	- CC00000000-3	0.0000000E-38	€-500000000°	·0000000000	.00000000F-3	• OCCOCCOE-3	.000000000.	· 000000000·	*C000000000.	£-3000000000		
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S	1	0.00000000E-3	.000000000.	.000000000.	.000000000E-3	.0000C000E-3	.0000000E-3
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1	3	0.000000000	.000000000.	.00000000E-3	.000000000.	.00000000E-3	.0000000E-3
!~	4	C. CC000000E-3	. 000000000E-3	.000000000.	.0000000E-3	.0C000000C-3	.0000000E-3
$\boldsymbol{\omega}$	4	0.00000000E-3	.000000000.	.000000000.	.000000000.		
	-						
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$\boldsymbol{\sigma}$	7	0.00000000E-3	.000C0C0C-3	.00000000E-3	.000000000.	.C0000000E-3	.00000000E-3
ഗ	73	0.0000000E-3	.00000000E-3	.00000000E-3	. 00000000E-3	.000000730.	.00000000E-3
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S	29	0.0000000E-3	* C0000000E-3	.00000000-3	.45852944E 0	.31658304E 0	.17489095E 0
S	73	-0.14051295E-0	0.78504923E-0	.43026156E-0	•31658305E 0	.32695791E 0	.17336038E 0
4)	52	-0.14017667E 0	0.77136103E-0	.43270178E-0	.17489094E 0	.17336036E 0	.92633961E 0
\sim	ር የ	±0.74853902E 0	.41270283E C	.23150944E 0	•14051295E-0	•14017666E 0	.74853903E 0
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382	25	0.33342622E-03	0.184009495-03	-0.10318049E-03	•43026154E-0	•43270175E-0	.73150944E 0
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SEC (U.T.)	SEC (U.T.)	SEC (U.T.)	SEC (U.T.)	SEC (U.T.)	SEC (U.T.)
0.55204885E 05 -0.52419600E 04 0.52145808E 01 -0.52345809E 04 0.52209366E 01	0.55229771E 05 -0.51106241E 04 0.53399309E 01 -0.51030891E 04 0.53461065E 01	0.55254657E 05 -0.49762064E 04 0.54622651E 01 -0.49685200E 04 0.54682565E 01	0.55279542E 05 -0.48387824E 04 0.55814966E 01 -0.48309492E 04 0.55872999E 01	0.55304429E 05 -0.46984309E 04 0.56975399E 01 -0.46904557E 04 0.57031512E 01	0.55329314E 05 -0.45552320E 04 0.58103111E 01 -0.45471195E 04 0.58157269E 01
DAYS 0.14618619E 04 0.28569716E 01 0.14788571E 04 0.28714437E 01	DAYS 0.15325139E 04 0.28207926E 01 0.15498641E 04 0.28348498E 01	DAYS 0.16022436E 04 0.27828552E 01 0.16199384E 04 0.27964883E 01	DAYS 0.16710075E 04 0.27431776E 01 0.16890362E 04 0.27563777E 01	DAYS 0.17387626E 04 0.27017791E 01 0.17571143E 04 0.27145376E 01	0.18054662E 04 0.26586806E 01 0.18241298E 04 0.26709890E 01
0.55950000E 04 0.50591229E 04 0.43537152E 01 0.50618230E 04 0.43365432E 01	0.55950000E 04 0.51659381E 04 0.42301896E 01 0.51682101E 04 0.42129571E 01	0.55950000E 04 0.52696448E 04 0.41039126E 01 0.52714873E 04 0.40866299E 01	0.55950000E 04 0.53701755E 04 0.39749546E 01 0.53715873E 04 0.39576321E 01	0.55950000E 04 0.54674644E 04 0.38433883E 01 0.54684448E 04 0.38260364E 01	0.55950000E 04 0.55614473E 04 0.37092887E 01 0.55619955E C4 0.36919178E 01
# TIME FROM JD 2433282.5 = R VECTOR (1950) = Y VECTOR (1950) = R VECTOR (DATE) = Y VECTOR (DATE) = E	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) = E	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = V VECTOR (DATE) = V VECTOR (DATE)	TIME FROM JD 24332R2.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (CATE) = V VECTOR (DATE) =	TIME FRCM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)

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0.5595000 0.5652062 0.3572733 0.5652178 0.3555353	0.5595000 0.5739249 0.3433800 0.5738932 0.3416423	0.5595000 0.5822950 0.3292573 0.5822201	0.5595000 0.5903108 0.3149135 0.5901928 0.3131794	0.5595000 0.5979671 0.3003572 0.5978059	0.5595000 0.6052585 0.2855971 0.6050543	0.559500
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0.22394954E 04 0.23114056E 01 0.22600153E 04 0.23203506E 01	DAYS 0.22963257F 04 0.22556103E 01 0.23170620E 04 0.22640478E 01	DAYS 0.23517494E 04 0.21983604E 01 0.23726892E 04 0.22062846E 01	DAYS 0.24057306E 04 0.21396894E 01 0.24268611E 04 0.21470948E 01	DAYS 0.24582343E 04 0.20796323E 01 0.24795427E 04 0.20865138E 01	DAYS 0.25092266E 04 0.25306997E 04 0.20245779E 01	DAYS 0.25586744E 04
0.61218021F 04 0.27064234E 01 0.61193311E 04 0.26892158E 01	0.55950000E 04 0.61872740E 04 0.25550197E 01 0.61843755E 04 0.25378779E 01	0.55950000E 04 0.62489559E 04 0.24018543E 01 0.62456317F 04 0.23847889E 01	0.55950000E 04 0.63068051E 04 0.22470223E 01 0.63030573E 04 0.22300439E 01	0.55950000E 04 0.63607814E 04 0.20906211E 01 0.63565123E 04 0.20737402E 01	0.55950000E 04 0.64108470E 04 0.19327496E 01 0.64062592E 04 0.19159767E 01	0.55950000E 04 0.64569668E 04
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-0.14044447E 04 0.72360658E 01	0.55827034E 05 -0.12336779E 04 0.72679647E 01 -0.12239506E 04 0.72688870E 01	0.55851920E 05 -0.10524427E 04 0.72965332E 01 -0.10426955E 04 0.72972127E 01	0.55876806E 05 -0.87055280E 03 0.73205808E 01 -0.86079163E 03 0.73210168E 01	0.55901691E 05 -0.68812098E 03 0.73400851E 01 -0.67835200E 03 0.73402773E 01	0.55926578E 05 -0.50526051E 03 0.73550269E 01 -0.49548978E 03 0.73549749E 01	0.55951463E 05 -0.32208517E 03 0.73653905E 01 -0.31231878E 03
0.28434414E 04 0.15563899E 01	DAYS 0.28589815E 04 0.14830732E 01 0.28812882E 04 0.14850619E 01	DAYS 0.28943984E 04 0.14113247E 01 0.29173477E 04 0.14127566E 01	DAYS 0.29292181E 04 0.13386469E 01 0.29515961E 04 0.13395207E 01	DAYS 0.29616181E 04 0.12650874E 01 0.29840109E 04 0.12654022E 01	DAYS 0.29921771E 04 0.11906944E 01 0.30145707E 04 0.11904496E 01	DAYS 0.30208748E 04 0.11155168E 01 0.30432553E 04
0.66417239E 04 0.77936238E 00	0.55950000E 04 0.6668834E 04 0.62918416E 00 0.66590684E 04 0.61364674E 00	0.55950000E 04 0.66804713E 04 0.46275826E 00 0.66722722E 04 0.44742044E 00	0.55950000E 04 0.66899124F 04 0.29592245E 00 0.66813340E 04 0.28079392E 00	0.55950000E 04 0.66951974E 04 0.12878812E 00 0.66862454E 04 0.11387843E 00	0.55950000E 04 0.66963208E 04 -0.38532974E-01 0.66870005E 04 -0.53214395E-01	0.55950000E 04 C.66932790E 04 -0.20592881E 00 0.66835963E 04
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0,73650942E 01	0.55976350E 05 -0.13870889E 03 0.73711637E 01 -0.12895291E 03 0.73706232E 01	0.56001235E 05 0.44753768E 02 0.73723379E 01 0.54493260E 02 0.73715534E 01	0.56026122E 05 0.22818842E 03 0.73689080E 01 0.23790536E 03 0.73678799E 01	0.56051007E 05 0.41148028E 03 0.73608726E 01 0.42116861E 03 0.73596014E 01	0.56075894E 05 0.59451501E 03 0.73482336E 01 0.60416869E 03 0.73467202E 01	0.56100779E 05 0.77717802E 03 0.73309969E 01 0.78679103E 03 0.732°2419E 01
0.11147122E 01	DAYS 0.30476924E 04 0.10396042E 01 0.30700460E 04 0.10382400E 01	DAYS 0.30726122E 04 0.96300703E 00 0.30949248E 04 0.96108390E 00	DAYS 0.30956178E 04 0.88577627E 00 0.31178757E 04 0.88329510E 00	DAYS 0.31166942E 04 0.80796351F 00 0.31388834E 04 0.80492564F 00	DAYS 0.31358273E 04 0.72962068E 00 0.31579340E 04 0.72602780E 00	DAYS 0.31530048E 04 0.65080047E 00 0.31750152E 04 0.64665467E 00
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ME FROM JD 2433282.5 = VECTOR (1950) = VECTOR (1950) = VECTOR (DATE) = VECTOR (CATE) = VECTOR (CATE)	0.55950000E 04 0.65556782E 04 -0.13703271E 01 0.65436396E 04 -0.13828616E 01	DAYS 0.31682154E 04 0.57155591E 00 0.31901158E 04 0.56685966E 00	0.56125666E 05 0.95935477E 03 0.73091718E 01 0.96892111E 03 0.73071765E 01	SEC (U.T.)
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ME FROM JD 2433282.5 = VECTOR (1950) = VECTOR (1950) = VECTOR (DATE) = VECTOR (DATE) = VECTOR (DATE)	0.55950000E 04 0.63867949E 04 -0.20200276E 01 0.63735706E 04 -0.20312934E 01	DAYS 0.32092107E 04 0.25140537E 00 0.32305351E 04 0.24453928E 00	0.56225209E 05 0.16809268E 04 0.71762971E 01 0.16902471E 04	SEC (U.T.)
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	00
	0.72543477E
0.20358529E 04 0.70828327E 01 0.20450151F 04 0.70794256E 01	-0.22986172E 04 0.70828327E 01 0.15396125E 03
0.32177131E 04 0.90183808E-01 0.32386693E 04 0.82257124E-01	0.20687971E 04 -0.23853086E 00 -0.58288431E 01
0.62783251E 04 -0.23377284E 01 0.62645569E 04 -0.23483167E 01	0.17567471E 04 -0.22524199E 01 0.35566449E 04
0 0 0 0	11 11 11
VECTOR (1950) VECTOR (1950) VECTOR (DATE) VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R, ROOT, AZ, ELEV

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UNDRFLOW AT 33550 IN MQ

EPOCH (REL. TO 1550.0)	i, II	0.55950000E 04	0.72833081E 00	(DAYS, DAYS)
EPCCH (REL. JD 2433282.5)		0.56274981E 05	0.55950000E 04	(DAYS U.T.)
POSITICN VECTOR (DATE)	9 11 11 11	0.61279427E 04	0.31832442E 04	0.21339417E 04
VELOCITY VECTOR (DATE)		-0.25601562E 01	-0.26524332E-01	0.70425999E 01
DELTA RACIUS		-0.13661419E 03	-0.55425065E 02	0.88926515E 02
DELTA VELOCITY		-0.21183954E 00	-0.10878146E 00	-0.36825711E-01
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0.57473525E-01	0.23348182E-01	1297	0.89253357E-04	455	71
0.16980946E 00	0.68687804E-01	0	0.26316513E-03	01	8
0.33055931E 00	0.13400103E 00	-0.21513200E 00	0.512589236-03	0.26316513E-03	33
03	02	02	00	00	-01
3872655E	6293343E	90331177E	21513200E	11043149E	37412994E
-0.1	-0.5	0	0	0	0
0.1	•	•	ô	01 -0.	01 -0
2 -0.1	2 -0.	2 0.	-0-	0	9
.86258942E 02 -0.1	2 0.35277802E 02 -0.	0.56293350E 02 0.	.13400103E 00 -0.	•68687797E-01 -0.	•23348186E-01 -0

THERE WAS NO RECTIFICATION AT THIS TIME

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5 SEC (U.T.) 1 4	4 1 3 0.12704640E 01	5 SEC (U.T.) 4 4	4 1 3 0.18231791E 01
0.56284978E 09 0.21065527E 0 0.70619178E 0 0.21156804E 0	-0.22279520E 0.0.70619178E 0.0.15346003E 0.0.15546003E 0.0.155460003E 0.0.155460003E 0.0.1554600000000000000000000000000000000000	0.56294974E 09 0.21770396E 09 0.70402915E 09 0.21861319E 09	-0.21575005E 04 0.70402915E 01 0.15294119E 03
DAYS 0.32184527E 04 0.57766852E-01 0.32393286E 04 0.49629479E-01	0.20661719E 04 -0.27088556E 00 -0.58047956E 01	DAYS 0.32188681E 04 0.25346192E-01 0.32396616E 04 0.16998963E-01	0.20632215E 04 -0.30324380E 00 -0.57788375E 01
0.55950000E 04 0.62546403E 04 -0.24008514E 01 0.62407670E 04 -0.24113004E 01	0.17338110E 04 -0.23153034E 01 0.34984192E 04	0.55950000E 04 0.62303258E 04 -0.24637286E 01 0.62163487E 04 -0.24740373E 01	0.17102487E 04 -0.23779413E 01 0.34404421E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JO 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLCYD GBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

1433282.5		. 62546403E 0 . 62546403E 0 . 24608514E 0 . 62407670E 0 . 24113004E 0 . 17338110E 0	44848 48	DAYS 0.32184527E 04 0.57766852E-01 0.32393286E 04 0.49629479E-01	0.56284978E 05 0.21065527E 04 0.70619178E 01 0.21156804E 04 0.70584186E 01	SEC (U.T.)
DOT, AZ, ELEV	11	4984192E 0		047956E	5346003E 0	0.12704640E 01
ROM JD 2433282.5 : 0R (1950) : 0R (1950) : 0R (0ATE)	0 11 11 11	0.55950000E 0.62303258E 0.24637286E 0.62163487E 00.24740373E 0.	14H44	DAYS 0.32188681E 04 0.25346192E-01 0.32396616E 04 0.16998963E-01	0.56294974E 05 0.21770396E 04 0.70402915E 01 0.21861319E 04 0.70367005E 01	SEC (U.T.)
FLCYD GBSERVES RELATIVE POSITION : RELATIVE VELOCITY : R, RODI, AZ, ELEV :	11 It y	0.17102487E 0. -0.23779413E 0. 0.34404421E 0.	4 14 4 	0.20632215E 04 -0.30324380E 00 -0.57788975E 01	-0.21575005E 04 0.70402915E 01 0.15294119E 03	0.18231791E 01

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SEC (U.T.)	0.238469645 01	SEC (U.T.)	0.29544208E 01
0.56304985E 05 0.22474107E 04 0.70179226E 01 0.22564666E 04 0.70142401E 01	-0.20871658E 04 0.70179226E 01 0.15240308E 03	0.56314997E 05 0.23175542E 04 0.69948452E 01 0.23265728E 04 0.69910715E 01	-0.20170596E 04 0.69948452E 01 0.15184521E 03
DAYS 0.32189593E 04 -0.71231084E-02 0.32396682E 04 -0.15679650E-01	0.20599353E 04 -0.33565032E 00 -0.57510036E 01	DAYS 0.32187255E 04 -0.39588966E-01 0.32393477E 04 -0.48353938E-01	0.20563277E 04 -0.36805332E 00 -0.57210248E 01
0.55950000E 04 0.62053464E 04 -0.25264467E 01 0.61912668E 04 -0.25366138E 01	0.16860276E 04 -0.24404192E 01 0.33826445E 04	0.55950000E 04 0.61797406E 04 -0.25889044E 01 0.61655599E 04 -0.25989289E 01	0.16611828E C4 -0.25026371E 01 0.33251378E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTJR (1953) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLGYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOI, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

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			0.26159544E-01 0.10812853E-01 -0.15714646E-01 0.39445080E-04 0.20385964E-04 0.83130838E-05
DAYS, DAYS) DAYS U.T.)	.24173471E 04 .69446530E 01 .90774340E 02 .46418507E-01		0.66149730E-01 0.27055835E-01 -0.39661304E-01 0.99272188E-04 0.51460083E-04
.72879395E 00 (0.31770894E 04 0 0.16560688E 00 0 0.62258314E 02 0 0.11725294E 00 -0	# Q. #:	0.12791006E 00 0.52622620E-01 -0.76857375E-01 0.19227092E-03 0.99272181E-04 0.39445089E-04
0.55950000E 04 0	0.60145764E 04 0. -0.28258927E 01 -0. -0.15098346E 03 -0. -0.22696388E 00 -0.	HE ERRORS IN STATE *	E 02 -0.51125036E 02 E 02 -0.21086090E 02 E 02 0.30766915E 02 E-01 -0.76857400E-01 E-01 -0.3961298E-01 E-01 -0.15714664E-01
1950.0) = (2433282.5) =	IR (DATE) =	: MATRIX FOR THE	0.34854742 0.14639354 -0.21086097 0.52622634 0.27055832
EPOCH (REL. TO EPOCH (REL. JD	POSITICN VECTOR (VELOCITY VECTOR (DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.852300845 02 0.34854739E 02 -0.51125029E 02 0.12791008E 00 0.66145705E-01

THERE WAS NO RECTIFICATION AT THIS TIME

TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	0 0 0 0 0	0.55950000E 04 0.61535655E 04 -0.26509676E 01 0.61352854E 04	DAYS 0.32181682E 04 -0.71981271E-01 0.32387018E 04 -0.80953345E-01	0.56324987E 05 0.23873195E 04 0.69711114E 01 0.23963000E 04 0.69672471E 01	SEC (U.T.)
FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R, RDOT, AZ, ELEY	ини	0.16357715E 04 -0.25644611E 01 0.32680571E 04	0.20523999E 04 -0.40038268E 00 -0.56889117E 01	-0.19473324E 04 0.69711114E 01 0.15126789E 03	0.35314470E 01
TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	11 11 11 11 11	0.55950000E 04 0.61267715E 04 -0.27127592E 01 0.61123934E 04 -0.27224961E 01	DAYS 0.32172872E 04 -0.10436357E 00 0.32377301E 04 -0.11354183E 00	0.56334978E 05 0.24568442E 04 0.69466773E 01 0.24657856E 04 0.69427729E 01	SEC (U.T.)
FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R, RCOT, AZ, ELEV	H H H	0.16097451E 04 -0.26260134E 01 0.32113073E 04	0.20481473E 04 -0.43270186E 00 -0.56544712E 01	-0.18778468E 04 0.69466773E 01 0.15066878E 03	0.41171793E 01
UNDRFLOW AT 33550 IN MQ	Ø				

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			0.22515357E-01 0.93783413E-02 -0.12979564E-01 0.33447122E-04 0.17340685E-04
AYS,DAYS) AYS U.T.)	.25561499E 04 .68916765E 01 .90364326E 02 .51046385E-01		0.53054717E-01 0.21816103E-01 -0.30520273E-01 0.78367439E-04 0.40796138E-04
72902521E 00 (D 55950000E 04 (D	31726944E 04 0 23362684E 00 0 65035681E 02 0	* * •	0.10222960E 00 0.42350352E-01 -0.58977371E-01 0.15152428E-03 0.78367428E-04
55950000E 04 0. 56334978E 05 0.	59558820E 04 0. 29541987E 01 -0. 15651134E 03 -0. 23170260E 00 -0.	ERRORS IN STATE **	-0.39839622E 02 -0.16555414E 02 0.23032245E 02 -0.58977400E-01 -0.30520268E-01
1950.0) = 0. 2433282.5) = 0.	(DATE) = 0. (DATE) = -0.	MATRIX FOR THE ER	0.28459142E 02 0.12084222E 02 -0.16555421E 02 0.42350369E-01 0.21816101E-01 0.93783485E-02
EPOCH (REL. TO 1 EPOCH (REL. JO 2	POSITION VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE M	0.69199964E 02 0.28459137E 02 -0.39835614E 02 0.10222962E 00 0.53054652E-01 0.22515366E-01

THERE WAS NO RECTIFICATION AT THIS TIME

SEC (U.T.)	0.471188335 01	SEC (U.T.)	0.53158023E 01
0.56344969E 05 0.25261216E 04 0.69215456E 01 0.25350230E 04 0.69175014E 01	-0.18086094E 04 0.69215456E 01 0.15004668E 03	0.56354959E 05 0.25951442E 04 0.68957193E 01 0.26040047E 04 0.68915858E 01	-0.17396277E 04 0.68957193E 01 0.14940028E 03
DAYS 0.32160828E 04 -0.13673216E 00 0.32364330E 04 -0.14611566E 00	0.20435696E 04 -0.46500716E 00 -0.56175600E 01	0.32145552E 04 -0.16908324E 00 0.32348106E 04 -0.17867101E 00	0.20386675E 04 -0.49729477E 00 -0.55780255E 01
0.55950000E 04 0.6C993615E 04 -0.27742719E 01 0.6C848868E 04 -0.27838635E 01	0.15831064E 04 -0.26872869E 01 0.31549121E 04	0.55950000E 04 0.60713386E 04 -0.28354985E 01 0.60567689E 04 -0.28449440E 01	0.15558588E 04 -0.27482744E 01 0.30988976E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) = V VECTOR (DATE)	FLGYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

25648E 00 (DAYS,DAYS) 50000E 04 (DAYS U.T.)	69266E 04 0.26938536E 04 61882E 00 0.68356852E 01 83995E 02 0.89848964E 02 94781E 00 -0.55900542E-01	**	17362177F-01 0.45502786E-01 0.20640823E-0	16434189E-01 0.18810024E-01 0.86592562E-0	.8359526E-01 -0.25099399E-01 -0.11410224E-	•12735447E-03 0.66162875E-04 0.30205076E-0	*66162861E-04 0.34591323E-04 0.15710564E-0	0205082E-04 0.15710581E-04 0.73771830E-0
00 (DAYS, DAYS 04 (DAYS U.T.	569266E 04 0.26938536E 0 161882E 00 0.68356852E 0 383995E 02 0.89848964E 0 294781E 00 -0.55900542E-0	** d	17362177F-01 0.45502786E-	16434189E-01 0.18810024E-	8359526E-01 -0.25099399E-	•12735447E-03 0.66162875E-	*66162861E-04 0.34591323E-	30205082E-04 0.15710581E-
) = 0.55950000E 04 0.73) = 0.56354959E 05 0.55	= 0.58946159E 04 0.316 = -0.30813822E 01 -0.308 = -0.16215291E 03 -0.678 = -0.23643826E 00 -0.123	# #	E 02 -0.33171648E 02	E 02 -0.13883401E 02	E 02 0.18411,798E 02	C9E-01 -0.48359657E-0	22E-01 -0.25C99396E-0	-0.11410242
EPOCH (REL. 10 1950.0 EPOCH (REL. JD 2433282.5)	POSITICN VECTOR (DATE) VELOCITY VECTOR (DATE) DELTA RABIUS DELTA VELOCITY	THE COVARIANCE MATRIX FOR THE ERRORS IN STAT	25E 02	Ē 02	02 -0.1	1E-01 0.3	•45502761E-01 0.1881	0.86592

THERE WAS NO RECTIFICATION AT THIS TIME

SEC (U.T.)	0.59304416E 01	SEC (U.T.)	0.65548010F 01
0.56364971E 05 0.26640467E 04 0.63691460E 01 0.26728654E 04 0.68649234E 01	-0.16707670E 04 0.68691460E 01 0.14872675E 03	0.56374982E 05 0.27326799E 04 0.68418812E 01 0.27414559E 04 0.68375698E 01	-0.16021765E 04 0.68418812E 01 0.14802596E 03
DAYS 0.32127003E 04 -0.20148027E 00 0.32328587E 04 -0.21127174E 00	0.20334314E 04 -0.52962805E 00 -0.55356134E 01	DAYS 0.32105211E 04 -0.23385306E 00 0.32305805E 04 -0.24384722E 00	0.20278699E 04 -0.56193694E 00 -0.54902279E 01
0.55950000E 04 0.60426458E 04 -0.28965586E 01 0.60279822E 04 -0.29058565E 01	0.15279464E 04 -0.28090949E 01 0.30431769E 04	0.55950000E 04 0.60133430E 04 -0.29573191E 01 0.59985871E 04 -0.29664687E 01	0.14994276E 04 -0.28696160E 01 0.29878937E 04
IIME FRGM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (0ATE) = V VECTOR (0ATE) =	FLCYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2432282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =

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UNDRFLOW AT 33550 IN MQ

(DAYS, DAYS)	0.28307033E 04 0.67765544E 01 0.89247479E 02 -0.61015408E-01
00	4 0 0 0 0 0 0
0.72948822E 0.55950000E	0.31597509E -0.36973028E -0.70829586E -0.12588305E
0.55950000E 04 0.56374982E 05	0.58306170E 04 -0.32077139E 01 -0.16797006E 03 -0.24124520E 00
H 4	H H H H
EPOCH (REL. TO 1950.9) EPOCH (REL. JD 2433282.5)	POSITION VECTOR (DATE) VELOCITY VECTOR (DATE) DELTA RAGIUS DELTA VELOCITY

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0.19734481E-01 0.83347703E-02 -0.10452227E-01 0.28444745E-04 0.14844458E-04
0.40837367E-01 0.16971367E-01 -0.21583229E-01 0.58456808E-04 0.30695965E-04
0.78114581F-01 0.32789609E-01 -0.41456757E-01 0.11214938E-03 0.58456792E-04
-0.28875290E 02 -0.12168074E 02 0.15375571E 02 -0.41456791E-01 -0.21582226E-01
0.22690979E 02 0.98079886E 01 -0.12168082E 02 0.32789631E-01 0.16971366E-01
0.54546620E 02 0.2269C571E 02 -0.2887528CE 02 0.781146C8E-01 0.40837342E-01

THERE WAS NO RECTIFICATION AT THIS TIME

SEC (U.T.)	0.72206841E 01	SFC (U.T.)	0.78977276E 01
0.56385488E 05 0.28044048E 04 0.68125297E 01 0.28131351E 04 0.68081259E 01	-0.15304973E 04 0.69125297E 01 0.14725955E 03	0.56395993E 05 0.28758177E 04 0.67824242E 01 0.28845012E 04 0.67779283F 01	-0.14591312E 04 0.67824242E 01 0.14645945E 03
DAYS 0.32078860E 04 -0.26779422E 00 0.32278393E 04 -0.27799996E 00	0.20216830E 04 -0.59581083E 00 -0.54391990E 01	DAYS 0.32048946E 04 -0.30170064E 00 0.32247395E 04 -0.31211681E 00	0.20151384E 04 -0.62964979E 00 -0.53844560E 01
0.55950C00E 04 0.59819410E 04 -0.302C7498E 01 0.5967C897E 04 -0.30257428E 01	0.14688527E 04 -0.29327955E 01 0.29303843E 04	0.55950000E 04 0.59498743E C4 -0.30838359E 01 0.59349294E 04 -0.30926712E 03	0.14376176E 04 -0.29956304E 01 0.28734284E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) = V VECTOR (DATE)	FLOYC OBSFRVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLCYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV = UNDRFLOW AT 33550 IN MQ

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	(DAYS, DAYS)	0.29730510E 04 0.67112402E 01 0.88549795E 02 -0.66688007E-01	
	00	04 00 02 00	
	0.72973141E 0.55950000E	0.31506896E -0.44119819E -0.74049925E -0.12908138E	** •
	04	00 00 00	STATE
	0,55950000E 0,56395993E	0.57606115F -0.33391123E -0.17431795E -0.24644110E	
	D O	n n ii n	Ī
	EPUCH (REL. TO 1950.0) EPUCH (REL. JD 2433282.5)	POSITION VECTOR (DATE) VELOCITY VECTOR (DATE) DELTA RADIUS DELTA VELOCITY	THE CUVARIANCE MATRIX FOR THE ERRORS IN
)			

0.19574591E-01 0.83221939E-02 -0.99038760E-02 0.27766947E-04 0.14543491E-04
0.38028637E-01 0.15895074E-01 -0.19202370E-01 0.53556841E-04 0.28251766E-04
0.72452914E-01 0.30615881E-01 -0.36757641E-01 0.10237488E-03 0.53556822E-04
-0.26015666E 02 -0.11038484E 02 0.13251286E 02 -0.36757677E-01 -0.19202368E-01 -0.99038952E-02
0.21521875E 02 0.93713008E 01 -0.11038492E 02 0.30615905E-01 0.15895074E-01
0.21521865E 02 0.21521865E 02 -0.26015656E 02 0.72452944E-01 0.38028612E-01 0.19574601E-01

THERE WAS NO RECTIFICATION AT THIS TIME

05 SEC (U.T.) 04 01 04 01	04 01 03 0.85521011E 01	05 SEC (U.T.) 04 01 04 01	04 01 03 0.92168491E 01
0.56405984E 0.29434330E 0.67530980E 0.29520711E 0.67485150E	-0.13915612E 0.67530980E 0.14566545E	0.56415975E 0.30107516E 0.67230969E 0.30193435E 0.67184273E	-0.13242888E 0.67230969E 0.14483723E
DAYS 0.32017194E 04 -0.33390931E 00 0.32214592E 04 -0.34452448E 00	0.20085813E 04 -0.66179410E 00 -0.53287265E 01	DAYS 0.31982227E 04 -0.36607886E 00 0.32178556E 04 -0.37689193E 00	0.20017016E 04 -0.69389912E 00 -0.52691848E 01
0.55950000E 04 0.59187661E 04 -0.31435031E 01 0.59037336E 04 -0.31521876E 01	0.14073043E 04 -0.30550587E 01 0.28198133E 04	0.55950000E 04 0.58870638E 04 -0.32028443E 01 0.58719454E 04 -0.32113772E 01	0.13764011E 04 -0.31141610E 01 0.27667725F 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =	TIME FROM JO 2432282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV = UNDRFLOW AT 33550 IN MQ

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4.	(2

			0.19788938E-01 0.84639725E-02 -0.95774321E-02 0.27646667E-04	
(DAYS, DAYS) (DAYS U.T.)	.31075322E 04 .66457261E 01 .88188667E 02 .72701097E-01		0.36307040E-01 0.15258997E-01 -0.17539524E-CI 0.50350723E-04	1111111111111
0.72996268E 00 (DA'	.31402809E 04 0 .50969397E 00 0 .77574660E 02 0	* * * *	2 0.68904984E-01 2 0.29296382E-01 2 -0.33460686E-01 1 0.95899636E-04	0 140.010100
55950000E 04 56415975E 05	56905817E 04 34639775E 01 - 18136372E 03 - 25260032E 00 -	ERRORS IN STATE	-0.24045115E 02 -0.10266557E 02 0.11731097E 02 -0.33460723E-01	1 1 1 1 1 1 1 1 1
1950.0) = 0. 2433282.5) = 0.	DATE) = 0. DATE) = -0.	MATRIX FOR THE ER	0.20906243E 02 0.91596683E 01 -0.10266565E 02 0.29296408E-01 0.15258957E-01	
EPOCH (REL. TO EPOCH (REL. JD	POSITICN VECTOR (VELOCITY VECTOR (DELTA RABIUS DELTA VELOCITY	THE COVARIANCE	0.49648365E 02 0.20906231E 02 -0.24045103E 02 0.68905016E-01 0.36307014F-01	

0.50350723E-04 0.26677417E-04 0.14532470E-04

0.95899636E-04 0.50350701E-04 0.27646669E-04

> -0.17539523E-01 -0.95774517E-02

0.29296408E-01 0.15258997E-01 0.84639837E-02

0.19788949E-01

0.81712567E-0'

THERE WAS NO RECTIFICATION AT THIS TIME

SEC (U.T.)	0.98934599E 01	SEC (U.T.)	0.10580531E 02
0.56425986E 05 0.30779053E 04 0.66923602E 01 0.30864500E 04 0.66876042E 01	-0.12571824E 04 0.66923602E 01 0.14397101E 03	0.56435998E 05 0.31447478E 04 0.66609523E 01 0.31532445E 04 0.66561106E 01	-0.11903879E 04 0.66609523E 01 0.14306610E 03
DAYS 0.31943966E 04 -0.39827290E 00 0.32139202E 04 -0.40928316E 00	0.19944814E 04 -0.72602826E 00 -0.52054565E 01	DAYS 0.31902484E 04 -0.43042098E 00 0.32096608E 04 -0.44162729F 00	0.19869427E 04 -0.75811137E 00 -0.51373919E 01
0.55950000E 04 0.58547029E 04 -0.32619762E 01 0.58394998E 04 -0.32703563E 01	0.13448455E 04 -0.31730534E 01 0.27142352E 04	0.55950000E 04 0.58217518E 04 -0.33207686E 01 0.58064656E 04 -0.33289950E 01	0.13127021E 04 -0.32316066E 01 0.26623582E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (CATE) =	FLCYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLGYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV = UNDRFLOW AT 33550 IN MQ

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			0.20426592E-0 0.87874780E-0 -0.94468949E-0 0.28104119E-0 0.14828111E-0
(DAYS, DAYS) (DAYS U.T.)	0.32410600E 04 0.65769424E 01 0.87815529E 02 0.79168111E-01		1 0.35473424E-01 1 0.14993519E-01 1 -0.16378675E-01 4 0.48446284E-04 4 0.25781533E-04 4 0.14828123E-04
0.73019442E 00 (D	0.31283181E 04 0 -0.57841986E 00 0 -0.81342735E 02 0 -0.13679257E 00 -0	** d **	0.67055902E-0 0.28684077E-0 -0.31134475E-0 0.91924883E-0 0.48446260E-0
0.55950000E 04 0.56435998E 05 0	0.56175795E 04 0.35881787E 01 0.18888611E 03 0.25918372E 00	Ε	2 -0.22716513E 02 1 -0.97586089E 01 0.10604215E 02 1 -0.31134513E-01 1 -0.16378674E-01 2 -0.94469149E-02
1950.0) = 2423282.5) =	(DATE) =	THE COVARIANCE MATRIX FOR THE ERRORS IN STA	0.20782686E 02 0.91548818E 01 -0.975E6169E 01 0.28684105E-01 0.14993520E-01
EPOCH (REL. TO EPOCH (REL. JO	POSITICN VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.49054578F 02 0.20782673E 02 -0.22716500E 02 0.67055537E-01 0.35473397E-01

THERE WAS NO RECTIFICATION AT THIS TIME

YS 31857881E 04 0.32111360E 04 46245395E 00 0.66289440E 01 32050876E 04 0.32195839E 04 47385474E 00 0.66240171E 01	19790954F 04 -0.11240485E 04 79007929E 00 0.66289440F 01 50648799E 01 0.14212242E 03 0.11276614E 02	YS , 0.56455979E 05 SEC (U.T.) 31810082E 04 0.3277209E 04 49443427E 00 0.65962749E 01 32001927E 04 0.3285592F 04 50602836E 00 0.65912634E 01	19709273E 04 -0.1058032E 04 82199438E 00 0.65962749E 01 49874948E 01 0.14113570E 03 0.11982958E 02
0.55950000E 04 DAY 0.57882833E 04 0.3 -0.33790959E 01 -0.4 0.57729156E 04 0.3	0.12800443E 04 0.1 -0.32896951E 01 -0.7 0.26112864E 04 -0.5	0.55950000E 04 DAY C.57542341E 04 0.3 -0.34370727E 01 -0.4 G.57387866E 04 0.3 -0.34449901E 01 -0.5	0.12468C97E 04 0.1 -0.33474232E 01 -0.8 0.256C9613E 04 -0.4
TIME FROM JO 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (CATE) = V VECTOR (CATE) =	FLOYD OBSERVES RFLATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROW JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLCYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =

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			0.21447519E-01 0.92790010E-02 -0.94694239E-02 0.29060943E-04 0.15392447E-04
(DAYS, DAYS) (DAYS U.T.)	.33728329E 04 .65053384E 01 .87233810E 02		0.35333884E-01 0.15022572E-01 -0.15577873E-01 0.47527900E-04 0.25404049E-04
.73042569E 00 .55950000E 04	31150117E 04 0 64678333E 00 0 85181046E 0? 0	** d **	0.66521727E-01 0.28627820E-01 -0.29501311E-01 0.89828925E-04 0.47527873E-04
,55950000E 04 0	0.55423167E 04 0.3 -0.37106132E 01 -0.6 -0.19646980E 03 -0.8 -0.26562314E 00 -0.1	THE ERRORS IN STATE *	-0.21853730E 02 -0.9441690E 01 0.97509460E 01 -0.29501349E-01 -0.15577873E-01
1950.0) = C. 2433282.5) = O.	(DATE) = (DATE) = :	MATRIX FOR THE ER	0.21C61005E 02 0.93222414E 01 -0.94441772E 01 0.28627850E-01 0.15022574E-01 0.92790148E-02
EPOCH (REL. TO EPOCH (REL. JD	POSITICN VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.49402808E 02 C.2106C990E 02 -0.21853717F 02 0.66521763F-01 0.35323857E-01

THERE WAS NO RECTIFICATION AT THIS TIME

SEC (U.T.)	0.12699329E 02	SEC (U.T.)	0.13425324E 02
0.56465969E 05 0.33429365E 04 0.65629485E 01 0.33512842E 04 0.65578529E 01	-0.99234814E 03 0.65629485E 01 0.14010343E 03	0.56475960E 05 0.34083356E 04 0.65289693E 01 0.34166320E 04 0.65237901E 01	-0.92700034E 03 0.65289693E 01 0.13902282E 03
DAYS 0.31759088F 04 -0.52635898E 00 0.31949766E 04 -0.53814517E 00	0.19624383E 04 -0.85385368E 00 -0.49049349E 01	DAYS 0.31704910E 04 -0.55822408E 00 0.31894401E 04 -0.57020115E 00	0.19536344E 04 -0.88565331E 00 -0.48168780E 01
C.55950000E 04 0.57196070E 04 -0.34946938E 01 0.5704C912E 04 -0.35024555F 01	0.12130013F 04 -0.34048156F 01 0.25114321F 04	0.55950000E 04 0.56844064E 04 -0.35519519E 01 0.56688038E 04 -0.35595573E 01	0.11786219E 04 -0.34618355E 01 0.24627559E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLCYC OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, A7, ELEV =	TIME FROW JD 2435282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYC CBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R; ROOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

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			0.22820565E-01 0.99287765E-02 -0.96074095E-02 0.30452314E-04 0.16194629E-04
.S.DAYS) .S. U.T.)	35025183E 04 64313924E 01 85886231E 02 92397689E-01		0.35732130E-01 0.15285064E-01 -0.15024379E-01 0.47343215E-04 0.25417169E-04
	31009080E 04 0. 71397462E 00 0. 88532024E 02 0. 14377347E 00 -0.	**	0.66992119E-01 0.29005693E-01 -0.28341262E-01 0.89114470E-04 0.47343187E-04
55950000E 04 0. 56475960E 05 0.	4659796E 04 0.32975C5E 01 -0.3282417E 03 -0.7019?25E 00 -0.	ERRORS IN STATE **	-0.21314460E 02 -0.92659634E 01 0.90789179E 01 -0.28341301E-01 -0.15024379E-01 -0.96074303E-02
1950.0) = 0. 2433282.5) = 0.	(DATE) = 0.54 (DATE) = -0.38 = -0.2	MATRIX FOR THE ER	0.21668605E 02 0.96341556E 01 -0.92659714E 01 0.29005725E-01 0.15285066E-01 0.99287916E-02
EPOCH (REL. TO EPOCH (REL. JD	POSITICN VECTOR (VELOCITY VECTOR (DELTA RACIUS DELTA VELOCITY	THE COVARIANCE	0.50503440E 02 0.2165F588E 02 -0.21314445E 02 0.66992157E-01 0.35732103F-01

THERE WAS NO RECTIFICATION AT THIS TIME

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SEC (U.T.)	0.14162094E 02	SEC (U.T.)	0.14907388E 02
0.56485971E 05 0.34735259E 04 0.64942687E 01 0.34817700E 04 0.64890054E 01	-0.86186237E 03 0.64942687E 01 0.13788906E 03	0.56495983E 05 0.35383656E 04 0.64589205E 01 0.35465566E 04 0.64535755E 01	-0.79707578E 03 0.64589205E 01 0.13670107E 03
DAYS 0.31647428E 04 -0.59C79212E 00 0.31855710E 04 -0.60225921E 00	0.19444845E 04 -0.91745540E 00 -0.47228115E 01	DAYS 0.31586760E 04 -0.62189363E 00 0.31773814E 04 -0.63424949E 00	0.19350195F 04 -0.94919090E 00 -0.46225531E 01
0.55950000E 04 0.56485610E 04 -0.36089590E 01 0.56328831E 04 -0.36164069E 01	0.11436054E 04 -0.35186034E 01 0.24143830E 04	0.55950000E 04 0.56121469E 04 -0.35655900E 01 0.55963951E 04 -C.36728797E 01	0.11080228F 04 -0.35749955E 01 0.23679832E 04
TIME FROW JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, A2, ELEV =

UNDRFLOW AT 33550 IN MQ

0 t	.55950000E 04 .56495983E 05	0.55950000E 04 0.56495983E 05
S		• 5 5 5 5 5 5 5
447F 01	44447F 01	0.3944467F 01
) - -	10 J-000t-100-0	10 J-00011000
347E 03	47E 03	0.20704347E 03
000	00 100101100	00 100101 00
703E 00	-0°2/1/8/03E 00 -0	0°7'1'8'07E 00

THE COVARIANCE MATRIX FOR THE ERRORS IN STATE ** P **

0.24456204E-01 0.10701606E-01 -0.98025844E-02 0.32140299E-04 0.17164587E-04
0.36451304E-01 0.15692144E-01 -0.14594989E-01 0.47574818E-04 0.25656687E-04
0.68046989E-01 0.29645170E-01 -0.27417826E-01 0.89168670E-04 0.47574790E-04
-0.20934083E 02 -0.91555604E 01 0.84994175E 01 -0.27417866E-01 -0.14594991E-01
0.22489069E 02 0.10043392E 02 -0.91555680E 01 0.29645203E-01 0.15692146E-01
0.52071372E 02 0.22489050E 02 -0.20934067E 02 0.68047026E-01 0.36451277E-01

THERE WAS NO RECTIFICATION AT TH'S TIME

0 2	11	0.55950000E 04	4	YS	0.56505973E 05	SEC (U.T.)
1950	11	.55752445E	4	.31523047E	.36027157E 0	
1950	11	.37217233F	 1	•65355989E	.64230031E 0	
ATE	11	.55594208E	4	3	.36108530E 0	
ΒA	31	.37288544E	_	6610283E	•64175761E 0	
BSERVE						
IVE POSITIO	I	.10719550E 0		.19252536E	.73277942E 0	
VE VELOCIT	1)	.36308904E 0	_	-0.98079105E 00	0.64230031E 01	
OT, AZ,	11	E 0		45159876E	.13545869E 0	0.15658882E 02
2	II	.55950000E 0			•56515964E 0	SEC (U.T.)
(1950)	Ħ	.55377831E 0		.31456172E 0	.36667040E 0	
(1950)	H	37774709E 0	إحج	-0.68515338E 00	. 0.63864489E 01	
DATE	Н	.55218889E 0		.31640721E 0	.36747866E 0	
DATE	н	.37844428E 0		.69788211F 0	•63809406E 0	
OBSERVES IVE POSITIO	П	.10353318E 0	4	.19151704E 0	6884579E 0	
VE VEL	H	36863995E 0		-0.10123183E 01	0.63864489E 01	
OT, AZ, ELE	11	.22775303E 0	4	.44025574E 0	.13415634E 0	0.16417032E 02
AT 33550 IN MQ	~					

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(DAYS, DAYS) (DAYS U.T.)	0.37537574E 04 0.62794219E 01 0.78970818E 02 -0.10151868E C0
0.73111996F 00 0.55950000E 04	0.30727964E 04 -0.84105811E 00 -0.91275685E 02 -0.14317600E 00
0.55950000E 04 0.56515964E 05	0.53157545E 04 -0.40511351E 01 -0.20613446E 03 -0.26669234E 00
1950.0) = 2433282.5) =	DATE) = DATE) = =
® EPOCH (REL. TO 19 EPOCH (REL. JD 24	POSITICN VECTOR (VELOCITY VECTOR (DELTA RADIUS DELTA VELOCITY

THE COVARIANCE MATRIX FOR THE ERRORS IN STATE ** P **

0.26104194E-01 0.11490874E-01 -0.99452741E-02 0.33790500E-04 0.18125467E-04
0.37094244E-01 0.16073346E-01 -0.14119589E-01 0.47695421E-04 0.25842598E-04
0.68938001E-01 0.30224794F-01 -0.26411400E-01 0.88998826E-04 0.47695395E-04
-0.20470988E 02 -0.90087588E 01 0.79103405E 01 -0.26411438E-01 -0.14119591E-01
0.23280698E 02 0.10446481E 02 -0.90087661E 01 0.30224826E-01 0.16073348F-01
0.53543014E 02 0.23280679E 02 -0.2047C972E 02 0.68938036E-01 0.37094218F-01 0.26104205E-01

THERE WAS NO RECTIFICATION AT THIS TIME

SEC (U.T.)	0.17182111E 02	SEC (U.T.)	0.17951028E 02
0.56525976E 05 0.37304546E 04 0.63491848E 01 0.37384817E 04 0.63435956E 01	-0.60515070E 03 0.63491848E 01 0.13278796E 03	0.56535987E 05 0.37928289E 04 0.63112900E 01 0.38017996E 04 0.63056204E 01	-0.54183276E 03 0.63112900F 01 0.13135302E 03
DAYS 0.31335998E 04 -0.71673552E 00 0.31569262E 04 -0.72964909E 00	0.19047511E 04 -0.10438339E 01 -0.42816465E 01	DAYS 0.31312666E 04 -0.74823752E 00 0.31494629E 04 -0.76133459E 00	0.18940150E 04 -0.10752692E 01 -0.41531278E 01
0.559500C0E 04 0.54996875E 04 -0.38329403E 01 0.54837243E 04 -0.38397519E 01	C.958G7977E 03 -0.37416302E 01 0.22339309E 04	0.55950000E 04 0.54610389E 04 -0.38880100E 01 0.54450083E 04 -0.38946608E 01	0.96027856E 03 -0.37964613E 01 0.21915771E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RCOT, AZ, ELEV =	TIME FROM JO 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITICN = RELATIVE VELOCITY = R, RDOT, AZ, ELEV = UNDRFLOW AT 23550 IN MQ

55950000E 04 0.73135170E no (DAYS,DAYS) 56535987E 05 0.55950000E 04 (DAYS U.T.)	52488876E 04 0.30619112E 04 0.38730161E 04 41447970E 01 -0.89626732E 00 0.62052931E 01 19512067E 03 -0.87551635F 02 0.71216573E 02 25013625E 00 -0.13493274E 00 -0.10032775E CC	RORS IN STATE ** P **	-0.19577016E 02 0.68457765E-01 0.37010978E-01 0.27285503E-0: -0.86720572E 01 0.30213969E-01 0.16143176E-01 0.12087073E-0: 0.71863697E 01 -0.24882457E-01 0.87076572E-04 0.45851740E-04 0.34793643E-0: -0.13360977E-01 0.46881719E-04 0.25531579E-04 0.18749964E-0:
595000 653598	248887 144797 951206 501362	THE ERRORS IN	5E 02 -0.1957 5E 02 -0.8672 7E 01 0.7186 7E-01 -0.2488 7E-01 -0.1336
1950.0) : 2432282.5) :	(DATE)	MATRIX FOR	0.2362513 0.10659959 -C.8672063 0.3021399
FPOCH (REL. TO EPOCH (REL. JO	POSITICN VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.53965287E 02 0.23625118F 02 -0.19577000E 02 0.68457755E-01

THERE WAS NO RECTIFICATION AT THIS TIME

SEC (U.T.)	0.18720369E 02	SEC (U.T.)	0.19489499E 02
е 05 е 01 е 04	E 03 E 03	е 05 е 01 е 01	Е 03 Е 03
0.56545978 0.38566916 0.62728487 0.38646052 0.62670994	-0.47902716 0.62728487 0.12985155	0.56555968 0.39191671 0.62337879 0.39270229 0.62279596	-0.41660950 0.62337879 0.12827748
• 400 000 000	04 01 01	, 40000 40040	04 01 01
6345E 9149E 6990E 7032E	9836E 5563E 9450E	6895E 5913E 6205E 1834E	5383E 7570E 5086E
YS 3123 7795 3141 7928	1882 1106 4016	YS 31156 81085 31336 82431	18716 11377 38725
00000000000000000000000000000000000000	000	00000	000
04 01 01 01	03 01 04	04 04 01 04	03
0.55950000E 0.54219222E -0.39425623E 0.54058260E -0.39490513E	0.92201239E -0.38507753E 0.21506281E	0.55950000E 0.53822625E -0.39967054E 0.53661022E -0.40030332E	0.88320697E -0.39046801E 0.21110774E
11 11 11 11	11 11 11	11 11 11 11 11	j
TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R, RDOT, AZ, ELEV	TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	FLCYD OBSERVES RELATIVE POSITION RELATIVE VELOCKTY R, ROOT, AZ, ELEV

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UNDRFLOW AT 33550 IN MQ

			0.27277407E-0 0.12166162E-0 -0.93187962E-0 0.34275307E-0. 0.18560316E-0.
1YS, DAYS) 1YS U.T.}	.39863504E 04 .61360451E 01 .59327497E 02 .91914522E-01		0.35364902E-01 0.15524390E-01 -0.12073358E-01 0.44131017E-04 0.24173563E-04
•73158297E 00 (DA) •55950000E 04 (DA)	.30556772E 04 0.3 .94227163E 00 0.6 .77943280E 02 0.5 .11795229E 00 -0.9	** d.	0.65079889E-01 0.28923870E-01 -0.2238493E-01 0.81574717E-04 0.44131005E-04
*55950000E 04 0	0.51931786E 04 0.0.42205738E 01 -0.0.17292360E 03 -0.0.21754062E 00 -0.0.	ERRORS IN STATE **	-0.17875780E 02 -0.79745257E 01 0.62225703E 01 -0.22385023E-01 -0.12073361E-01 -0.93188144E-02
1950.0) = 0 2433282.5) = 0	(DATE) = - (DATE) = -	THE	0.22949787E 02 0.10426138E 02 -0.79745315E 01 0.28923890E-01 0.15524390E-01
% EPOCH (REL. TO EPOCH (REL. JO	POSITICN VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE MATRIX FOR	0.52066952E 02 0.22949772E 02 -0.17875765E 02 0.65079913E-01 0.35364880E-01

THERE WAS NO RECTIFICATION AT THIS TIME

SEC (U.T.)	0.20257490F 02	SEC (U.T.)	0.21019698E 02
0.56565979E 05 0.39813768E 04 0.61940300E 01 0.39891739E 04 0.61881232E 01	-0.35445853E 03 0.61940300E 01 0.12662441E 03	0.56575991E 05 0.40431855E 04 0.61536592E 01 0.40509230E 04).61476744E 01	-0.29270938E 03 0.61536592E 01 0.12489245E 03
DAYS 0.31074153E 04 -0.84210125E 00 0.31252107E 04 -0.85573982E 00	0.18599529E 04 -0.11689318E 01 -0.37191916E 01	DAYS 0.30988288E 04 -0.87324995E 00 0.31164867E 04 -0.88706645E 00	0.18479588E 04 -0.12000131E 01 -0.35569986E 01
0.55950000E 04 0.53419804E 04 -0.40505440E 01 0.53257576E 04 -0.40567091E 01	0.84378571E 03 -0.39582799E 01 0.20729302E 04	0.55950000E 04 0.53011615E 04 -0.41039604E 01 0.52848778E 04 -0.41099622E 01	0.80383026E 03 -0.40114579E 01 0.20363629E 04
TIME FROM JO 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROGT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

(DAYS, DAYS)	0.40949998E 04 0.60720487E 01 0.44076783E 02 -0.75625651E-01
0.73181471E 00 0.55950000E 04	0.30541107E 04 -0.97963039F 00 -0.62376046E 02 -0.92563925E-01
0.55950000E 04 C.56575991E 05	0.51482107E 04 -0.42797135E 01 -0.13666706E 03 -0.16975137E 00
ЕРОСН (REL. TO 1950.0) = ЕРОСН (REL. JO 2433282.5) =	POSITION VECTOR (DATE) = VELOCITY VECTOR (DATE) = DELTA RADIUS = DELTA VELOCITY =

THE COVARIANCE MATRIX FOR THE ERRORS IN STATE ** P **

0.255007535-0. 0.114589355-0. -0.820482145-0. 0.315854795-0. 0.171916265-0.
0.31634774E-01 0.13969675E-01 -0.10171735E-01 0.38882907E-04 0.21448585E-04
0.57887391F-01 0.25917916E-01 -0.18777558E-01 0.71515002E-04 0.38882907E-04
-0.15218746E 02 -0.68419878E 01 0.50140782E 01 -0.18777580E-01 -0.10171738E-01
0.20856617E 02 0.95580225E 01 -0.68419928E 01 0.25917924E-01 0.13969673E-01
0.47604577E 02 0.20856508E 02 -0.15218725E 02 0.57887404E-01 0.31634757E-01

THERE WAS NO RECTIFICATION AT THIS TIME

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5 SEC (U.1.) 4 4	3 1 3 0.21771341E 02	5 SEC (U.T.) 4 4	3 0.22510196F 02
0.56585981E 0 0.41044609E 0 0.61127656E 0 0.41121383E 0	-0.23149408E 0 0.61127656E 0 0.12308309E 0	0.56595972E 0.0.41653250E 0 0.60712712E 0.41729413E 0.0.60651327E 0	-0.17069104E 0 0.60712712E 0 0.12119064E 0
DAYS 0.30899496E 04 -0.90423810E 00 0.31074686E 04 -0.91823074E 00	0.18356759E 04 -0.12309337E 01 -0.33860717E 01	DAYS 0.30807613E 04 -0.93512681E 00 0.30981396E 04 -0.94929413E 00	0.18230827E 04 -0.12617548E 01 -0.32059110E 01
0.55950000E 04 0.52598957E 04 -0.41568404E 01 0.52435529E 04 -0.41626787E 01	0.76343097E 03 -0.40640998E 01 0.20015300E 04	0.55950000E 04 0.52181035E 04 -0.42092896E 01 0.52017032E 04 -0.42149638E 01	0.72250916E 03 -C.41163109E 01 0.19684474E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD GBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

(DAYS, DAYS)	0.42013411E 04 0.60104529E 01 0.28399769E 02 -0.54679736E-01	
0.73204598E 00 0.55950000E 04	0.30542355E 04 -0.10130141E 01 -0.43904063E 02 -0.63719989E-01	** d **
0.55950000E 04 0.56595972E 05	0.51072400E 04 -0.43310577E 01 -0.94463189E 02 -0.11609398E 00	1E ERRORS IN STATE
<pre>P EPOCH (REL. TO 1950.0) = EPOCH (REL. JD 2433282.5) =</pre>	POSITION VECTOR (DATE) = VELOCITY VECTOR (DATE) = DELTA RADIUS = DELTA VELOCITY =	THE COVARIANCE MATRIX FOR THE ERRORS IN

0.39310274E 0.17551605E -0.11951981E 0.47697695E-0.26233391E-

0.22C71700E-01 0.99994075E-02 -0.66537805E-02 0.26951801E-04 0.12671512E-04
0.26233403E-01 0.11642594E-01 -0.79031227E-02 0.31751194E-04 0.17669641E-04
0.47697693E-01 0.21523152E-01 -0.14531161E-01 0.58095639E-04 0.31751207E-04
-0.11951990E 02 -0.54196041E 01 0.37221015E 01 -0.14531175E-01 -0.79031255E-02 -0.66537931E-02
0.175516C9E 02 0.81333916E 01 -0.54196083E 01 0.21523148E-01 0.11642591E-01 0.99994123E-02
4E 02 5E 02 1E 02 5E-01 1E-01

THERE WAS NO RECTIFICATION AT THIS TIME

TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	и и и и и	0.55950000E 04 0.51757020E 04 -0.42614084E 01 0.51592457E 04 -0.42669177E 01	DAYS 0.30712449E 04 -0.96597592E 00 0.30884805E 04 -0.98031680E 00	. 405983E 05 0.42258956E 04 0.60290934E 01 0.42334501E 04 0.60228788E 01	SEC (U.T.)
FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R, RDOT, AZ, ELEV	11 11 11	0.68C98322E 03 -0.41681914E 01 0.19371478E C4	0.18101556E 04 -0.12925360E 01 -0.30160108E 01	-0.11018225E 03 0.60290934E 01 0.11920928E 03	0.23233528E 02
TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (CATE)	11 11 11 11 11	0.55950000F 04 0.51327805E 04 -0.43130836E C1 0.51162700E 04 -0.43184276E 01	DAYS 0.30614203E 04 -0.99671865E 00 0.30785114E 04 -0.10112316E 01	0.56615995E 05 0.42860410E 04 0.59863222E 01 0.42935330E 04 0.59800321E 01	SEC (U.T.)
FLOYD OBSERVES RFLATIVE POSITION RELATIVE VELOCITY R, ROOT, AZ, ELEV	li li li	0.63894153E 03 -0.42196285E 01 0.19077931E 04	0.17969191E 04 -0.13232106E 01 -0.28167148E 01	-0.50099365E 02 0.59863222E 01 0.11714191E 03	0.23935227E 02

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			0.17876385E-01 0.81712750E-02 -0.50127829E-02 0.21548346E-04 0.11861419E-04				
AYS, DAYS } AYS U.T.)	0.43087778E 04 0.59460384E 01 0.15244760E 02 0.33993757E-01		1 0.20382203E-01 0.90778975E-02 1 -0.57114771E-02 4 0.242799C9E-04 4 0.13667163E-04 4 0.13861424E-04).43087778E 04).59460384E 01		
0.73227772F 00 (0.0)	0.30519287E 04 (-0.10487277F 01 (-0.26582695E 02 (-0.37495593E-01 -0.	** C **	01 0.36785079E-01 01 0.16736404E-01 01 -0.10465969E-01 01 0.4418544E-04 02 0.24279931E-04 02 0.21548340E-04		0.30519287E 04 0 -0.10487277E 01 0		
0.55950000E 04 0.56615995E 05	0.5060R483E 04 -0.43861717E 01 -0.55421723E 02 -0.67744167E-01	IE FRRORS IN STATE	02 -0.87369738E 01 -0.39998329E 01 0.25702932E -01 -0.10465976E- -02 -0.57114793E-	16160	0.50608483E 04 -0.43861717E 01		0.74776414E 04 0.22280758E-01 0.10735342E 02 0.24827538E 02 0.25826448E 02 0.81488110F 02 -0.10995342E-02
50.0) =	DATE) = OATE) = = = = = = = = = = = = = = = = = =	TRIX FOR TH	0.13817250E C.64934383E 0.39958367E 0.16736389E 0.90778922E C.31712757E	S BEEN RECT	2 () DATE) = 2 () DATE) = 2	EMENTS	(KM) (DEG) = (DEG) = (DEG) = (DEG) = (RAD) = (
Б ЕРОСН (REL. TO 1918) ЕРОСН (REL. JO 243)	POSITICN VECTOR (VELOCITY VECTOR (DELTA RACIUS)	THE COVARIANCE MA	0.17876367E 02 0.13817251E 02 -0.87369676F 01 0.36785074F-01 0.26382196E-01 0.1787638GE-01	THF TRAJECTORY HAS	POSITICN VECTOR (R VELOCITY VECTOR (V	ELLIPTIC ORBIT ELE	SEMIMAJOR AXIS ECCENTRICITY TRUE ANJWOLY DATE R ASC OF ASC NUDE ARG OF PERIAPSF ORBIT INCLINATION DEL NODE PER REV

	90819E 02	(U.T.)	.95814E 02
	0.24090	SEC (0.246
0.59071504E 04 0.59071504E 04 0.43707662E 04 0.59006833E 01	0.27133789E 02 0.59071504E 01 0.11343114E 03	0.56635976E 05 0.44222139E 04 0.58623946E 01 0.44294946E 04 0.58558532E 01	0.85862244E 02 0.58623946E 01 0.11111772E 03
DAYS 0.30239071E 04 -0.10657655E 01 0.30406620E 04 -0.10806826E 01	0.17558076E 04 -0.13921892E 01 -0.25185055E 01	DAYS 0.30131059E 04 -0.10964456E 01 0.30297110E 04 -0.11115323E 01	0.17415951E 04 -0.14228010E 01 -0.22906741E 01
0.55950000E 04 0.50325674E 04 -0.44343504E 01 0.50160704E 04 -0.44393473E 01	0.53967694E 03 -0.43406573E 01 0.18370758E 04	0.55950000E 04 0.49880104E 04 -0.44852745E 01 C.49714643E C4 -0.44901034F 01	0.4960C824E 03 -0.43913436E 01 0.18128844E 04
TIME FRAM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLCYU UBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSFRVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

		70	10	10	01
(DAYS, DAYS)	(DAYS U.T.)	95542E	8775209E	9403938E	0.21667763E-
0.73250899E 00	0.55950000 04	0.30463147F 04	10877775	503726E	375471
0.55950000E 04	0.56635976E 05	0	8 E	3E	-
ij	11	ji	н	ŧI	li
EPUCH (REE, TO 1950.C)	LP. N. C. J. 2433282.51	POS TEN VECTOR C DATE	VC . DATE)	DELTA RAPIUS	DELTA VELOCITY

IN CLIVARIANCE MATRIX FOR THE ERRORS IN STATE ** P **

0.13020126E-01 0.60142842E-02 -0.33551637E-02 0.15504842E-04 0.85903778E-05
0.14252418E-01 0.63482089E-02 -0.36698815E-02 0.16688244E-04 0.95566515E-05
0.25478090E-01 0.11698431E-01 -0.67141122E-02 0.30198222E-04 0.16688273E-04
005
-0.569085831 -0.263612928 0.158771981 -0.67141157 -0.366988328
0.56908583 0.263612928 0.15877198 0.67141157 0.366988328

THE SALUFICTORY HAS BEEN RECTIFIED

0.44195542E 04	
0.304631476 04	
0.500806095 04	-0.44470568E
11	"
(R DATE	(V DATE
VECTOR (VEC TOR
PASITICA	VELOCIAN

FULLTIN DRBIT ELEMENTS

30E	373676E-		0.24828821E 02			-0.1C912677F-02	-0.32903638F-02
ļļ	Н	Ħ	11	IJ	ij	п	Ħ
(KX)		(DEC)	(DEG)	(DEG)	(DEG)	(RAD)	(RAD)
SEMIMAJOR AXIS	-	TRUF SNOMOLY DATE	R ASC OF ASC NODE	ARG 7- PERIAPSE	ORBI! INCLINATION	DEL NOOF PFR REV	

37E 05 SEC (0.1.) 17E 04	5E 0	6E 0	9E 0	6E 0	5E 01	1E 0	9 E	2E 0	0 E 0	1E 0	0 39		75E 03	0E 01	0E 0	
0.5664598 0.4473681	.583785	.448094	.583130	.137317	0.5837855	.109716	.566559	.453189	.579240		.578578		.1954	9240	107280	
804416		30346189E	11192980E	.17432377E	-0.14304683F 01	1148513E	ΑY	*30068379E	345145E	.30	497971E		.17286098E 0	-0.14607323E 01	.18755139E 0	
0.55950000E 04 0.49791888E 04	.44943137E 0	625513E 0	990809E 0	8803638E 0	-0.44001446E 01	8154650E 0	.55950000E 0	339447E 0	.45442219E 0	49172604E 0	488213E		4369025E 0	-0.44498145E 01	953164F 0	
IME FROM JO	ECIOR (1950)	VECTOR (DAT	VECTOR (DAT	YD OBSERVES ELATIVE POSIT	ATIVE VELOCI	, RDOT, AZ, E	IME FROM JD 2	VECTOR (195	VECTOR (195	ECTO	VECTOR (DAT	SERVE	RELATIVE POSITI	E VEL	, RONT. AZ, EL	OM NI OSSER IN WOLLING

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			0.99383311E-02 0.46383984E-02 -0.23260446E-02 0.11696302E-04 0.65254550E-05 0.64575960E-05			
S, DAYS } S U.T.}	45328723E 04 58007791E 01 62298212E 01 14998540E-01		0.10469589E-01 0.46546090E-02 -0.24487822E-02 0.12041932E-04 0.70372117E-05 0.65254546E-05		45328723E 04 58007791E 01	
0.7327407 ² E 00 (DAY 0.55950000F 04 (DAY	0.30345012E 04 0. 0.11340105E 01 0. 0.11240703E 02 -0. 0.15786513E-01 0.	* * d **	1 0.18516736E-01 0.85789828E-02 1 -0.44796237E-02 2 0.21662593E-04 2 0.12041964E-04 2 0.11696297E-04		0.30345012E 04 0. 0.11340105E 01 0.	
0.5595CCCOE 04 0.5665599F 05	0.49418344E 04 -0.45203459E 01 -0.24573993E 02 0.28475257E-01	ERRORS IN STATE	01 -0.38575959E 0 01 -0.18087653E 0 01 0.10248382E 0 02 -0.44796253E-0 02 -0.24467838E-0 02 -0.24467838E-0	FIFD	0.49418344E 04 (
1950.0) = 2433282.5) =	K (DATE) = K (DATE) = E	MATRIX FOR THE	0.72239416E 0.35409497E -0.18087692E 0.85789567E- 0.46546016E-	HAS BFEN PECTI	(R DATE) = (V DATE) =	ELEMENTS
9 EPOCH 18FL. TO EPOCH 18FL. JO	POSITION VECTOR VELOCITY VECTOR DELTA MABIUS DELTA VELOCITY	THE CIVARIANCE	C.1593680F 02 0.72236501E 01 -C.38575934E 01 C.18516726F-01 0.10469588E-01 0.99383228F-02	THE TRAJECTORY	POSITION VECTOR VELOCITY VECTOR	FLL JPTIC ORBIT

0.75293311E 04 0.24309775E-01 0.23260010E 02 0.24828077E 02 0.15254175E 02 0.81481152E 02 -0.10855744E-02

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SEMIMAJOR AXIS
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(XX)

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SEC (U.T.)	0.27123124E 02	SEC (U.T.)	0.27580292E 02
0.56665989E 05 0.45861779E 04 0.57603918E 01 0.45933485E 04	0.24971613E 03 0.57603918E 01 0.10544583E 03	0.56675980E 05 0.46434984E 04 0.57142836E 01 0.46506021E 04 0.57075524E 01	0.30696967E 03 0.57142836E 01 0.10289645E 03
DAYS 0.30060023E 04 -0.11496529E 01 0.30223521E 04 -0.11650097E 01	0.17244421E 04 -0.14758019E 01 -0.16721438E 01	DAYS 0.29943670E 04 -0.11795580E 01 0.30105626E 04 -0.11950769E 01	0,17C93941E 04 -0,15056379E 01 -0,14226504F 01
0.55950000E 04 0.49124175E 04 -0.45665521E 01 0.48956572E 04 -0.45710540E 01	0.423C3180E 03 -0.44719070E 01 0.17930462E 04	0.55950C00F 04 0.48665507E 04 -0.46152887E 01 0.48457462F 04 -0.46196232E 01	0.378C6763E 03 -0.45204060E 01 0.17774121E 04
TIME FROW JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

			0.78077641E-02 0.368105805-02 -0.16348530E-02 0.90854431E-05 0.51068961E-05 0.52905671E-05		
AYS, DAYS) AYS U.T.)	0.46465382E 04 0.57184050E 01 0.40638185E 01 0.10852657E-01		1 0.79352189E-02 0.35130504E-02 2 -0.16613025E-02 0.89581793E-05 5 0.53624179E-05).46465382E 04).57184050E 01
0.73297200E 00 (D	0.30185294E 04 -0.11841008E 01 0.79669062E 01 0.10976126E-01	***	01 0.13F65820E-01 01 0.64806R12E-02 00 -0.30458396E-02 02 0.16016854E-02 02 0.89582120E-05 02 0.90854387F-05		0.30185294E 04 0 -0.11841C08E 01 0
)) = 0.55950000F 04 32.5) = 0.56675980E 05	TE) = 0.48670094E 04 TE) = -C.45999113E 01 = 0.17262239E 02 = C.19711917E-01	FOR THE ERRORS IN STATE	047125E 01 -0.26676063E 6C4813E 01 -0.12667426E 667466E 01 0.68110189E 806534E-02 -0.30458405E- 130425E-02 -0.16613040E- 810527E-02 -0.16348601E-	EN RECTIFIED	TE) = 0.48670094F 04 TE) = -0.45999113E 01
© EPOCH (REL. TO 1950.0 EPOCH (REL. JD 243328	POSITICN VECTOR (DAT VELOCITY VECTOR (DAT DELTA RADIUS DELTA VELOCITY	THE COVARIANCE MATRIX	0.1215C710F 02 0.55 0.55047272F 01 0.27 -0.26676043E 01 -0.12 0.13865809E-01 0.64 0.79352186F-02 0.35	THE TRAJECTORY HAS BE	POSITICN VECTOR (R DA'NELOCITY VECTOR (V DA

	0.75442856E 04 0.25043313E-01 0.26959002E 02 0.24826047F 02 0.12615058E 02 C.81479958E 02 -0.10815037E-02
MENTS	(KM) (DEG) (DEG) (DEG) (RAD) (RAD)
ELLIPTIC ORBIT ELEMENTS	SEMIMAJOR AXIS ECCENTRICITY TRUE ANGMOLY DATE R ASC OF ASC NODE ARG OF PERIAPSE ORBIT INCLINATION DEL NODE PER REV

0.75442856	0.250433130	0.269590021		0.12615098			-0.32493206
ij	ij	ļí	H	•		,	IJ
(KX)		(DEG)	(DEG)	(DEG)	(DEG)	(RAD)	(RAD)
SEMIMAJOR AXIS		Y DAT	R ASC OF ASC NODE	ARG OF PERIAPSE	ORBIT INCLINATION	DEL NODE PER REV	DEL APSE PFR REV

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TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)		0.55950000E 0 0.48368821E 0 -0.46452088E 0 0.48200123E 0 -0.46494240E 0	004 (001 -(004 (001 -(000 -(001	DAYS 0.29897721E 04 0.11990403E 01 0.30058676E 04 0.12146587E 01	0.56685971E 05 0.46990955E 04 0.56771411E 01 0.47061559E 04 0.56703662E 01	SEC (U.T.)
FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R, ROOT, AZ, ELEV	11 H H	0.34928156E 0 -0.455CC889E 0 0.17743559E 0	133	0.17014458E 04 0.15250512E 01 0.11981570E 01	0.36252350E 03 0.56771411E 01 0.10074713E 03	0.28255942E 02
TIME FRGM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	# H H H H	0.55950000E 04 0.47902346E 04 -0.46928989E 01 0.47733235E 04 -0.46969465E 01	4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		0.56695961E 05 0.47555800E 04 0.56301946E 01 0.47625723E 04 0.56233501E 01	SEC (U.T.)
FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R, RDOT, AZ, ELEV UNDRFLOW AT 33550 IN MQ	"""	0.30354456E 0; -0.45975414E 0 0.17634978E 0	100-	0.16859047E 04 0.15545429E 01 0.93998215E 00	0.41893994E 03 0.55301946E 01 0.98096076E 02	0.23602905E 02

N D

			0.62860539E-02 0.29926433E-02 -0.11542848E-02 0.72350127E-05 0.40998587E-05
AYS, DAYS) AYS U.T.)	0.47592227E 04 0.56333339E 01 0.33496431E 01 0.99838180E-02	•	0.61782866E-02 0.27169866E-02 -0.11358077E-02 0.68390469E-05 0.42105056E-05
0.73320326E 00 (D. 0.55950000E 04 (D.	.30007676E 04 .12346685E 01 .71839305E 01 -	* * C. * *	1 0.10649736E-01 0 0.50196716E-02 0 -0.20943384E-02 2 0.12150148E-04 2 0.68390793E-05 2 0.72350081E-05
0.55950000E 04 0.56695961E 05	0.47887496E 04 0 0.46795872E 01 -0 0.15426056E 02 0 0.17359211E-01 0	ERRORS IN STATE *	1 -0.18688515E 01 1 -0.89925984E 00 0 0.46612856E 00 2 -0.20943393E-02 2 -0.11358093E-02 2 -0.11542919E-02
1950.0) = (2433282.5) = ((DATE) =	MATRIX FOR THE	0.42978318E 01 0.22070814E 01 -0.89926387E 0(0.50196433E-02 0.27169785E-02
G EPOCH (REL. TO EPOCH (REL. JO	POSITICN VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.94938983E 01 0.42978421E 01 -0.18688497E 01 0.10649726E-01 0.61782872E-02 0.62860451E-02

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0.47592227E	0.5633339F
04	01
0.30007676E	-0.12346685E
04	01
	-0.45795872E
11	H
(R DATE)	(V DATE)
CN VECTOR	LY VECTOR
POSITIC	VELOCIT

ELLIPTIC ORBIT ELEMENTS

Ш	0.25716597E-01	30280804E	24823674E	щ	81478908E	III.	-0.32381995E-02
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(KW)		(DEG)	ш	u	(DEG)	(RAD)	(RAD)
SEMIMAJOR AXIS	ECCENTRICITY	UE AN	JF ASC	F PERIA	ORBIT INCLINATION	DEL NOCE PFR REV	EL APSE PER R

SEC (U.T.)	.0.29152541E 02	SEC (U.T.)	0.29373246E 02
0.56705973E 05 0.48111221E 04 0.55911060E 01 0.48180673E 04 0.55842160E 01	0.47443488E 03 0.55911060E 01 0.95808168E 02	0.56715984E 05 0.48668571E 04 0.55432216E 01 0.48737329E 04	0.53010052E 03 0.55432216E 01 0.93081396E 02
DAYS 0.29717348E 04 -0.12489586E 01 0.29875642E 04 -0.12648392E 01	0.16766192E 04 -0.15748302E 01 -0.70697451E 00	DAYS 0.29590845E 04 -0.12782344E 01 0.29747541E 04 -0.12942705E 01	0.16605487E 04 -0.16040362E 01 -0.44314589E 00
0.55950000E 04 0.47578092E 04 -0.47240689E 01 0.47408373E 04 -0.47279914E 01	C.27201514E 03 -0.46284733E 01 0.17635568E 04	0.55950CCOE 04 0.471028C9E C4 -0.47708053E 01 0.469327C6E 04 -0.47745599E 01	0.22540619E 03 -0.46749719E 01 0.17576224E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RCOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =

			0.51929877E-02 0.24949615E-02 -0.81461810E-03 0.59127972E-05 0.33800687E-05 0.38190292E-05								
YS, DAYS) YS U.T.)	.48703337E 04 .55476630E 01 .33991290E 01 .11399619E-01		0.49473142E-02 0.21564669E-02 -0.77915903E-03 0.53644650E-05 0.34094647E-05 0.33800673E-05	•48703337E 04	, ,						
0.73343500E 00 (DA	0.29827978E 04 0 -0.12835999E 01 0 0.80436883E 01 -0 0.10670638E-01 0	** d **	01 0.84001765E-02 00 0.39910588E-02 00 -0.14524485E-02 02 0.94671811E-05 03 0.53644965E-05	0.29827978E 04 0							
0.55950000E 04 0.56715984E 05	0.47103877E 04 0.47555763E 01 0.17117107E 02 0.18983539E-01	E ERRORS IN STATE	01 -0.13242446E 01 -0.64600569E 00 0.33103724E -02 -0.14524497E- -02 -0.77916079E- -02 -0.81462529E-	1FIED 0.47103877E 04 -0.47555763F 01 -		75713	.33/23414E 0 .24821649E 0	.79764781E 0	C.81477331E 0	.10742798E-0	ローコイスのつのファビーロ
0.0) = 3282.5) =	DATE) = DATE) == =	IX FOR TH	.34430392E .18108737E .646C0978E .359103C6E .21564588E	BEEN RECTI DATE) = DATE) =	S	Σ	(DEG) =	DEG)	DEG)	(RAD) = (BAD) =	2
N EPOCH (REL. TO 195 EPOCH (REL. JO 243	POSITICN VECTOR (VELOCITY VECTOR (DELTA RADIUS DELTA VELOCITY	THE COVARIANCE MATR	0.76151541F 01 0.3443C496E 01 -0.13242427E 01 -0 0.84001675E-02 0.49473152E-02 0.51925791E-02	THE TRAJECTORY HAS POSITION VECTOR (R	SIT EL	!	ASC OF ASC	COF PERIAPSE	RBIT INCLINA	DEL MUDE PER REV DEL APSE PER REV	- L A

SEC (U.T.)	0.29834409E 02	SEC (U.T.)	0.29920722E 02
0.56725975E 05 0.49213370E 04 0.55047247E 01 0.49281669E 04 0.54977254E 01	0.58453455E 03 0.55047247E 01 0.90811496E 02	0.56735965E 05 0.49760909E 04 0.54561558F 01 0.49828506E 04 0.54490899E 01	0.63921820E 03 0.54561558E 01 0.88061100E 02
DAYS 0.29535597E 04 -0.12971116E 01 0.29691235E 04 -0.13132415E 01	0.16516628E 04 -0.16228435E 01 -0.21513110E 00	DAYS 0.29404565E 04 -0.13259678E 01 0.29558583E 04 -0.13422492E 01	0.16351431E 04 -0.16516296E 01 0.48799843E-01
0.55950000E 04 0.46788661E 04 -0.47990211E 01 0.46617953E 04 -0.48026562E 01	0.19488959E 03 -0.47029503E 01 0.17628535E 04	0.55950000E 04 0.46306926E 04 -0.48445988E 01 0.46135862E 04 -0.48480664E 01	0.14764172E 03 -0.47482907E 01 0.17618430E 04
ME FROM JD 2433282.5 = VECTOR (1950) = VECTOR (1950) = VECTOR (DATE) = VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R. ROOT. AZ. ELEV =	IME FRCM JO 2433282.5 = VECTOR (1950) = VECTOR (1950) = VECTOR (DATE) = VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

		.44082788E-0 .21356378E-0 .57087202E-0 .49655848E-0	.33695671E-0								
49843626E 04 54432266E 01 15120695E 01 58632712E-02		.40802592E-0 .17603138E-0 .53345071E-0 .43305428E-0	.28652256E-0	49843626E 04 54432266E 01							
.29518284E 04 0. .13475534E 01 0. .40298347E 01 0. .53041209E-02 -0.	* d. *	• 68164854E-0 • 32626860E-0 • 10132225E-0 • 75900771E-0	.49655795E-0	29518284E 04 0. 13475534E 01 0.							
0.46050422E 04 0 0.48573963E 01 -0 0.85240469E 01 -0 0.93299133E-02 -0	ERRORS IN STATE *	1 -0.94783141E 0 1 -0.46895583E 0 0 0.24638392E 0 2 -0.10132242E-0	2 -0.57087944E-0	0.46050422E 04 0		75653608E 0 26087942E-0	34043023E 0	88831836F O	81480377E 0	107554905-0	32316264E-0
DATE) = - DATE) = -	TRIX FOR THE	.28357921E .15261286E .46895995E .32626583E-	0.21356323E-	R DATE) = V DATE) = V	EMENTS		# (S)	1 (9	ii (9)	- = (0	- = (0
POSITICN VECTOR (VELOCITY VECTOR (OELTA RADIUS DELTA VELOCITY	THE COVARIANCE MA	6286C913E 0 28358024E 0 94782928E 0 68164777E-0	440827C2E-02 E TRAJECTORY HA	OSITION VECTOR (ELOCITY VECTOR (ELLIPTIC ORBIT EL		RUE ANDMOLY DAT	RG OF PERIAPSE	RBIT INCLINA	EL NODE PER	EL APSE PER
	SITICN VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.49843626E 0 LOCITY VECTOR (DATE) = -0.48573963E 01 -0.13475534E 01 0.54432266E 0 LTA RADIUS = -0.85440469E 01 -0.40298347E 01 0.15120695E 0 LTA VELOCITY = -0.93299133E-02 -0.53041209E-02 -0.58632712E-0	SITICN VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.49843626E 0 LOCITY VECTOR (DATE) = -0.48573963E 01 -0.13475534E 01 0.54432266E 0 LTA RADIUS = -0.85440469E 01 -0.40298347E 01 0.15120695E 0 LTA VELOCITY = -0.93299133E-02 -0.53041209E-02 -0.58632712E-0 E COVARIANCE MATRIX FOR THE ERRORS IN STATE ** P **	SITICN VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.49843626E 04 LOCITY VECTOR (DATE) = -0.48573963E 01 -0.13475534E 01 0.54432266E 01 LTA RADIUS LTA VELOCITY LTA VELOCITY LTA VELOCITY E COVARIANCE MATRIX FOR THE ERRORS IN STATE	SITICN VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.49843626E 04 LOCITY VECTOR (DATE) = -0.48573963E 01 -0.13475534E 01 0.54432266E 01 LTA RADIUS	SITICN VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.49843626E 04 LTA RADIUS	SITICN VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.49843626E 04 LUGITY VECTOR (DATE) = -0.48573963E 01 -0.13475534E 01 0.54432266E 01 LTA VELOCITY LTA VELOCITY	OSITICN VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.4984362EE 04 0.4984362EE 04 0.4984362EE 04 0.4984362EE 01 0.4605042E 01 0.4605042E 01 0.4602834TE 01 0.5443226EE 01 0.46226EE 01 0.46226EE 01 0.462695E 01 0.462696EE 02 0.4608278EE 02 0.4608278EE 02 0.1526428EE 02 0.462866EE 02 0.462866EE 02 0.462878EE 02 0.462878EE 02 0.462878EE 02 0.462878EE 02 0.462878EE 02 0.4663832EE	OSITION VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.49843626E 04 ELLOITY VECTOR (DATE) = -0.485793E 01 -0.1347534E 01 0.5543256E 01 ELLOITY VECTOR (DATE) = -0.4957963E 01 -0.429347E 01 0.15120695E 01 -0.49843626E 01 0.15120695E 01 -0.49843626E 01 0.15120695E 01 -0.49823712E-02 -0.53641209E-02 -0.58632712E-02 -0.53641209E-02 -0.58632712E-02 -0.53641209E-02 -0.58632712E-02 -0.53641209E-02 -0.58632712E-02 -0.53641209E-02 -0.58632712E-02 -0.53641209E-02 -0.17603138E-02 -0.17603138E-03 -0.17603138E-0	OSITICN VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.49843626E 04 FELCITY VECTOR (DATE) = -0.4645963E 01 -0.13475534E 01 0.15120695E 01 FELCITY VECTOR (DATE) = -0.4646469E 01 -0.4020934TE 01 0.15120695E 01 FELTA VELOCITY FELCITY VECTOR (DATE) = -0.93299133E-02 -0.53041209E-02 -0.58632712E-02 FELTA VELOCITY FELCITY VECTOR (DATE) = -0.93299133E-02 -0.53041209E-02 -0.536432712E-02 FELTA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE ERRORS IN STATE ** P ** FELCA VELOCITY FOR THE TRAJECTORY HAS BEEN RECTIFIED OSTITION VECTOR (K DATE) = -0.46050422E 04 0.29518284E 01 0.54432266E 01 FELCA VELOCITY FOR THE TRAJECTORY VECTOR (K DATE) = -0.48573963E 01 -0.13475534E 01 0.54432266E 01 FELCA VELOCITY FOR THE	OSITICN VECTOR (DATE) = 0.446050422E 04 0.29518284E 04 0.49843626E 04 0.4984362E 01 0.4605042E 01 0.46029347E 01 0.544522E6E 01 0.46029347E 01 0.544522E6E 01 0.46029347E 01 0.544526E 01 0.46029347E 01 0.544526E 01 0.46029347E 01 0.544526E 01 0.46029347E 01 0.544526E 01 0.46029347E 01 0.46029347E 01 0.46029347E 01 0.46029347E 01 0.4603796E 02 0.46090592E 00 0.45409059E 00 0.46090592E 00 0.49090592E 00 0.4909059E 0	SITICN VECTOR (DATE) = 0.46050422E 04 0.29518284E 04 0.49843626E 01

	02		02
SEC (U.T.)	0.29810550E	SEC (U.T.)	0.29733447E
0.56745977E 05 0.50345444E 04 0.53990615E 01 0.50412192E 04 0.53919145E 01	0.69758679E 03 0.53990615E 01 0.84918569E 02	0.56755988E 05 0.50883471E 04 0.53492337E 01 0.50949500E 04 0.53420215E 01	0.75131763E 03 0.53492337E 01 0.82170632E 02
DAYS 0.2922744E 04 -0.13603957E 01 0.29374807E 04 -0.13768619E 01	0.16135071E 04 -0.16859871E 01 0.34770581E 00	DAYS 0.29085117E 04 -0.13890298E 01 0.29235523E 04 -0.14056446E 01	0.15963211E 04 -0.17145507E 01 0.61107774E 00
0.55950C00E 04 0.45724467E 04 -0.49001309E 01 0.45553165E 04 -0.49034000E 01	C. 90336914E 02 -0.48035852E 01 0.17601685E 04	0.55950000E 04 0.45231660E 04 -0.49447980E 01 0.45060040E 04 -0.49478985E 01	0.41991699E 02 -0.48480147E 01 0.17647897E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD GBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R. ROOT. A7. ELEV =

UNDRFLOW AT 33550 IN MQ

(DAYS, DAYS) (DAYS U.T.)	0.50952590E 04 0.53405868E 01 0.30897555E C0 -0.14347029E-02
0.73389801E 00 0.55950000E 04	0.29225968E 04 -0.14069025E 01 -0.95555549E 00 -0.12579913E-02
0.55950000E 04 0.56755988E 05	0.45039788E 04 -0.49500748E 01 -0.20252047E 01 -0.21762910E-02
H tI	n n n
CH (REL. TO 1950.0) CH (REL. JD 2433282.5)	POSITICN VECTOR (DATE) VELOCITY VECTOR (DATE) DELTA RADIUS DELTA VELOCITY
EPOCH	POS VEL DEL DEL

THE COVARIANCE MATRIX FOR THE ERRORS IN STATE ** P **

0.38096787E-02 0.18594624E-02 -0.38634342E-03 0.42447113E-05 0.24740744E-05
0.343269)8E-02 0.14632861E-02 -0.35536857E-03 0.35619463E-05 0.24340928E-05
0.56345648E-02 0.27153228E-02 -0.69749247E-03 0.61984103E-05 0.35619751E-05
-0.67438260E 00 -0.33869328E 00 0.19241503E 00 -0.69749461E-03 -0.35537078E-03
0.23779263E 01 0.13085026E 01 -0.33869741E 00 0.27152958E-02 0.14632783E-02
0.52892697E 01 0.23779363E 01 -0.67438018E 00 0.56345585E-02 0.34326923E-02 0.38096704E-02

THE TRAJECTORY HAS BEEN RECTIFIED

40	01
0.50952590E	.53405868E
	01
0.29225968E	-0.14069025E
04	0
0.45039788E	-0.49500748E
11	II
(R DATE)	(V DATE)
VECTOR	VECTOR
OSITION	VELOCITY

ELLIPTIC ORBIT ELEMENTS

540149	0	226962E	0.24807950E 02	83479	1482015E	7120E-0	-0.32328847E-02
Ð	II	33	H	H	II	11	Iį
X X		(DEG)	(DEG)	w	(DEG)	(RAD)	(RAD)
SEMIMAJOR AXIS	ECCENTRICITY	TRUE ANCHOLY DATE	SC	ARG OF PERIAPSE	ORBIT INCLINATION	DEL NODE PER REV	L APSE PER RE

SEC (U.T.)	0.29569404F 02	SEC (U.T.)	0.29342310E 02
0.56765979E 05 0.51444072E 04 0.52955181E 01 0.51509333E 04 0.52882372E 01	0.80730096E 03 0.52955181E 01 0.79289180E 02	0.56775969E 05 0.51970599E 04 0.52447619E 01 0.52035131E 04 0.52374175E 01	0.85988068E 03 0.52447619E 01 0.76609653E 02
DAYS 0.28928168E 04 -0.14189453E 01 0.29076808E 04 -0.14357165E 01	0.15771972E 04 -0.17443956E 01 0.88662280E 00	DAYS 0.28784993E 04 -0.14472054E 01 0.28931950E 04 -0.14641213E 01	0.15594597E 04 -0.17725849E 01 0.11425785E 01
0.55950000E 04 0.44706077E 04 -0.49918471E 01 0.44534170E 04 -0.49947691E 01	-C.96271362E 01 -C.48948267E 01 0.17718291E 04	0.55950000E 04 0.44205178E 04 -0.50353837E 01 0.44032988E 04 -0.50381370E 01	-0.58774597E 02 -0.49381261E 01 0.17817867E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R. ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV T

UNDRFLOW AT 33550 IN MQ

			0.33696339E-02 0.16553338E-02 -0.24678409E-03 0.37122673E-05 0.21868719E-05				
'S, DAYS) 'S U.T. }	52037346E 04 52361878E 01 22155910E 00 12296080E-02		0.29608230E-02 0.12467744E-02 -0.22645126E-03 0.30018262E-05 0.21336416E-05		52037346E 04 52361878E 01		
0.73412928E 00 (DAY 0.55950000F 04 (DAY	0.28923944F 04 0. -0.14651641E 01 0. -0.80059736E 00 0. -0.10428051E-02 -0.	** d **	0 0.47717908E-02 0 0.23137061E-02 0 -0.47110161E-03 0.51854158E-05 0.30018535E-05		0.28923944E 04 0. -0.14651641E 01 0.		•
0.55950000E 04 0.56775969E 05	0.44016112E 04 -0.50399230E 01 - -0.16875151E 01 - -0.17859844E-02 -	E ERRORS IN STATE	01 -0.47639907E 0 01 -0.24311736E 0 00 0.15942915E 0 -02 -0.47110421E-0 -02 -0.22645373E-0	IFIED	0.44016112E 04 -0.50399230E 01 -		0.75625949E 04 C.25812171E-01 0.36527850E 02 0.24801555E 02 0.87612374E 01 0.81483406E 02 -0.10759252E-02 -0.32341792E-02
950.0) = 433282.5) =	(DATE) = (DATE) = = = = = = = = = = = = = = = = = =	ATRIX FOR THE	0.20428281E 0.11469209E -0.24312149E 0.23136800E 0.12467668E	S BEEN RECT	(R DATE) = (V DATE) =	EMENTS	(KM) = (OEG) = (DEG) = (DEG) = (RA) = (RAD) =
© EPOCH (REL. TO 19 EPOCH (REL. JD 24	POSITION VECTOR (VELOCITY VECTOR (DELTA RADIUS DELTA VELOCITY	THE COVARIANCE MA	0.45616C83E 01 0.20428377E 01 -0.47635635E 00 0.47717859E-02 0.256C8246E-02 0.33696257E-02	THE TRAJECTORY HA	POSITICN VECTOR (ELLIPTIC ORBIT EL	SEMIMAJOR AXIS ECCENTRICITY TRUE ANOMOLY DATE R ASC OF ASC NODE ARG OF PERIAPSE ORBIT INCLINATION DEL NODE PER REV

E FROM JO	И	.55950000E 0	4	AYS	0.56785980E 05	SEC (U.T.)
ECT0R (1950	II	3672844E 0	à,	.28623478F 0	.52520501E 0	
ECTOR (1950	11	50808395E 0	•	4765157E 0	.51900483E 0	
CTOR (DATE	đ	3500398F 0	7	.2	•52584256E 0	
ECTOR (DATE	11	C834649E 0	·	4935828E 0	.51826375E 0	
O OBSERVE						
FLATIVE POSITIO	ij	11C5920E 0	m	15358739E 0	.91479321F 0	
LATIVE VEL	11	3946E 0	, ,1	-0.18018241F 01	0.51900483E 01	
, RDOT, AZ, ELE	Ħ	945451E 0	4	.14079840E 0	.73824601E O	0.29032542E 02
E FROM JD 2	11	5950000E	. †	ΑY	.55795992E 0	SEC (U.T.)
CTOR (195	IJ	3162046E	. †	.28474258E 0	.53037499E 0	
ECT03 (1950	H	1234562E	1	0.15045051E 0	.51381832E 0	
ECTOR (DATE	{	ш	ς†-	0.28617711E 04	0.53100510E 04	
CTOR (DAT	ii	1259622	•	.15217138E 0	.51307102E 0	
YD OBSFRVE						
ELATIVE POSITIO	11	6118573F 0	w.	15215206E 0	.96641858E 0	
LATIVE VELOC	Ħ	257235E 0		-0.18297423E 01	0.51381832F 01	
, RDOT, AZ, ELE	JI	8095880E 0	4	16531689E 0	.71247322E 0	0.28669081E 02

UNDRFLOW AT 33550 IN MQ

			0.30506968E-02 0.15069055E-02 -0.13834314E-03 0.3321023E-05 0.19782208E-05
YS,DAYS) YS U.T.)	.53101990E 04 .51297004E 01 .14807598E 00 .10098147E-02		0.26170461E-02 0.10896517E-02 -0.13071795E-03 0.25914782E-05 0.19160846E-05
.73436102E 00 (DA)	.15225428E 04 0. .15225428E 01 0. .64331163E 00 0. .82896966E-03 -0.	* * d *	0.41402766E-02 0.20187490E-02 -0.30490845E-03 0.44430394E-05 0.25915041E-05 0.33210158E-05
•5595C000E 04 0.	• 42975869E 04 0 • 51272674E 01 -0 • 13481887E 01 -0 • 14051696E-02 -0	ERRORS IN STATE **	-0.32964701E 00 -0.17127345E 00 0.14020236E 00 -0.30491143E-03 -0.13072068E-03
1950.0) = C. 2433282.5} = O.	(DATE) = 0 (DATE) = -0 = -0	MATRIX FOR THE EF	0.17990828E 01 0.10275135E 01 -0.17127753E 00 0.20167238E-02 0.10896443E-02 0.15069012E-02
S EPOCH (REL. TO EPOCH (REL. JO	POSITICN VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.40321047E 01 0.1799C920E 01 -0.32964399E 00 0.41402730E-02 0.26170478E-02 0.30506888E-02

ELLIPTIC ORBIT ELEMENTS

THE TRAJECTORY HAS BEEN RECTIFIED

0.53101990E 04 0.51297004E 01

0.28611278E 04 -0.15225428E 01

04 01

Щ	25651617E-		m	m	ш	En I	2355151E-
ļi	Ħ	Ц	11	II	H	Ħ	H
(XX)		(DEG)	ш	(DEG)	(DEG)	Ø	4 .7
SEMIMAJOR AXIS	ECCENTRICITY	MOLY DAT	ASC OF ASC	ARG OF PERIAPSE	ORBIT INCLINATION	DEL NODE PER REV	EL APSE PER RE

IME FROM JD 2433282.5	Ħ	5950000E 0		ΑY	.56805982E 0	SEC (U.T.)
ECTUR (1950)	11	.426253		28308924E	0.53574481E 04	
CTOR (195	1)	1672257E 0	ŀ		.50827404E 0	
ECTOR (DAT	! !	.42452444E 0		.28450575E	.53636708E 0	
_	Ħ	1694552E 0	ı	5504309E	.50752035E 0	
OBSERVES		0 11/10/00/10 0		7.632		
FLAIIVE FUN		-0 -0 -0 -0 -0 -0 -0 -0 -0 -0 -0 -0 -0 -) C	0.10010014E 04	0 50827404F 01	
ELAIIVE VELUCI	ij	0 310626006.0		* 10 302 420E	0 110000000	
, RDOT, AZ, EL	11	8278145E C		.19031691E	•68610835E 0	0.28234589E 02
E FROM JD 2	11	5950000E		AYS ,	.56815973	SEC (U.T.)
ECTUR (1950)	II	.42107049E		.28154380E 0	.54079653E 0	
ECT03 (195	П	2086313E	ŧ	.15606683E 0	.50300118E 0	
ECTOR (DAT	ĮĮ	.41933915E		0.28294290E 04	0.54141124E 04	
ECTOR (DA	II	6915	1	.15781600E 0	.50224145E 0	
D CBSERVE						
ELATIVE POSITIO	11	.26477148E 0		.14826803E 0	.10704800E 0	
ELATIVE VEL	II	-0.51104248E 01	\$	0.18857627E 01	0.50300118E 01	
, RDUT, AZ, ELE	11	.18478020E 0		•21331498E 0	.66180216E 0	0.27756544E 02

UNDRFLOW AT 23550 IN MQ

			0.28220602E-02 0.14004585E-02 0.51272011E-04 0.30335407E-05 0.18276804E-05			
DAYS, DAYS) DAYS U.T.)	0.54142167E 04 0.50215121E 01 0.10433077E 00 -0.90237358E-03		02 0.23654449E-02 02 0.97571689E-03 03 .0.57444988E-04 05 0.22878058E-05 05 0.17577487E-05 05 0.18276802E-05	0.54142167E 04 0.50215121E 01		
0.73459229E 00 ((0.28288652E 04 0.15788771E 01 -0.56377818E 00 -0.71705695E-03	* * * *	00 0.36744718E- 00 0.18008752E- 00 -0.17946652E- -03 0.38927084E- -04 0.22878303E-	0.28288652E 04 -0.15788771E 01		•
= 0.55950000E 04 = 0.56815973E 05	= 0.41922181E 04 = -0.52118960E 01 = -0.11733451E 01 = -0.12045291E-02	THE ERRORS IN STATE	35E 01 -0.21765470E 42E 00 -0.11564752E 54E 00 0.13015359E 09E-02 -0.17946981E 64E-03 -0.57447978E 47E-02 -0.51280655E	ECTIFIED = 0.41922181E 04 = -0.52118960E 01		= 0.75593933E 04 = 0.25472217E-01 = 0.39486772E 02 = 0.24788316E 02 = 0.81528981E 01 = 0.81485473E 02 = -0.10765397E-02 = -0.32369986E-02
1950.0) 2433282.5)	(DATE) (DATE)	MATRIX FOR	0.162217 0.9393194 -0.1156519 0.18C0850 0.975769	HAS BEEN R (R DATE) (V DATE)	ELEMENTS	(KM) TE (DEG) DE (DEG) ON (DEG) V (RAD)
R EPOCH (REL. TO EPOCH (REL. JO	POSITION VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.36462679E 01 0.16221823E 01 -0.21765140E 00 0.36744654E-02 0.23654466E-02	THE TRAJECTORY POSITICN VECTOR VELOCITY VECTOR	ELLIPTIC ORBIT	SEMIMAJOR AXIS ECCENTRICITY TRUE ANOMOLY DA R ASC OF ASC NO ARG OF PERIAPSE ORBIT INCLINATI DEL NODE PER RE

	: 02		.: 02
SEC (U.T.)	0.27215741E	SEC (U.T.)	9.26644004E
0.56825984E 05 0.54605928E 04 0.49735554E 01 0.54666605E 04 0.49658963E 01	0.11230281E 04 0.49735554E 01 0.63705619E 02	0.56835996E 05 0.55101157E 04 0.49197735E 01 0.55161064E 04 0.49120553E 01	0.11724741E 04 0.49197735E 01 0.61433715E 02
DAYS 0.27983954E 04 -0.15887006E 01 0.28122036E 04 -0.16063330E 01	0.14622020E 04 -0.19137232E 01 0.23661706E 01	DAYS 0.27823537E 04 -0.16159961E 01 0.27959847E 04 -0.16337627E 01	0.14427311E 04 -0.19409468E 01 0.25795443E 01
0.55950000E 04 0.41562554E 04 -0.52509974E 01 0.413892295 04 -0.52528815E 01	-0.31825616E 03 -0.51525537E 01 0.18709660E 04	0.55950000E 04 0.41034835E 04 -0.52913960E 01 0.40861329E 04 -0.52931103E 01	-0.370C5975E 03 -0.51927152E 01 0.18955508E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV = UNDRFLOW AT 33550 IN MQ

			0.26619730E-02 0.13263095E-02 0.21636019E-04 0.28231382E-05 0.17207560E-05 0.23896263E-05	
rs, DAYS) rs u.t.)	.55161741E 04 .49112634E 01 .67740413E-01 .79188447E-03		0.218071 0.893525 0.899400 0.206043 0.164199 0.172075	.55161741E 04 .49112634E 01
0.73482403E 00 (DAY 0.55950000E 04 (DAY	0.27954996E 04 0. -0.16343726E 01 0. -0.48511968E 00 0. -0.60984703E-03 -0.	* * d * *	0.32281316E-0. 0.16391146E-0. -0.81226991E-0. 0.34791018E-0. 0.20604546E-0.	0.2/954996E 04 0 -0.16343726E 01 0
0.55950000E 04 0.56835996E 05	0.40851295E 04 -0.52941244E 01 -r.10033764E 01 -0.10142095E-02	E ERRORS IN STATE	01 -0.12879043E 00 -0.70858383E- -01 0.12635755E -02 -0.81230513E- -03 0.89615719E- -02 0.21627089E-	0.40851295E 04 -0.52941244E 01
1950.0) = 2433282.5} =	DR (DATE) = 3R (DATE) = 4	E MATRIX FOR THE	0.14947918E 0.87454312E -0.7C862310E 0.16390910E 0.89351818E 0.13263061E	OR (R DATE) = OR (V DATE) =
GE - TO CH (REL. TO EPOCH (REL.	POSITION VECTOR VFLOCITY VECTOR DELTA RABIUS DELTA VELOCITY	THE COVARIANCE	3336 3336 336 51	POSITICN VECTOR VELOCITY VECTOR

0.75574844E 04 0.25276957E-01 0.41138099E 02 0.24781423E 02 0.76744313E 01 0.81486180E 02 -0.10769735E-02

H H H H H H H H

SEMIMAJOR AXIS
ECCENTRICITY
TRUE ANOMOLY DATE
R ASC OF ASC NODE
ARG OF PERIAPSE
ORBIT INCLINATION
DEL NODE PER REV

(KM)

ELLIPTIC ORBIT ELEMENTS

(DEG) (DEG) (DEG) (RAD) (RAD)

05 SEC (U.T.) 04 01 04	04 01 02 0.26023618E 02	05 SEC (U.T.) 04 01 04 01)4)1)2 0.25383678E 02
0.56845986E (0.55814535E (0.48625682E (0.55673640E (0.48547905E (0.12237316E (0.48625682E (0.59147023E (0.56855977E (0.56097617F (0.48079840E (0.56155942E (0.48001491E (0.12719618F 0 0.48079840E 0 0.57052509E 0
DAYS 0.27648779E 04 -0.16433635E 01 0.27783242E 04 -0.16612656E 01	0.14218239E 04 -0.19682422E 01 0.27928050E 01	DAYS 0.27483252E 04 -0.16702398E 01 0.27615920E 04 -0.16882721E 01	0.14018460E 04 -0.19950463E 01 0.29874605E 01
0.55950000E 04 0.40484927E 04 -0.53321789E 01 0.40311263E 04 -C.53337181E 01	-0.42407928E 03 -0.52332613E 01 0.19232643E C4	0.55950000E 04 0.39950242E 04 -0.53713904E 01 0.39776433E 04 -0.53727600E 01	-0.47657278E 03 -0.52722361F 01 0.19519684E 04
TIME FROM JD 2432282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) = F	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R; ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELFV = UNDRFLOW AT 33550 IN YQ

			0.25532510E-02 0.12766683E-02 0.85144790E-04 0.26695006E-05 0.16462227E-05 0.23479941E-05
(DAYS,DAYS) (DAYS U.T.)	.56156322E 04 47994752E 01 38078536E-01 67387668E-03		0.20443851E-02 0.83458117E-03 0.49126507E-04 0.18877962E-05 0.15568317E-05
.73505530F 00 (DAY	.27611872E 04 0. .16887757E 01 0. .40479624E 00 0. .50365795E-03 -0.	* *	0.30679369E-02 0.15181459E-02 -0.15610731E-05 0.31633296E-05 0.18878183E-05 0.26694930E-05
.55950000E 04 0.	.397681C7E 04 0.2 .53735884E 01 -0.1 .832568C9E 00 -0.4 .87538651E-03 -0.5	ERRORS IN STATE **	-0.55522562E-01 -0.33398278E-01 0.12700576E 00 -0.15647483E-05 0.49123018E-04
1950.0 $1 = C.$ $2433282.5) = 0.$	(DATE) = 0 (DATE) = -0 = -0	MATRIX FOR THE EF	0.14038508E 01 0.82725813E 00 -0.33402103E-01 0.15181229E-02 0.83457421E-03 0.12766653E-02
919 EPOCH (RFL. TO EPOCH (REL. JD	POSITICN VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.31619938E 01 0.14036989E 01 -0.55518792E-01 0.30679365E-02 0.20443869E-02

0.39768107E	-0.53735884E
11	II
DATE)	DATE)
<u>R</u>	>
VECTOR	VECTOR
POSITION	VELOCITY

ELLIPTIC ORBIT ELEMENTS

THE TRAJECTORY HAS BEEN RECTIFIED

0.56156322E 0.47994752E

0.27611872E 04 -0.16887757E 01

04 01

0.75553696E 04	597E-	42904823E	0.24774336E 02		3670E	-0.10774923E-02	
JI	II	11	ř*	H	li	11	II
(KW)		(DEG)	(DEG)	(DEC)	(DEG)	(RAD)	(RAD)
SEMIMAJOR AXIS	ECCENTRICITY	TRUE ANOMOLY DATE	R ASC OF ASC NODE	ARG OF PERIAPSE	ORBIT INCLINATION	DEL NODE PER REV	DEL APSE PER REV

SEC (U.T.)	0.24706215E 02	SEC (U.T.)	0.24017990F 02
0.56865968E 05 0.56599033E 04 0.47499732F 01 0.56454547F 04 0.47420810E 01	0.13220223F 04 0.47499732E 01 0.54954942E 02	0.56875958E 05 0.57070821E 04 6.46945059F 01 0.57127543F 04 0.46865580E 01	0.13691219F 04 0.46945059E 01 0.53036331E 02
DAYS 0.27303988E 04 -0.16969849E 01 0.27434790E 04 -0.17151475E 01	0.13804877E 04 -0.20217191E 01 0.31806648E 01	DAYS 0.27133122E 04 -0.17234874E 01 0.27262103E 04 -0.17417765E 01	0.13599744E 04 -0.20481491E 01 0.33567252E 01
0.55950000E 04 0.39394167E 04 -0.54106622E 01 0.39220232E 04 -0.54118577E 01	-0.53120084E 03 -0.53112713E 01 0.19838507E 04	0.55950000E 04 0.38851697E 04 -0.54487562E 01 0.36677551F 04 -0.54497821E 01	-0.58446460F 03 -0.53491287E 01 0.20163393F 04
TIME FROM JD 2432282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RFLATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =	TIME FRG* JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLUYD OBSFRVES RELATIVE POSITION = RELATIVE VELOCITY = R; RDOT, AZ, ELEV = UNDRFLOW AT 33550 IN 40

		.24842127E-62 .12462634E-02 .14284012E-03 .25585377E-05 .15963738E-05
(DAYS, DAYS) {DAYS U.T.}	57127747E 04 46858867E 01 20442979E-01 67122000E-03	0.19437159E-02 0.79301952E-03 0.90658076E-04 0.17549013E-05 0.14939706E-05 0.15963744E-05
73528656E 00 55950000F 04	27258134F 04 0. 17422627E 01 0. 39685396E 00 0. 48619946E-03 -0.	* p ** 0.28707638E-02 0.14273C50E-02 0.65603963E-04 0.29183048E-05 0.17549222E-05
55950000F 04 0. 56875958E 05 0.	38669553E 04 0. 54505754E 01 -0. 80973204E 00 -0. 79328725E-03 -0.	ERRORS IN STATE ** 1
ro 1950.0) = C.	TOR (DATE) = 0. TOR (DATE ; = -0.	MATRIX FOR THF 0.134C5050E 0 0.79336971E 0 -0.72275603E-0 0.14272826E-0 0.79301268E-0 0.79301268E-0
FPOCH (REL. J	POSITICN VECT VELNCITY VECT NELTA RABIUS DELTA VELNCIT	THE COVARIANCE 0.30155386E 01 0.13405128E 01 0.75354029E-02 0.28707642E-02 0.19437177E-02

POSITICN VECTOR	8 8	DATE)	0 II	0.38669553F 04	0.27258134E 04	0.57127747E 04
VELOCITY VECTOR	8 5	OATE)		-0.54505754E 01	-0.17422627E 01	0.46858867E 01
11800 71101110	ü	Z Z Z				

THE TRAJECTORY HAS BEEN RECTIFIED

0.75529485E 04	Į			0.63654473E 01		-0.10781209E-02	-0.32424589E-02
11	11	Ħ	ŧŧ	Ħ	H	II	II
(KM)		(DEC)	(DEG)	(DEG)	(DEG)	(RAD)	(RAD)
SEMIMAJOR AXIS	ECCENTRICITY	TRUE ANOMOLY DATE	R ASC OF ASC NODE		DRBIT INCLINATION	DEL NODE PER REV	L APSE PER RE

I

TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	пппп	0.55950000E 0.38287134E -0.54867278E 0.38112996E -0.54875798E	04 04 01 04 01	DAYS 0.26948396E 04 -0.17497378E 01 0.27075481E 04 -0.17681530E 01	0.56885970E 05 0.57561172E 04 0.46355009E 01 0.57617071E 04 0.46274976E 01	SEC (U.T.)
FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R, ROOT, AZ, ELEV	11 11 11	-0.63993198E -0.53868635E 0.20520389E	03 01 04	0.13380639E 04 -0.20743267E 01 0.35306986E 01	0.14180747E 04 0.46355009E 01 0.51115834E 02	0.23299059E 02
TIME FROM JD 2433282,5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	11 11 11 11 11	0.55950000E C.37735983E -0.55237656E 0.37561768E -0.55244477E	04 01 01 01	DAYS 0.26771913E 04 -0.17759096E 01 0.26897149E 04 -0.17944477E 01	0.56895981E 05 0.58022424E 04 0.45790605E 01 0.58077520E 04 0.45710031E 01	SEC (U.T.)
FLCYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R; ROOT, AZ; ELEV	11 11 11	-C.694C5426E -O.54236643E O.20880138E	03 01 04	0.13169830E 04 -0.21004256E 01 0.36P88570E 01	0.14641196E 04 0.45790605E 01 0.49363441E 02	0.22579087E 02
UNDRFLOW AT 33550 IN MQ	œ					

- 519 -SID 65-1203-1

			244636135 12312467E 19732716E 24799969E	.15654066E-0 .23461889E-0		
AYS, DAYS } AYS U.T.)	0.58077543E 04 0.45704088E 01 0.23362258E-02 0.59430349E-03		2 0.18696148E-02 2 0.76463254E-03 3 0.12783574E-03 5 0.16511290E-05	0.14475297E-0 0.15656073E-0		0.58077543E 04 0.45704088E 01
0.73551831E 00 (D 0.55950000E 04 (D	0.26893699E 04 -0.17948661E 01 -0.34495654E 00 -0.41840800E-03	* * *	01 0.27201645E-0 01 0.13589457E-0 00 0.12437948E-0 03 0.27249171E-0	03 0.16511489E-0 03 0.24799886E-0		0.26893699E 04 -0.17948661E 01
0.55950000E 04 0.56895981E 05	0.37554767E 04 -0.55251225E 01 -0.70014572E 00 -0.67480320E-03	ERRORS IN STATE	01 0.64098996E- 00 0.28970017E- 01 0.13763373E 02 0.12437570E-	3 0.12783179 2 0.19731750	FIED	0.37554767E 04 -0.55251225E 01
1950.0) = 2433282.5) =	(DATE) = (DATE) = = = = = = = = = = = = = = = = = =	: MATRIX FOR THE	0.12981846E 0.76991492E 0.28966438E- 0.13589238E-	0.12312445E-	HAS BEEN RECTI	R (R DATE) = R (V 3ATE) =
S EPOCH (REL. TO EPOCH (REL. JD	POSITICN VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	29123604E 12931922F 64103110E 27201656E	.186961675-0 .24463538E-0	THE TRAJECTORY	POSITION VECTO

C.75502838E 04	.46786610E	.24759491E	28E	.81487071E	47E-	275-
11 11	Iļ	ij	II	11	ł	II
(KM)	ш	OE	(DEG)	ш	◂	(RAD)
SEMIMAJOR AXIS ECCENTRICITY	RUE AND	SC OF ASC	OF PERIAPSE	BIT INCLIN	L NOOE PER RE	EL APSE PER R

SEC (U.T.)	0.21840970E 02	SEC (U.T.)	0.211070646 02
0.56905972E 05 0.58499607E 04 0.45194C98E 01 0.58553871E 04 0.45112993E 01	0.15117547E 04 0.45194098E 01 0.47622239E 02	0.56915962E 05 0.58948276E 04 0.44622586E 01 0.59001727E 04 0.44540957E 01	0.155854use U4 0.44622586E O1 0.46033250F 02
DAYS 0.26583001E 04 -0.18014918E 01 0.26706325E 04 -0.18201507E 01	0.12946583E 04 -0.21259347E 01 0.38434091E 01	DAYS 0.26401732E 04 -0.18272156E 01 0.26523186E 04 -0.18459934E 01	0.12731028E 04 -0.21515854E 01 0.39839547E 01
0.55950000E 04 0.37166350E 04 -0.55601816E 01 0.36992077E 04 -0.55606911E 01	-0.75002191E 03 -0.54598439E 01 0.21269873E 04	0.55950000E 04 0.36609055E 04 -0.55959995E 01 0.36434740E 04 -0.55963396E 01	-0.80475186E 03 -0.54954255E 01 0.21659257E 04
TIME FROM JD 2433282,5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) = F	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDCT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

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			0.24325936E-02 0.12283239E-02 0.25022358E-03 0.24257481E-05 0.15493522E-05
/S, DAYS) /S U.T.)	.59001613E 04 44535230E 01 11443097E-01 57272184E-03		0.18152158E-02 0.74615302E-03 0.16208031E-03 0.15687529E-05 0.14131185E-05
3574957E 00 (DAYS, 5950000E 04 (DAYS	6519911E 04 0.8463847E 01 0.2748242E 00 -0.9139928E-03 -0.	* *	0.26039345E-02 0.13072923F-02 0.17726610E-03 0.25694359E-05 0.15687719E-05
5950000E 04 0.7 6915962E 05 0.5	6428143E 04 0.2 5969653E 01 -0.1 5971595E 00 -0.3 2565282E-03 -0.3	ORS IN STATE **	0.11649307E 00 0.56785070E-01 0.14654554E 00 0.17726235E-03 0.16207614E-03 0.25021370E-03
950.0) = 0.55 433282.5) = 0.56	DATE) = 0.3 DATE) = -0.5 = -0.6	MATRIX FOR THE ERRORS	0.12718376E 01 0.75453749E 00 0.56781634E-01 0.13672710E-02 0.74614539E-03 0.12283221E-02
EPOCH (REL. JO 24	POSITION VECTOR (VELOCITY VECTOR (DELTA RADIUS DELTA VELOCITY	THE COVARIANCE MA	0.28416660E 01 0.12718450E 01 0.11645731E 00 0.26039363E-02 0.18152177E-02 0.24325862E-02

	0.75473341E 04	0.24369313E-01	0.48912405E 02	0.24751719E 02	0.45629190E 01	0.81486983E 02	-0.10796738E-02	-0.324713476-02
	11	Ц	Ħ	H	11	В	II	H
MENTS	(KM)		(DEG)	(DEG)	(DEG)	(DEG)	(RAD)	(RAD)
FLLIPTIC ORBIT ELEMENTS	SEMIMAJOR AXIS	ECCENTRICITY	TRUE ANOMOLY DATE	R ASC OF ASC NODE	ARG OF PERIAPSE	ORBIT INCLINATION	DEL NODE PER REV	DEL APSE PER REV

0.59001613E 0.44535230E

04 01

0.26519911E -0.18463847E

01

0.36428143E -0.55969653E

11 11

DATE! DATE!

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POSITICN VECTOR VELOCITY VECTOR

BEEN RECTIFIED

THE TRAJECTORY HAS

SEC (U.T.)	0.20358755E 02	SEC (U.T.)	0.19619360E 02
0.56925974E 05 0.59414060E 04 0.44017177E 01 0.59466669E 04 0.43935037E 01	0.16030345E 04 0.44017177F 01 0.44450987E 02	0.56935985E 05 0.59851826E 04 0.43436475E 01 0.59903610E 04 0.43353828E 01	0.16467286E 04 0.43436475E 01 0.43006824E 02
DAYS 0.26207690E 04 -0.18522642E 01 0.26327207E 04 -0.18711583E 01	0.12502594E 04 -0.21765605E 01 0.41210558E 01	DAYS 0.26020983E 04 -0.18776361E 01 0.26138602E 04 -0.18966453E 01	0.12281496E 04 -0.22018586E 01 0.42457848F 01
0.55950000E 04 0.36031685E 04 -C.56310672E 01 0.35857346E 04 -0.56312351E 01	-0.86148370E 03 -0.55302565E 01 0.22079453E 04	0.55950000E 04 0.35466199E 04 -C.56658001E 01 0.35291851E 04 -0.56657985E 01	-0.91702179E 03 -0.55647525E 01 0.22496656E 04
IIME FRGM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JO 2433282.5 = R VECTOR (1950) = V VECTOR (DATE) = V VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

			0.24386754E-02 0.12355961E-02 0.30309571E-03 0.23904566E-05 0.15447583E-05 0.24242312E-05	
AYS, DAYS) AYS U.T.)	0.59903381E 04 0.43348668E 01 0.22928023E-01 0.51598955E-03		2 0.17759021E-02 2 0.73543926E-03 3 0.19461011E-03 5 0.15023385E-05 5 0.13877516E-05 5 0.15447594E-05	0.59903381E 04 0.43348668E 01
0.73598132E 00 (D/ 0.55950000E 04 (D/	0.26135703E 04 -0.18969886F 01 -0.28988180E 00 -0	* d *	00 0.25136543E-0 01 0.12683913E-0 00 0.22633259E-0 03 0.24420849E-0 03 0.15023565E-0	0.26135703E 04 -0.18969886E 01
0.55950000E 04 0.56935985E 05	0.35286039E 04 -0.56653404E 01 -0.58125498E 00 -0.54191070E-03	E ERRORS IN STATE	01 0.16670163E 00 0.83717056E- 01 0.15755039E- 02 0.22632891E- 03 0.19460573E- 02 0.303C8565E	
EPUCH (REL. TO 1950.0) = EPOCH (REL. JO 2433282.5) =	POSITIUN VECTOR (DATE) = VELNCITY VECTOR (DATE) = DELTA RACIUS = DELTA VELOCITY =	THE COVARIANCE MATRIX FOR THE	7 4 2 4 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	THE TRAJECTORY HAS BEEN RECT POSITION VECTOR (R DATE) = VELOCITY VECTOR (V DATE) =

0.75441295E 04 0.24129352E-01 0.51175177E 02 0.24743707E 02 0.34623335E 01 0.81486699E 02 -0.10806019E-02

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ELLIPTIC ORBIT ELEMENIS

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SEC (U.T.)	0.18875207E 02	SEC (U.T.)	0.18141811E 02
0.56945976E 05 0.60304252E 04 0.42825333E 01 0.60355187E 04	0.16918864E 04 0.42825333E 01 0.41577024E 02	0.56955966E 05 0.60729177E 04 0.42238132E 01 0.60779279E 04	0.17342955E 04 0.42238132E 01 0.40270426E 02
DAYS 0.25822898E 04 -0.19020114E 01 0.25938564E 04 -0.19211317E 01	0.12049063E 04 -0.22261601E 01 0.43662043E 01	DAYS 0.25631628E 04 -0.19269179E 01 0.25745379E 04 -0.19461493E 01	0.11823493E 04 -0.22509928E 01 0.44760041E 01
0.5595CG00E 04 0.34884085E 04 -0.56993252E 01 0.347G9745E 04 -0.56991529E 01	-0.97422131E 03 -0.55980414E 01 0.22942070E 04	0.55950C00E 04 C.34313005E 04 -0.57328205E 01 0.34138691E 04 -0.57324793E 01	-0.10303137E 04 -0.56313005E 01 0.23382209E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYO OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R* RDOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R. ROOT, AZ, ELEV = UNDRFLOW AT 33550 IN MQ

		•24603880E-0	0.12510759E-02 0.35674149E-03 0.23694076E-05	.15491357E-0 .24861255E-0				
,DAYS) U.T.)	42150432E 01 28121101E-01 40736123E-03	.17479012E-0	0.73064370E-03 0.22603810E-03 0.14477700E-05	•13690418E-0 •15491370E-0		60778997E 04 42150432E 01		
.73621258E 00 (DA .55950000E 04 (DA	*19464139E 01 0* *22444469E 00 -0* *26465696E-03 -0*	0.244270525-0	0.12390401E 0.27263621E 0.23356424E	0.14477872E-0 0.23693988E-0		0.25743134E 04 0.1.19464139E 01 00.		
55950000E 04 56955966E 05	0.54134202E 04 0 0.57228903E 01 -0 0.44887463E 00 -0 0.41108603E-03 -0	0.21577582F O	0.11028972E 00 0.17051840E 00 0.27263264E-03	0.22603354E-0 0.35673125E-0	EO).34134202E 04 0		0.75407120E 04 0.23896959E-01 1.53578872E 02 0.24735458E 02 0.22157463E 01 0.81486210E 02 0.10816191E-02
33282.5) = 33282.5) = 504E	(DATE) = 0 (DATE) = -0 (DATE) = -0 (= -0	0 102683000	0.74213018E 00 0.74213018E 00 0.11028659E 00 0.12390195E-02	.12510747E-0	HAS BEEN RECTIFI	(R DATE) = 0 (V DATE) = -0	ELEMENTS	TE (DEG) = 0 DE (DEG) = 0 ON (DEG) = 0 V (RAD) = -0 V (RAD) = -0
POCH (RE: 15 POCH (RE: JE	VELOCITY VECTOR DELTA FILL DELTA VELOLITY THE COMMOTANCE		יש אישי	17475(27-0 24603896E-0	THE TOLLS TORY !	POSITION VECTOR VELOCITY VECTOR	ELLIPTIC ORBIT	SEMIMAJOR AXIS ECCENTRICITY TRUE ANOMOLY DA' R ASC OF ASC NOT ARG OF PERIAPSE ORBIT INCLINATIO DEL NODF PER REV

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SEC (U.T.)	0.17407458E 02	SEC (U.T.)	0.16683124E 02
35748E 05 69966E 04 19842E 01 19210E 04	'82886E 04 19842E 01 74083E 02	75989E 05 83655E 04 24017E 01 32054E 04 39450E 01	95730E 04 24017E 01 86582E 02
0.569 0.611 0.416 0.612 0.415	0.177 0.416 0.389	0.569 0.615 0.410 0.616	0.181 0.410 0.377
DAYS 0.25429144E 04 -0.19506815E 01 0.25540920E 04 -0.19700191E 01	0.11586608E 04 -0.22746823E 01 0.45816564E 01	DAYS 0.25232626E 04 -0.19752160E 01 0.25342461E 04 -0.19946609E 01	0.11355731E 04 -0.22991424E 01 0.46784109E 01
04 04 01 04 01	04 01 04	04 00 01 01	04 01 04
0.55950000E 0.33724666E -0.57648872F C.33550392E -0.57643763E	-0.1C881265E -0.56631307E 0.23851256E	0.55950000E 0.33145901E -0.57972717E 0.32971686E -0.57965919E	-0.11449776E -0.56952789E 0.24313259E
11 11 11 11 11	11 11 11		11 11 11
TIME FRGM JD 2433282. R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R. ROOT, AZ, ELEV	TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSÍTION RELATIVE VELOCITY R, ROOT, AZ, ELEV

UNDRFLOW AT 33550 IN MQ

(DAYS, DAYS)	0.61631596E 04 0.40934160E 01 -0.45720529E-01 -0.52893053E-03
000	п 04 п 01 п 00 п 00
0.73644432E 0.55950000E	0.25339565E -0.19949929E -0.28962828E -0.33204081E
04	00 00 -03
0.55950000E 0.56975989E	C.32965969E -C.57171763E -C.51526346E
p p	n 16 H H
1550.0 2433282.5)	(DATE)
101	ECTOR ECTOR US CITY
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THE COVARIANCE MATRIX FOR THE ERP.URS IN STATE ** P **

0.24955346E-02 0.12737991E-02 0.41219511E-03 0.23596441E-05 0.15609523E-05	
0.17287414E-02 0.73061915E-03 0.25703402E-03 0.14021140E-05 0.13553901E-05 0.15609537E-05	
0.23865334E-02 0.12170754E-02 0.31725331E-03 0.22448427E-05 0.14021304E-05 0.23596351E-05	
0.26485649E 00 0.13709713E 00 0.18549937E 00 0.31724988E-03 0.25702926E-03	
0.12586661E 01 0.74294309E 00 0.13709418E 00 0.12170551E-02 0.73061274E-03	
0.27603657E 01 0.12584732E 01 0.26486C95E 00 0.23865368E-02 0.17287435E-02	

THE TRAJECTORY HAS BEEN RECTIFIED

0.61631596E 04	0.40934160E 01
0.25339565E 04	
= 0.32965969E 04	
(R DATE)	(V DATE)
POSITICA VECTOR	VELOCITY VECTOR

ELLIPTIC ORBIT ELEMENTS

0.75369213E 04	0.23666219E-01 0.56106776E 02	0.24726917E 02	0.84623569E 00	0.81485578E 02	-0.10827633E-02	-0.32557619E-02
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(KW)	(DEG)	(DEG)	(050)	(DEG)	(RAD)	(RAD)
EMIMAJOR AXIS	CENTRICITY UE ANDWOLY DATE	() ()	3 OF PERIAPSE	NCL INATION	E PER REV	8 1 1 1

SEC (U.T.)	0.15961072E 02	SEC (U.T.)	0.15252904E 02
0.56985980E 05 0.62010805E 04 0.40399138F 01 0.62058337E 04	0.18622014E 04 0.40399138E 01 0.36611534E 02	0.56995971E 05 0.62411417E 04 0.39797414E 01 0.62458097E 04 0.39711944E 01	0.19021773E 04 0.39797414E 01 0.35535404E 02
DAYS 0.25025367E 04 -0.19983996E 01 0.251332C8E 04 -0.20179461E 01	0.11114114E 04 -0.2322516E 01 0.47708583E 01	DAYS 0.24824510E 04 -0.20224530E 01 0.24930393E 04 -0.20421027E 01	0.10878943E 04 -0.23462304E 01 0.48555809E 01
0.55950000F 04 0.32551435E 04 -0.58279692E 01 0.32377297E 04 -0.58271207E 01	-C.12033961E 04 -0.57257403E 01 0.24801595E 04	0.55950000F 04 0.31967621E 04 -0.58591014E 01 0.31793576E 04 -0.58580847E 01	-0.12607456E 04 -0.57566366E 01 0.25280965E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = P VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =	TIME FROM JO 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLCYD GBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROCT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

			0.25414236E-02 0.130247700-02 0.46983602E-03 0.23582447E-05 0.15785070E-05
'S,DAYS) 'S U.T.)	62457495E 04 39706247E 01 60177338E-01 56965912E-03		0.17162238E-02 0.73424805E-03 0.28782678E-03 0.13630696E-05 0.13454219E-05
.73667559E 00 (DAY.	.24927308E 04 0. .20424499E 01 0. .30849953E 00 -0. .34723013E-03 -0.	** ** C.	0.23413497E-02 0.12006158E-02 0.36056197E-03 0.21657198F-05 0.13630852F-05
.55950000E 04 0	.31787537E 04 0. .58586195E 01 -0. .60382378E 00 -0.	ERRURS IN STATE *	0.31438887E 00 0.16437305E 00 0.20247935E 00 0.36055870E-03 0.28782184E-03
1950.0) = 0. 2433282.5) = 0.	(DATE) = 0. (DATE) = -C. = -0.	MATRIX FOR THE E	0.12692693E 01 0.74733364E 00 0.16437028E 00 0.12005958E-02 0.73424172E-03
OEPOCH (REL. TO EPOCH (REL. JO	POSITICN VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.27622888E 01 0.12692763E 01 0.31439336E 00 0.23413535E-02 0.17162260E-02

0.62457495E	0.39706247E
0.24927308E 04	
0.31787537E 04	
11	11
(R DATE)	(V DATE)
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THE TRAJECTORY HAS BEEN RECTIFIED

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FLLIPTIC ORBIT ELEMENTS	
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(KM)	(DEG)	(DEG)	(RAD)
SEMIMAJOR AXIS ECCENTRICITY	TRUE ANGMOLY DATE	RG OF PERIAPSE RBIT INCLINATIO	EL NODE PER RE EL APSE PER RE

SEC (U.T.)	0.14545728E 02	sec (U.T.)	0.13853421E 02
0.57005982E 05 0.62826525E 04 0.39164737E 01 0.62872328E 04 0.39078839E 01	0.19436004E 04 0.39164737E 01 0.34465827E 02	0.57015993E 05 0.63215564E 04 0.38554908E 01 0.63260504E 04 0.38468571E 01	0.19824180E 04 0.38554908E 01 0.33485115E 02
DAYS 0.24612258E 04 -0.20450950E 01 0.24716123E 04 -0.20648419E 01	0.10632276E 04 -0.23687976E 01 0.49364479E 01	DAYS 0.24406331E 04 -0.20687580E 01 0.24508214E 04 -0.20886042E 01	0.10391932E 04 -0.23923854E 01 0.50107966E 01
0.55950000E 04 0.31365851E 04 -0.58884692E 01 0.31191917E 04 -0.58872845E 01	-0.13198851E 04 -0.57857681E 01 0.25787850E 04	0.55950000E 04 0.30774833E 04 -0.59184675E 01 0.30601025E 04 -0.59171148E 01	-0.13779439E 04 -0.58155299E 01 0.26284279E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROW JD 2433282.5 = R VECTOR (1950) = R VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLGYD OBSERVES PELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

			0.25969593E-02 0.13366604E-02 0.53044844E-03 0.23635036E-05 0.16009703E-05
(DAYS,DAYS) (DAYS U.T.)	.63259828E 04 .38463205E 01 .67545458E-01 .53660038E-03		0.17089784E-02 0.74090135E-03 0.31882355F-03 0.13289720E-05 0.13382444E-05
.73690733E 00 (DA) .55950000E 04 (DA)	4505349E 04 0 0889229F 01 0 8648026E 00 -0 1875257E-03 -0	* *	0.23045737E-02 0.11884237E-02 0.40315890E-03 0.20952898E-05 0.13289869E-05
.55950000E 04 0.7	.30595448E 04 0.2 .59175997E 01 -0.2 .55769007E 00 -0.2	THE ERRORS IN STATF **	0.36511265E 00 0.19252277E 00 0.22161837E 00 0.40315582E-03 0.31881843E-03
50.0) = 0. 33282.5) = 0.	DATE) = 0.3C DATE) = -0.59 = -0.55	MATRIX FOR THE ERRC	0.12852868E 01 0.75488210E 00 0.19252019E 00 0.11884039E-02 0.74089507E-03
EPOCH (REL. TO 199 EPOCH (REL. JO 24:	POSITION VECTOR (VELOCITY VECTOR (DELTA RADIUS	THE COVARIANCE MA	0.27743C38E 01 0.12852937E 01 0.36511715E 00 0.23045779E-02 0.17089807E-02

THE TRAJECTORY HAS BEEN RECTIFIED

0.63259828E 04	0.38463205E 01
0.24505349E 04	
= 0.30595448E 04	
(R DATE)	VECTOR (V DATE)
—	VELOCITY

ELLIPTIC ORBIT ELEMENTS

	ı			0.35768756E 03		ı	1
ļI	II	ļį	II	IJ	11	11	I
(KX)		(DEG)	(DEG)	(DEG)	(DEG)	(RAD)	
SEMIMAJOR AXIS	ECCENTRICITY	α	R ASC OF ASC NODE	ARG OF PERIAPSE	ORBIT INCLINATION	DEL NODE PER REV	APSE PFR

فسند استعد

SEC (U.T.)	0.13167846E 02	SEC (U.T.)	0.12495597E 02
0.57025984E 05 0.63616956E 04 0.37918120E 01 0.63661013E 04 0.37831378E 01	0.20224689E 04 0.37918120E 01 0.32514727E 02	0.57035975E 05 0.63992714E 04 0.37302997E 01 0.64035902E 04 0.37215835E 01	0.20599578E 04 0.37302997E 01 0.31622941E 02
DAYS 0.24190469E 04 -0.26907060E 01 0.24290321E 04 -0.21106443E 01	0.10141705E 04 -0.24142584E 01 0.50809469E 01	DAYS 0.23580434E 04 -0.21138736E 01 0.24078289E 04 -0.21339070E 01	0.98973959E 03 -0.24373508E 01 0.51458232E 01
0.55950000F 04 0.30169268E 04 -0.59463023E 01 0.29995603E 04 -0.59447832E 01	-0.14374562F 04 -0.58431289E 01 0.26805228E 04	0.29573751E 04 -0.59750364E 01 0.29400246E 04 -0.59733502E 01	-0.14959614E 04 -0.56716276E 01 0.27314668E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, 2DOT, AZ, ELFV =	TIME FPJM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

			0.26602697E-02 0.13754372E-02 0.59418154E-03 0.23734746E-05 0.16271736E-05 0.28526530E-05	
rs, DAYS) rs u.T.)	.64035130E 04 37210506E 01 77169575E-01 53281809E-03		0.17056391E-02 0.74985150E-03 0.35006001E-03 0.12984798E-05 0.13330193E-05 0.16271753E-05	
0.73713860E 00 (EAY 0.55950000E 04 (DAY	0.24075481E 04 0. 0.21342152E 01 0. 0.28086163E 00 -0. 0.30827842E-03 -0.	* * d	0 0.22739150E-02 0 0.11793265E-02 0 0.44508622E-03 3 0.20313035E-05 3 0.12984939E-05 3 0.23734652E-05 0.24075481E 04 0.	
0.55950000E 04 0.57035975E 05	0.29394812E 04 0.59738138E 01 - 0.54335234E 00 - 0.46364703E-03 -	ERRORS IN STATE	1 0.41716483E 00 0 0.22162971E 00 0 0.24294825E 00 2 0.44508334E-03 3 0.35005473E-03 2 0.59417071E-03 IED 1ED 0.29394812E 04 0	
1950.0) = 2433282.5) =	R (DATE) = R (DATE) =	: MATRIX FOR THE	0.13055612E 0 0.76503716E 0 0.22162733E 0 0.11793071E-0 0.74984529E-0 0.13754372E-0 R (R DATE) = -	
EPOCH (REL. TO EPOCH (REL. JO	POSITICN VECTO VELOCITY VECTO DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.27941307E 01 0.13055681E 01 0.41716933E 00 0.22739196E-02 0.17056415E-02 0.26602623E-02 THE TRAJECTORY POSITICN VECTORY	

0.75238893E 04 0.23084203E-01 0.64516151E 02 0.24699603E 02 0.35589520E 03 0.81482684E 02 -C.10868249E-02

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R ASC OF ASC NODE ARG OF PERIAPSE

ELLIPTIC ORBIT ELEMENTS

SEMIMAJOR AXIS ECCENTRICITY TRUE ANOMOLY DATE

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> ORBIT INCLINATION DEL NODE PER REV DEL APSE PER REV

-0.32666009E-02

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SEC (U.T.)	0.11829161E 02	SEC (U.T.)	0.11174927E U2
0.57045986E 05 0.64381857E 04 0.36659744E 01 0.64424153E 04 0.36572196E 01	0.20987829E 04 0.36659744E 01 0.30736872E 02	0.57055997E 05 0.64745754E 04 0.36037077E 01 0.64787171E 04 0.35949126E 01	0.21350847E 04 0.36037077E 01 0.29920804E 02
DAYS 0.23760089E 04 -0.21352338E 01 0.23855893E 04 -0.21553545E 01	0.96425844E 03 -0.24586353E 01 0.52068231E 01	DAYS 0.23545183E 04 -0.21579935E 01 0.23638969E 04 -0.21782055E 01	0.93933028E 03 -0.24813193E 01 0.52635906E 01
0.55950000F 04 0.28961942E 04 -0.60014846E 01 0.28788613E 04 -0.59956333E 01	-0.15560873E 04 -0.58978395E 01 0.27849760E 04	0.55950000E 04 0.28359731E 04 -0.60290644E 01 0.28186595E 04 -0.60270462E 01	-0.16152508E 04 -0.59251834E 01 0.28372457E 04
TIME FROM JO 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (5ATE) = V VECTOR (DATE) = C V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD CBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, CLEV = UNDRFLOW AT 33550 IN MQ

			0.27308683E-02 0.14186502E-02 0.66170630E-03 0.23871272E-05 0.16566702E-05			
S.DAYS) S U.T.)	64786158E 04 35942810E 01 10119842E 00 63149191E-03		0.17054219E-02 0.76074922E-03 0.38181201E-03 0.12706005E-05 0.13292280E-05	64786158E 04 35942810E 01		
.73737034E 00 (DAY	0.23635661E 04 0. 0.21785592E 01 0. 0.33075641E 00 -0.	* d. *	0.22478400E-02 0.11725832E-C2 0.48669498E-03 0.19719866E-05 0.12706140E-05	.23635661E 04 0.		
0.55950000E 04 0	0.28180265E C4 0. 0.60275764E 01 -0. 0.63294710E 00 -0.	ERRORS IN STATE *	1 0.47109100E 00 0 0.25200912E 00 0 0.26669639E 00 2 0.4866923E-03 3 0.38180656E-03 2 0.66169535E-03	IED 0.28180265E 04 0 0.60275764E 01 -0).75189818E 04).22947108E-01).67587916E 02).24685858E 02).35397396E 03).81431415E 02).10883912E-02
(950.0) = (433282.5) =	(DATE) = = - = - = - = - = - = - = - = -	MATRIX FOR THE	0.13296202E 0 0.77759086E 0 0.25200695E 0 0.11725639E-0 0.76074305E-0	S BEEN RECTIF R DATE) =	LEMENTS	(KM) = 0 E (DEG) = 0 E (DEG) = 0 (DEG) = 0 (RAD) = -0 (RAU) = -0
S EPOCH (REL. TO 1 EPOCH (REL. JO 2	POSITION VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE M	0.28206825E 01 0.13296272E 01 0.47109547E 00 0.22478449E-02 0.17054242F-02	THE TRAJECTORY HA POSITION VECTOR (VELOCITY VECTOR (ELLIPTIC ORBIT EL	SEMIMAJOR AXIS ECCENTRICITY TRUE ANGMOLY DATE R ASC OF ASC NODE ARG OF PERIAPSE ORBIT INCLINATION DEL NODE PER REV DEL APSE PER REV

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SEC (U.T.)	0.10528636E 02	SEC (U.T.)	0.98951340E 01
0.57065988E 05 0.65120873E 04 0.35389320E 01 0.65161391E 04 0.35301003E 01	0.21725067E 04 0.35389320E 01 0.29112322E 02	0.57075979E 05 0.65471306E 04 0.34761954E 01 0.65510939E 04 0.34673253E 01	0.22074615E 04 0.34761954E 01 0.28366888E 02
DAYS 0.23320814E 04 -0.21787177E 01 0.23412533E 04 -0.21990123E 01	0.91345622E 03 -0.25019677E 01 0.53164006E 01	DAYS 0.23102031E 04 -0.22009692E 01 0.23191718E 04 -0.22213507E 01	0.88814537E 03 -0.25241432E 01 0.53657981E 01
0.55950000E 04 0.27743398E 04 -0.60540934F 01 0.27570471F 04 -0.60519114E 01	-0.16758238E 04 -0.59499767E 01 0.28918113E 04	0.55950000E 04 0.27137234E 04 -0.6C803999E 01 0.26964533E 04 -0.60780520E 01	-0.17353762E 04 -0.59760478E 01 0.29450329E 04
TIME FRGW JD 2433282*5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) = V	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE) =	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV = UNDRFLOW AT 33550 IN MQ

			0.28073461E-0 0.14655994E-0 0.73303183E-0 0.24030724E-0 0.16885930E-0	
S,DAYS) S U.T.)	65509799E 04 34666896E 01 11399805E 00 63567116E-03		0.17074236E-02 0.77308425E-03 0.41400997E-03 0.12445227E-05 0.13263307E-05 0.16885950E-05	65509799E 04 34666896E 01
0.73760161E 00 (DAY 0.55950000E 04 (DAY	0.23188438E 04 0.0.22216987E 01 0.0.32805193E 00 -0.0.34802775E-03 -0.	** d **	0 0.22248905E-02 0 0.11674189E-02 0 0.52784925E-03 3 0.19160357E-05 3 0.12445355E-05	0.23188438E 04 0.
0.55950000E 04 0.57075979E 05	0.26958279E 04 0.60785654E 01 0.62534335E 00 0.51340857E-03	ERRORS IN STATE	1 0.52685765E 0 0 0.28365953E 0 0 0.29290930E 0 2 0.52784684E-0 3 0.41400436E-0 2 0.73302075E-0	0.26958279E 04 0.60785654E 01 -
0 1950.0) = D 2433282.5) =	OR (DATE) = - OR (DATE) = - '	E MATRIX FOR THE	1 0.13565470E 0 0.79214962E 0 0.28365757E 0 2 0.11673999E-0 2 0.77307814E-0 2 0.14655999E-0 Y HAS BEEN RECTIF	OR (R DATE) = -
© EPOCH (REL. TO EPOCH (REL. JD	POSITION VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.28523985E 01 0.13566539E 01 0.52686207E 00 0.22248958E-02 0.17C74260E-02 0.28073385E-02	POSITICN VECTOR VELOCITY VECTOR

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SID 65-1203-1

0.75138331E 04 0.22849821E-01 0.70782543E 02 0.24679902E 02 0.35192522E 03 0.81479989E 02 -0.10900547E-02

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SEMIMAJOR AXIS ECCENTRICITY

ELLIPTIC ORBIT ELEMENTS

(DEG) (DEG) (DEG) (DEG) (RAD)

TRUE ANOMOLY DATE
R ASC OF ASC NGDE
ARG OF PERIAPSE
ORBIT INCLINATION
DEL NODE PER REV

SEC (U.T.)	0.92694284E 01	SEC (U.T.)	0.86549325E 01
0.57085969E 05 0.65833217E 04 0.34109822E 01 0.65871945E 04	0.22435621E 04 0.34109822E 01 0.27626917E 02	0.57095960E 05 0.66170837E 04 0.33476773E 01 0.66208674E 04 0.33387361E 01	0.22772350E 04 0.33476773E 01 0.26942994E 02
0.22873874E 04 -0.22210473E 01 0.22961480E 04 -0.22415067E 01	0.86189261E 03 -0.25441453E 01 0.54113708E 01	DAYS 0.22650886E 04 -0.22428306E 01 0.22736444E 04 -0.22633729E 01	0.83616104E 03 -0.25658573E 01 0.54543703E 01
0.55950000E 04 0.26516435E 04 -0.61039841E 01 0.26343975E 04 -0.61014740E 01	-0.17963881E 04 -0.59993965E 01 0.30005733E 04	0.25950000E 04 0.25905346E 04 -0.61290687E 01 0.25733145E 04 -0.61263936E 01	-0.18564248E 04 -0.60242457E 01 0.30547140E 04
TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, RDOI, AZ, ELEV =	TIME FROM JD 2433282.5 = R VECTOR (1950) = V VECTOR (1950) = R VECTOR (DATE) = V VECTOR (DATE)	FLOYD OBSERVES RELATIVE POSITION = RELATIVE VELOCITY = R, ROOT, AZ, ELEV =

UNDRFLOW AT 33550 IN MQ

(DAYS, DAYS)	0.56207682E 04 0.33382370E 01 -0.99179737E-01 -0.49910284E-03
0.73783287E 00 0.55550000E 04	0.22733910E 04 -0.22636406E 01 -0.25341403E 00 -0.26774046E-03
0.55950000E 04 0.57095960E 05	0.25728327E 04 -0.61267809E 01 -0.48185023E 00 -0.38733633E-03
11 11	11 ti 11 fl
EPOCH (REL. TO 1950.0) EPOCH (REL. JD 2433282.5)	POSITION VECTOR (DATE) VELOCITY VECTOR (DATE) DELTA RADIUS

THE COVARIANCE MATRIX FOR THE ERRORS IN STATE ** P **

0.28892790E-02 0.15161323E-02 0.80860316E-03 0.24205223E-05 0.17225761E-05 0.32287317E-05
0.17111127E-02 0.78660216E-03 0.44678042E-03 0.12196247E-05 0.13239851E-05 0.17225783E-05
C.220405785-02 0.11633261E-02 0.56866270E-03 0.18623793E-05 C.12196369E-05 0.24205127E-05
0.58477246E 00 0.31677339E 00 0.32179832E 00 0.56866053E-03 0.44677467E-03
0.13862959E 01 0.80856143E 00 0.31677166E 00 0.11633073E-02 0.78659612E-03
0.28885162E 01 0.13863029E 01 0.58477682E 00 0.22046633E-02 0.17111152E-02

THE TRAJECTORY HAS BEEN RECTIFIED

04	01
0.66207682E	0.33382370E
0.22733910E 04	
0.25728327E 04	
11	Ħ
(R DATE)	(V DATE)
VECTOR	VECTOR
NOI.	X11

ELLIPTIC ORBIT ELEMENTS

0.75085379E 04	T L	ш	m	m	m	Ë.	
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(XX)		(DEG)	ш	9	(DEG)	⋖	(RAD)
RA	ECCENTRICITY	TRUE ANGMOLY DATE	R ASC OF ASC NODE	OF PERIA	ORBIT INCLINATION	DEL NODE PER REV	L APSE PER RE

TIME FROM JO 2433282.5 R VECTOR (1950) V VECTOR (1950) P VECTOR (DATE) V VCCTOR (DATE)	8 11 11 11 11	0.55950000E 04 0.25280493E 04 -0.61511484E 01 0.25108563E 04 -0.61483129E 01	DAYS 0.22419344F 04 -0.22622258E 01 0.22562808E 04 -0.22828409E 01	0.571C5971E 05 0.66520438E 04 0.32820832E 01 0.66557363E 04	SEC (U.T.)
FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY R; RCOT, AZ, ELEV	0 11 11	-0.15178329E 04 -0.60460898E 01 0.31111579F 04	0.80956525E 03 -0.25851709E 01 0.54934669F 01	0.23121039E 04 0.32820832F 01 0.26264058E 02	0.80506172F 01
TIME FROM JD 2433282.5 R VECTOR (1950) V VECTOR (1950) R VECTOR (DATE) V VECTOR (DATE)	0 0 0 0	0.55950000E 04 0.2466348?E 04 -0.61750538E 01 0.2491844E 04 -0.61720536E 01	DAYS 0.22191795E 04 -0.22835775E 01 0.22273191E 04 -0.23042715F 01	0.57115982E 05 0.66845818E 04 0.32181C89E 01 0.66881843E 04 0.32091006E 01	SEC (U.T.)
FLOYD OBSERVES RELATIVE POSITION RELATIVE VELOCITY RELATIVE AZ; ELEV	ų u ų	-0.15784524E 04 -0.60697595E 01 0.31662075E 04	0.78337245E 03 -0.26064458E 01 0.55308869E 01	0.23445519E 04 0.32181089E 01 0.25633863E 02	0.74532810E 01

UNDRICON AT 33550 IN MQ

			0.29763720E-02 0.15701654E-02 0.88887890E-03 0.24388036E-05 0.17583256E-05
(S, DAYS) (S U.T.)	.66880309E 04 .32083800E 01 .15333930E 00 .72058519E-03		0.17160612E-02 0.80110061E-03 0.48023167E-03 0.11954026E-05 0.13219129E-05 0.17583279E-05
.73806462E 00 (DAYS.).55950000E 04 (DAYS	0.22269554E 04 0.3.23046460E 01 0.3.36373093E 00 -0.3.37457054E-03 -0.	* * C. *	0.21845135E-02 0.11598835E-02 0.60920359E-03 0.18101612E-05 0.11954141E-05
0.55950000E 04 0 0.57115982E 05 0	0.24484998E 04 0. 0.61725928E 01 -0. 0.68452439E 00 -0. 0.53930064E-03 -0.	ERRORS IN STATE *	0.64512777E 00 0.35154020E 00 0.35361003E 00 0.60920168E-03 0.48022576E-03
1950.0) = 0 2433282.5) = 0	(DATE) = = - = - = - = - = - = - = - =	MATRIX FOR THE E	0.14183081E 01 0.82672034E 00 0.35153871E 00 0.11558649E-02 0.80109463E-03
EPOCH (REL. TO EPOCH (REL. JD	POSITION VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.29284455E 01 0.14183152E 01 0.64513206E 00 0.21845193E-02 0.17160638E-02

FI FMFNTS	
ORBIT	
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0.66880309E 0.32083800E

04

0.22269554E -0.23046460E

04

0.24484998E -0.61725928E

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DATE) DATE)

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POSITICN VECTOR VELOCITY VECTOR

BEEN RECTIFIED

THE TRAJECTORY HAS

Ī	0.77514470E 02	.34747976E	.81476669E	Ĭ	2842571E-
31 11	11 11	- 11	11	H	11
(KM)	(DEG)		(DEG)	(RAD)	(RAD)
SEMIMAJOR AXIS ECCENTRICITY	E ANOMOLY	RG OF PERIAPSE	ORBIT INCLINATION	R	R E

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FROM JD	11 11	0.55950000E 04 0.24033921E 04	AYS ,	0.57125973E 05 0.67180969E 04	SEC (U.T.)
ECTOR (1950	ļI	.61958063E	2	.31520803E 0	
ECTOR (DATE	iı	3862588E	.22035378E	.67216075E 0	
ECTOR (DATE	ļī	1926469E	3231426E	•31430416E 0	
OBSERVES					
ELATIVE POSITIO	t!	0403247E 0	.75636525E 0	.23779752E 0	
ELATIVE VEL	П	902	26251719E 0	.31520803E 0	
R RDOT, AZ, ELE	11	•32233180E 0	•55644903E	5009328E	0.68656973E 01
E FROM JD 2	1	5950000E 0	DAYS ,	.57135964E 0	SEC (U.T.)
ECTOR (1950)	11	.23413782E 0	1725026E	.67492671E 0	
ECT3R (1950	H	*62184300E 0	.23232068E	*30877265E 0	
VECTOR (DATE)	ļI	242773E 0	1802234E	526873F 0	
ECTOR (DATE	II	2151073E	.2344043	.307865	
OBSERVES					
ELATIVE POSITIO	H	1012506E 0	2982600E 0	.24090549E 0	
ELATIVE VE	H	-0.61126654E 01	-0.26439214E 01	0.30877265E 01	
, ROOT, AZ, ELE	Ħ	2789397E 0	5968342E 0	.24429651E 0	0.62872173E 01
DRFLOW AT 32550 IN MO	C				

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- 543 -SID 65-1203-1

			0.30675610E-02 0.16271526E-02 0.97373145E-03 0.24569732E-05 0.17952075E-05	
YS•DAYS) YS U.T.)	.67525285E 04 .30779629E 01 .15871855E 00 .69188405E-03		0.17217255E-02 0.81623724E-03 0.51420925E-03 0.11714614E-05 0.13198104E-05 0.17952099E-05	.67525285E 04 .30779629E 01
0.73829588E 00 (DA)	0.21798783E 04 00.23443948E 01 00.34512861E 00 -00.35106403E-03 -0.	**	00 0.21654515E-02 00 0.11566306E-02 00 0.64920136E-03 0.17588192E-05 0.11714722E-05 0.24569636E-05	0.21798783E 04 0.
0.55950000E 04	0.23236313E 04 -0.62156053E 01 -0.64597639E 00 -0.49801426E-03	ERRORS IN STATE	01	0.23236313E 04 -0.62156053E 01 -
1950.0 ; = 2433282.5} =	R (DATE) = .	MATRIX FOR THE	0.14521262E 0.84635054E 0.38788431E 0.11566122E- 0.81623130E- 0.16271538E-	(R DATE) = (V DATE) =
EPOCH (REL. TO EPOCH (REL. JD	POSITION VECTOR VELOCITY VECTOR DELTA RADIUS DELTA VELOCITY	THE COVARIANCE	0.29711736E 01 0.14521333E 01 0.76775190E 00 0.21654574E-02 0.17217281E-02 0.30675534E-02	POSITION VECTOR VELOCITY VECTOR

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5.0 CONCLUSIONS AND RECOMMENDATIONS

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The program described in the previous pages is an accurate and efficient tool for estimating the trajectory of a satellite traveling about the earth. There are, however, several features which should be incorporated in the program to extend the number of applications and to further enhance the accuracy. The most important of these are itemized below (not in the order of importance).

- The present program prints at intervals determined by the step size employed for the numerical integration. This mode of operation is completely adequate for applications of the type of the sample problem. However, should the program be applied to general trajectory problems (a simple task implemented by replacing the present subroutine DATAPE with a dummy which reads an end time and the subroutine FILTER with a routine which terminates operation if called), prints at regular prescribed intervals would normally be required, thus, an alternate logic for this application is recommended.
- The present logic employed in the integration cycle involves restarting the integration with the most recent values of \vec{r} and \vec{v} at those times when the step size has been changed. An improved logic would be to use the updated differences and sums for an epoch 3 steps before the most recent point to reevaluate the \vec{r} and \vec{v} at the time in the past using the central difference formula for integration. This procedure would assure that errors introduced in the extrapolation of \vec{r} and \vec{v} could be controlled to a higher degree.
- The present starter routine for the numerical integration is a 4th order Runge-Kutta. This routine provides a series of values of r, v and a which are differenced and summed to construct the table required in the Gauss-Jackson stepping. However, the Gauss routine operating with the predictor cycle done is a more precise routine than the R-K starter. Thus, if extreme precision is desired, the difference table provided by the start cycle must be corrected. This correction could be achieved by assuming the 6th difference is constant, constructing the missing differences back to ro, vo, and employing the central difference formula for reestimating the values of r and v to be used for the difference table.
- The constants of the math model (the coefficients of the potential function, the gravitational constant, the quantity CDA/M, etc.) could be estimated at the same time the state is being differentially corrected to adjust for slight bias errors. This mode of operation would assure that the trajectory could be estimated to a higher degree of precision than presently obtainable. Alternate logic would, of course, be required to determine when sufficient information was available in the data to make such a process convergent.

- 5) The present logic makes no attempt to correct the raw data for any known biases, for biases of the type displayed in Figures 2 and 5 (discussed in the sample problem), for time of signal propagation, for refraction, etc. Thus, these effects must be reflected in the data prior to processing in the PREPROCESSOR. Slight modification of the preliminary logic could, however, effect this correction and save considerable effort at the recording station. Thus, if corrections to the data are worthy of inclusion, these changes must be made.
- 6) Some editing of the raw data is presently accomplished (the observations are made "continuous" functions of time; e.g., if the data are increasing toward 2 m and a value of slightly more than zero is encountered, adjustment will be made to assure that all data fall near some continuous curve before smoothing). However, no editing to determine if time is recorded properly is attempted. Several tests of this latter nature should be devised to discard the bad data points so that the possibility of effecting the smoothed data files can be disregarded (see the discussion of the preliminary processor in the sample problem).
- 7) The present system of providing the input data might conceivably be revised to simplify operation. Particular attention should be directed to the manner in which time is input. This data could be provided in a more straightforward manner in the form of year, month, day, hour, second, or Julian date.

Other modifications would of course be required to allow lunar and planetary trajectories to be analyzed. These modifications would all stem from the inclusion of an accurate ephemeris routine and the logic necessary to produce information in other coordinate systems. Should this task be adjudged worthy of attention, simultaneous effort should be directed toward the inclusion of midcourse guidance logic so that simulations of true trajectories and studies of trajectory shaping can be effected with efficiency.

The application of this program to real problems (such as that which was attempted in the sample) requires precise data for the station, for the station errors, for the noise, and for the observations (this latter point was discussed in items 5 and 6). However, no means is provided within the logic as a check on these data. Thus, it is considered essential that the Facility be periodically calibrated against the remainder of the tracking network, and that the results of this calibration be utilized in preference to assumed data of the type built into subroutine TMPNT.

Finally, it is recommended that another sample problem be prepared. This new sample should utilize precisely reduced observed data (of all six types permissible) from several tracking stations (acquired over a period of several orbits), precise station data, precise noise data, and precise error data for the station's position. Only in this manner can a final check be performed.

APPENDIX I

CØMMØN

CØMMØN data storage is affected through the facility of labeled (non-blank) and unlabeled (blank) CØNMØN, A detailed description of the contents of both storage facilities is contained within this section.

Blank CØMMØN Map.

A blank (unlabeled) CØMMØN section is utilized as the principal means of communication between the various subprograms. This section, specified by the 525 element DATA array, is composed of the following five subarrays.

- CØN: A 15 element subarray, loaded at DATA (1), containing program constants and conversion factors.
- SAT: A 20 element subarray, loaded at DATA (16), containing data pertaining to the satellite at the initial epoch.
- SDA: A 250 element subarray, loaded at DATA (36), containing data pertaining to the tracking stations.
- STT. A 105 element subarray, loaded at DATA (286), containing statistical information and related data for the satellite.
- WRK: A 135 element subarray loaded at DATA (391). The primary function of the array is to act as a "scratch paper" or working array for communication between the various subroutines.

The following map, which describes the blank CONMON region in detail, utilizes standard FORTRAN nomenclature with a single exception. When a description refers to a series of locations in a DATA subarray (usually time), an abbreviated notation is used, in that, reference to the two cells WRK (50) and WRK (51) is written WRK (50,51). From the context, it will be apparent that WRK (50,51) is not a single element of a double subscripted array.

Description	Equatorial radii for reference ellipsoid. (Km) Polar radii for reference ellipsoid. (Km) Second coefficient of Jeffrey's potential function. Third coefficient of Jeffrey's potential function. Fourth coefficient of Jeffrey's potential function. Earth gravitational constant (Km ² /sec ²) Luna: gravitational constant (Km ² /sec ²) Solar gravitational constant (Km ² /sec ²) Astronomical unit. (Km) Conversion factor, mean solar days to sec. Conversion factor, degrees to radians Logical system input tape drive unit Logical system output tape drive unit	Satellite mass (K£) Cross sectional area of spherical satellite (M²) Satellite drag coefficient Satellite surface reflectivity Fosition and velocity vectors (or orbital elements) in the true equator of date frame at the initial epoch. See SAI (13), (Km-sec degree units) Whole day Whole day Time referenced to J. D. 2433282.223 (day). Indicator defining SAI (5) - SAI (10). I, cartesiar vectors. 2, Orbital elements. Indicates whether each station is to be checked at each integration step. 1, yes. 2, no.
FØRTRAN Names	RE RPØL CØEFJ, CJ CØEFH, CH CØEFD, CD GMERTH, GM, GME ØMEGA GNUØØN, UN, GMM GMSUN, US, GMS AU, REF CØNVZ NIN NØUT	SKASS AREA, 41 CD REFLEY, R1 RVEC (1), R (1) RVEC (2), R (2) RVEC (2), R (3) VVEC (1), V (1) VVEC (2), V (2) VVEC (2), V (2) VVEC (2), V (2) VVEC (2), V (2) VVEC (3), V (3) CHECK CHECK
ay Subarray	CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC	SAT (7) SAT (7) SAT (7) SAT (4) SAT (7) SAT (6) SAT (10) SAT (11) SAT (12) SAT (12) SAT (12)
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	Description	Indicates whether all stations are to be checked at the	<i>(</i> () ()	COMMON); O = no dump; non zero = dump Fixed point equivalent of SAT (14) Fixed point equivalent of SAT (15) Not used Not used	Latitude, first station Longitude, first station Altitude, first station Station name, first station Latitude, second station Latitude, second station	Station name, tenth station First station Horizon corrections for	Tenth station	Latitude variance, first station Longitude variance, first station Altitude variance, second station Longitude variance, second station Longitude variance, second station Longitude variance, second station Position error for each) Altitude variance, tenth station (station (rad2, rad2, Km2) Not used	C) Not used
FØRTRAN	Names	GØNØ	CODUMP	кснеск Nøgø	STATN (1) STATN (2) STATN (3) STATN (4) STATN (5)	STATN (40) HØRCØR (1)	HØRCØR (10)	STERR (1) STERR (2) STERR (3) STERR (4) STERR (5)	: STERR (30) STERR (31) :	STERR (90)
Array	Subarray	SAT (15)	SAT (1 6)	SAT (17) SAT (18) SAT (19) SAT (20)	SDA (1) SDA (2) SDA (3) SDA (4) SDA (5)	SDA (41) SDA (41) :	\mathcal{O}	SDA (51) SDA (52) SDA (53) SDA (54) SDA (55)	SDA (80) SDA (81)	SDA (140)
	DATA Location	30	31	33 83	37 37 39 40 40	75 ::	85	88 88 90 ••	115 311 :	175

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215 216 275 275 276	SDA SDA SDA SDA SDA	(180) (181) (240) (241)	SNØISE (40) SNØISE (41) SNØISE (100) NUMBEL	Elevation variance, tenth station rad ²) Not used Number of tracking stations employed Not used Number of tracking stations employed if
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3339 345 348 99 99		(57) (67) (67) (67)	~ こ 	Covariance matrix for contribution of errors in cbser and of errors in station location at the time WRK (61 Vector of position - velocity differentials at the tiwe WRK (42, 43) Km, Km/sec.
ない ひい ひ ひ ひ ひ	STE	(70) (105)	STATE (6) TP (1,1), P (1,1) PP (6,6), P (6,6)	Covariance matrix for errors in the estimates of the vector at time WRA $(61,62)$

Description		Transformation matrix, and its inverse, relating true equator of date frame of reference to the mean equincx	of $\dot{r}_{\rm D}$ = ROTATE $\dot{r}_{\rm so}$)	Nutation array relating the mean equator of date to the true equator of date ($\vec{\Gamma}_D = EN - \vec{\Gamma}_M \rangle$	1) Position and velocity vectors used to describe the conic s) reference trajectory (frame of 1950.0) at the most 1) recent rectification. Epoch defined by WRK (34, 35)	Whole day Epoch corresponding to the radius and Fractional day reference ellipse (days)	Position and velocity vectors utilized to define the state from which errors will propagate to the time of data acquisition. These vectors are in the true equator of data frame (Km, Km/sec)
FØR: RAN Names	RØTATE (1,1), AN (1,1)		røtinv (3,3)	$ EN (1,1) $ $ \vdots $ $ EN (3,3) $	RCØN(1), RCØ(1), RCØNIC(1 RCØN(2), RCØ(2), RCØNIC(2 RCØN(3), RCØ(3), RCØNIC(3 VCØN(1), VCØ(1), VCØNIC(1 VCØN(2), VCØ(2), VCØNIC(2	vcpn(3), vcp(3), vcpnlc(3) Tcgnw, Twcgn TcgnF, TFcgn	RTRAN(1), RTRANS(1) RTRAN(2), RTRANS(2) RTRAN(3), RTRANS(3) VTRAN(1), VTRANS(1) VTRAN(2), VTRANS(2)
	Subarray WRK (1)	: WRK (9) WRK (10)	WRK (is)	WRK (19) : WRK (27)	WRK (28) WRK (29) WRK (30) WRK (31) WRK (32)		WEK (36) WEK (37) WEK (38) WEK (39)
Array	DATA Location	366 366 700 700 700	÷ 708	409	418 419 420 421 422	423 424 425	426 427 429 430

Description		The epoch defining the point from which day errors will be propogated (days)	position and velocity vectors in the frame of	1950.O corresponding initially to SAT (5) and SAT (8) at the epoch defined by WRK (50,51) (Km, Km/sec.)				Whole day Days from J. D. 2433283.423 (1950.0)	Instantaneous satellite position	(Km)		Inctontoneous satellite welceitw and accelenation	vectors, relative to the reference conic, in the frame		
De		Whole day Fractional day	Satellite	1950.0 cor at the epo				Whole day	Instantane	•			vectors, r	00000	
FØRTRAN Names		7. C.	J.J.O.	ノーー	V50(1), VVEC(1), V(1), VEL(1), VEL(1), VEL(1)	SO	ノヘノヘ		DR(1),R(1),DELTA(1),	X(1) DR(2), R(2), DELTA(2), X(2)	DR(3),R(3),DELTA(3),	DV(1), RD(1), DRDØT(1),	ノヘノヘ	$DV(5)$, $RD(5)$, $DRD\phi T(5)$,	
Array	Subarray	WRK (42) WRK (43)	WRK (44) WRK (45)	WRK (46)	WRK (47)	WRK (48)	WRK (49)	WRK (50)	(52)	WRK (53)	WRK (54)	WRK (55)	WRK (56)	WRK (57)	WRK (58) WRK (59) WRK (60)
1	DATA Location	432	434 435	436	437	438	439	440	441	443	444	445	446	447	448 449 450

PØRTRAN Names Subarray Location TATE

Pracking station latitude (Geodetic) longitude and altitude (rad, rad, Km) SLAL SLØN SALT, H U(1), X(1) U(2), X(2) U(3), X(3) 106 107 (105)WRK WRK WRK WRK WRK.

,RVEC(1) RDATE(1)

(109) (۲۰۲۱)

667 667 667 667

50.7

Instantaneous position and velocity vectors in the true equator of date frame $(ext{Km, Km/sec})$

), RVEC(3)), VVEC(1)

RDATE(3) $\mathtt{VDATE}(\mathtt{l})$

113,

WRK WRK WRK WRK WRK WRK WEK **WRK** MRK WRK

502 503

114

504 505

 $\mathtt{RDATE}(2)$, $\mathtt{RVEC}(2)$

112)

VDATE(2), VVEC(2) VDATE(3), VVEC(3)

VDATE(3),

116)

115

), RC (1)

RCØNIC(3)

119)

VCØNIC(1

120

RCØNIC(2)

RCØNIC(1

117 118) , VC(2)

rcønic(2)

121

rcønic (3)

122

512 512 513

123

Up unit vector at the tracking station being checked.

True equator of date frame of reference.

Position and velocity vectors on the conic reference trajectory at the epoch (WRK (50,51))

of ~|v Step size employed by the Runge-Kutta starter WRK [68])

East unit vector at the tracking station being checked True equator of date frame. North unit vector at the tracking station being checked. True equator of date frame.

Array of constants utilized to define the conic reference trajectory

), A(2)

ELEM(2), ELEM(3), ELEM(1

> 132) 133)

WRK WRK WRK WRK WRK

131,

ELEM(4), A(4)

NSTEPS.

134

Number of integration steps from one data point to the next. Not used

508 508 508 508 509 510

),Y(1)),Y(2)),Y(3)

E(2) E(3) E(2)

125) 126) 127)

124)

WRK WRK 2(3)

WRK

514 517 517 517 518 518 520 521 522 522

128) 129) 130)

WRK WRK WRK

Labeled CØMNØN MAP

In addition to blank CØMMØN, CØMMØN storage utilized by the program includes three regions of labeled CØMMØN. These latter regions, containing tabulated atmospheric and ephemeris data, are set at load time by means of a BLØCK DATA subprogram. These regions are explicitly accessed by subroutines ATMS and EPHEM exclusively. A description of the data stored in the labeled CØMMØN regions is tabulated below.

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APPENDIX II

PROGRAM INPUT/OUTPUT TAPES

The program logic has been constructed in such a manner that variable input/output tape numbers can be employed so that operation on any system with a basic FORTRAN capability will be possible with a minimum of effort. This mode of operation has been provided by placing the desired tape numbers in COMMON [CON(16), CON(17)] while loading subroutine INPUT and calling for them in each routine requiring input or output.

Unfortunately, due to problems of checkout with the present NAASYS system, it was necessary to revise this logic and insert the actual tape units utilized in each routine.

INPUT	tape	unit	5
OUTPUT	tape	unit	6
SPECIAL	tape	unit	9

The linkage to COMMON was not, nowever, removed. Thus, if sufficient CORE exists to allow communication with each tape unit in this mode, the capability should be reinstated to assure complete compatibility of the program with all FORTRAN systems and to avoid problems associated with updating or changing the system.

For the sake of reference, the locations of all input/output statements in the program are listed below.

SUBROUTINE
MAIN INPUT REED SICRD DADUMP ATMS TRAK UPSTAT DATAPE ATANS CHOOSE

The preceding comments pertain only to those systems for which the use of control cards (in the binary deck) to equivalence the addresses of the tape units requested and those actually utilized is not permitted. However, if such operation is possible, this "fix" is by far the simplest remedy.

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13. ABSTRACT					

This document presents the formulation, computational logic and coding information developed for the purpose of effecting the definition of geocentric satellite orbits. The rationale for this process is constructed around the recursive minimum variance data filter developed by R. E. Kalman and a specially prepared magnetic tape generated in the preprocessor (SID 65 1203-2).

The trajectory portion of the program is formulated in the Encke manner and includes perturbing accelerations resulting from the first 3 harmonics of the Earth's potential function, atmospheric drag, solar radiation pressure, and solar and lunar gravitation. These accelerations are integrated via an uncorrected Gauss-Jackson routine started with a fourth order Runge-Kutta process.

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Security Classification

4.	LINK A		LINK B		LINK C	
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Orbit analysis, orbit differential correction, satellite tracking program						
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